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JUL 79 R R JOHNSTON, D E STEVENSON, W A ARON

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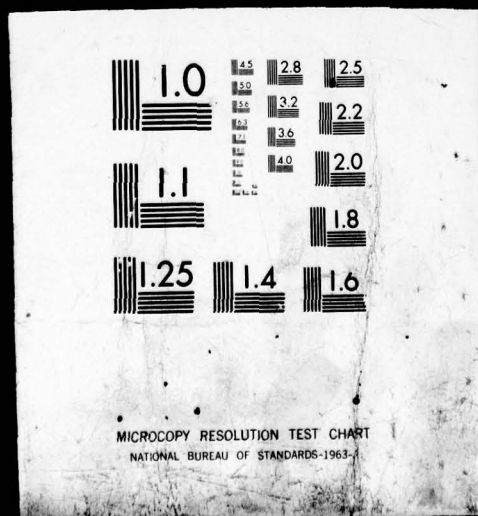
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Volume 24 — Natural Clouds

(Physical and Optical Properties and Statistics)

Science Applications, Inc.
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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The effect of natural clouds on IR observables from nuclear explosions is modeled for the wavelength range from 2 to 5 microns. A computer code for use with the ROSCOE-IR main program is provided to allow evaluation of the radiance resulting from transmission and reflection by natural clouds. Mie scattering cross-sections are calculated and used to generate transport cross-sections and bidirectional reflectance coefficients. Cloud transmission is treated by diffusion. A deterministic model allows the user to		

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18. SUPPLEMENTARY NOTES (Continued)

Incorporation of the Natural Cloud Model into ROSCOE-IR has led to a few differences in the coding, including:

1. The deletion of subroutine CLOUD1 in ROSCOE-IR and placement in subroutine CLDGEOM of calls to entry point CLDETOC in subroutine CLOUD9.
2. The recent establishment in the Cloud Model of a new subroutine CONVERT and the incorporation of the previous subroutines CTTOPOL and POLTOCT as entry points therein (a change not adopted in ROSCOE-IR).
3. The retention in ROSCOE-IR of the older name ALBEDO for a subroutine renamed CLDBDR in the Cloud Model.
4. The replacement of the calculation of the emission radiance in the deterministic cloud submodel by the calculation of only the emissivity, resulting in the deletion in subroutine CLOUD3 of PLANK(AA,TT) as an arithmetic function and as a factor in computing ESAVE and EMISS (each occurs twice). ROSCOE-IR has left the calculation of the emission radiance unaltered in the statistical cloud submodel.

20. ABSTRACT (Continued)

specify the cloud geometry. A statistical model allows selection of geographic weather averages and generates the probability distribution in radiance coefficients. Solar radiation and natural cloud thermal emission are treated.

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Conversion factors for U.S. customary
to metric (SI) units of measurement.

To Convert From	To	Multiply By
angstrom	meters (m)	1.000 000 X E -10
atmosphere (normal)	kilo pascal (kPa)	1.013 25 X E +2
bar	kilo pascal (kPa)	1.000 000 X E +2
barn	meter ² (m ²)	1.000 000 X E -28
British thermal unit (thermochemical)	joule (J)	1.054 350 X E +3
calorie (thermochemical)	joule (J)	4.184 000
cal (thermochemical)/cm ²	mega joule/m ² (MJ/m ²)	4.184 000 X E -2
curie	*giga becquerel (GBq)	3.700 000 X E +1
degree (angle)	radian (rad)	1.745 329 X E -2
degree Fahrenheit	degree kelvin (K)	$t_K = (t_F + 459.67)/1.8$
electron volt	joule (J)	1.602 19 X E -19
erg	joule (J)	1.000 000 X E -7
erg/second	watt (W)	1.000 000 X E -7
foot	meter (m)	3.048 000 X E -1
foot-pound-force	joule (J)	1.355 818
gallon (U. S. liquid)	meter ³ (m ³)	3.785 412 X E -3
inch	meter (m)	2.540 000 X E -2
jerk	joule (J)	1.000 000 X E +9
joule/kilogram (J/kg) (radiation dose absorbed)	Gray (Gy)	1.000 000
kilotons	terajoules	4.183
kip (1000 lbf)	newton (N)	4.448 222 X E +3
kip/inch ² (ksi)	kilo pascal (kPa)	6.894 757 X E +3
ktap	newton-second/m ² (N-s/m ²)	1.000 000 X E +2
micron	meter (m)	1.000 000 X E -6
mil	meter (m)	2.540 000 X E -5
mile (international)	meter (m)	1.609 344 X E +3
ounce	kilogram (kg)	2.834 952 X E -2
pound-force (lbs avoirdupois)	newton (N)	4.448 222
pound-force inch	newton-meter (N·m)	1.129 848 X E -1
pound-force/inch	newton/meter (N/m)	1.751 268 X E +2
pound-force/foot ²	kilo pascal (kPa)	4.788 026 X E -2
pound-force/inch ² (psi)	kilo pascal (kPa)	6.894 757
pound-mass (lbm avoirdupois)	kilogram (kg)	4.535 924 X E -1
pound-mass-foot ² (moment of inertia)	kilogram-meter ² (kg·m ²)	4.214 011 X E -2
pound-mass/foot ³	kilogram/meter ³ (kg/m ³)	1.601 846 X E +1
rad (radiation dose absorbed)	**Gray (Gy)	1.000 000 X E -2
roentgen	coulomb/kilogram (C/kg)	2.579 760 X E -4
shake	second (s)	1.000 000 X E -8
slug	kilogram (kg)	1.459 390 X E +1
torr (mm Hg, 0° C)	kilo pascal (kPa)	1.333 22 X E -1

*The becquerel (Bq) is the SI unit of radioactivity; 1 Bq = 1 event/s.

**The Gray (Gy) is the SI unit of absorbed radiation.

A more complete listing of conversions may be found in "Metric Practice Guide E 380-74," American Society for Testing and Materials.

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SECTION 1

INTRODUCTION

The ROSCOE-IR computer program provides a means for calculating IR observables from nuclear detonations (NUDETS). The general computational scheme in ROSCOE is to calculate the radiance along a line-of-sight (LOS) from the arbitrary location of the sensor looking toward the NUDET source region. By projecting a number of lines-of-sight to the source and its vicinity, it is possible to construct an image for imaging type sensors. For non-imaging sensors with finite field-of-view (FOV), it is possible to assess the radiance transmitted directly from the source and separately to assess the contribution at the detector of backgrounds and scattering contributions along the lines-of-sight not leading directly to the source. In each case, the NUDET source is modeled as a function of time and wavelength and the radiance along the LOS is calculated by integrating along the LOS toward the source. The transmission of the medium and the contribution to radiance by differential elements of the LOS through emission and scattering into the LOS are taken into account. Contributors to the radiance are thus NUDET source radiation at the end of the LOS; emission of the atmospheric elements between source and sensor; and scattering into the LOS of solar radiation, earth-emitted radiation, and NUDET radiation from source points off the LOS.

The presence of natural clouds in the atmosphere influences the observable IR radiance so strongly that the inclusion of a cloud model in the ROSCOE-IR program is essential for the realistic assessment of IR observables. In most areas of the world of interest in connection with nuclear explosions, clouds are present about two thirds of the time and, in fact, clouds will lie in a LOS about one half the time. Clouds produce several kinds of effects which are important both to imaging and non-imaging sensor systems. The most obvious effect of clouds is to obscure the source or to so reduce its intensity that it is not detectable by the sensor. Thick clouds provide direct attenuation factors as high as 10^4 or 10^5 even at the most transparent wavelengths.

In wavelength bands where there is strong absorption, such as at 2.7 microns, attenuation factors of this sort occur even for rather thin clouds. This attenuation by clouds has led to the well known rule of thumb that at many wavelengths NUDETS are not visible from above until the nuclear cloud has risen through the cloud tops.

A second effect of clouds even at moderately transparent wavelengths is to destroy the image of the source by multiple scattering so that the apparent source, when viewed from above, is a circular diffuse spot on the cloud top which may be many kilometers in radius. As the nuclear cloud rises, this diffuse source becomes smaller in radius, turning gradually into the nuclear cloud itself as it emerges from the cloud top. Many seconds typically are involved in the rise of the nuclear cloud from low altitudes to cloud-top altitudes.

A third effect of clouds arises in scattered or broken clouds so arranged that one cloud obscures the direct LOS to the source, while other LOS's lead to cloud edges which are illuminated by the source. Since cloud-edge reflections may contribute greater radiance than that produced along an obscured LOS, this effect gives rise to a number of lighted clouds in the vicinity of the source brighter than the (obscured) source. Other effects of clouds include a higher background radiance than in the absence of clouds because of the high albedo of cloud tops for solar radiation and a spottiness in the background when the clouds are scattered or broken.

It has been the purpose of the ROSCOE natural cloud project to provide a cloud model and the capability in ROSCOE-IR to calculate cloud effects on systems which look at NUDET environments. Satellite systems, particularly, have been kept in mind during the development of this natural cloud capability and the spectral dependence of effects has been sufficiently treated in the 2- to 5-micron region in order that realistic results will be provided for sensors whose spectral sensitivity lies within this range.

The complexity of clouds and the variability of cloudiness in a given region poses an immediate problem in cloud modeling. It is typical that any choice of cloud configurations used for transmission calculations leads to criticism by some reviewer. Such questions arise as, why does the cloud obscure the source when it is quite likely that the source will be visible through breaks? What would be the effect if the source were half obscured and half visible? Why worry about the

brightness of illuminated clouds when the direct view of the source will be so much brighter? Why worry about obscuration of the fireball when waiting awhile will allow it to break through the clouds? Each user who contemplates cloud effects tends to think of configurations which lead to maximum or minimum impact on a system and tends to focus on worst cases or best cases. Each possible cloud configuration has some validity in the problem, but a measure of the likelihood of the case is important for overall assessment.

For the ROSCOE-IR program a cloud-effects capability has been provided which allows the user to specify, within limits, the cloud scene of his choice so that the effects of scenes which he considers likely to be important can be assessed. This capability is called the deterministic model.

In addition to the deterministic model, a statistical cloud model, based on historical observation, is provided for ROSCOE. Frequency of occurrence of cloud types and average descriptions of the properties of each of the cloud types are obtained from a global cloud study and data bank prepared for NASA (Reference 1). By the use of this statistical natural cloud model, the ROSCOE program calculates the probability distribution for radiance along a LOS and thus determines the extremes in radiance which may be exhibited in the presence or absence of clouds. For a problem which has been done by the deterministic mode, the likelihood of such a result based on natural cloud occurrences can be judged.

The physical and geometric treatment of these two cloud models is described in the following section.

SECTION 2

CLOUD MODELS

The ROSCOE-IR program performs very detailed calculations to determine radiance along the line-of-sight to a sensor. The exact geometric location of the sensor and sources including the sun, the earth's surface, and the composition of the atmosphere as a function of location are taken into account. The radiance may be calculated at any wavelength selected in the 2- to 5-micron band. Source spectral powers, absorption and scattering cross-sections, reflectivities, and other physical properties affecting radiation transport must be known in detail as a function of wavelength. A cloud model for use in conjunction with ROSCOE-IR must thus have the same detailed physical and geometric description to enable these calculations to be performed with clouds in the scene. The deterministic and statistical cloud models have been so constructed that each calculation is made in the presence of clouds sufficiently described in physical properties and geometry that such detailed transmission calculations can be performed. For the statistical clouds a whole set of such calculations is done within the cloud model and selected fractiles of the integral distributions of results so obtained are provided as output.

2-1 DETERMINISTIC CLOUD MODEL

The introduction of deterministic clouds into the NUDET environment involves a specification sufficiently complete to allow radiation transmission calculations. Various deterministic cloud shapes have been used in other radiation transmission programs. These include modeling of clouds by horizontal slabs; spheres; hemispheres; round, rectangular, and hexagonal prisms; etc. For the ROSCOE natural cloud routines we have chosen ellipsoids. By the specification of the three axes, these may vary from spherical shapes to elliptical pancake shapes to very elongated rod-like shapes. The three axes are required to lie in the vertical direction and in the horizontal plane and the orientation of the longer axis in the horizontal plane must be specified.

Location in three dimensions of the center of the ellipsoid then completes the specification of the geometric cloud boundary. Any number of clouds up to 20 are permitted in the scene so long as they are not intersecting. This deterministic placement allows the investigation of the effects of obscuration of the source by clouds, the brightness and extent of illuminated cloud edges, and the brightness of edges surrounding a hole through which the source is viewed. The cloud type which is being represented is also identified as one of the naturally occurring types so that the water droplet density and size distribution may be specified. A sample obscuration case is described in Section 4.

Transmission calculations for both deterministic and statistical cloud models have been done by diffusion. The absorption and scattering cross-sections for the water droplets and the scattering phase functions have been calculated (Reference 2) by the Mie theory of scattering of photons by spherical droplet distributions. The droplet size parameters from Reference 1 (Table 6-1) were used and are given in Table 2-1. These mean radius and variance values were used to generate a gamma distribution in droplet size for each cloud type.

Such calculations were made for droplets in the range of radii for 4.5 to 10 μm for which Mie phase-function parameters were readily calculable. These sizes are characteristic of droplet sizes for cloud-types 1 through 10 in Table 2-1. The Mie-theory parameters for 40- μm radius droplets are extremely difficult to calculate and were regarded as being beyond the scope of the investigation.

The so-called 40- μm droplets are in the usual situation actually ice crystals. The approximation of simulating such large crystals by spherical droplets would be dubious, since the dimensions are large enough that irregularities are several wavelengths in size.

The application of the usual scattering and/or diffusion concepts would be seriously complicated by the fact that such crystals are typically spatially oriented, i.e., their axes tend to be aligned. For example, in diffusion this would imply an anisotropic medium, not just anisotropic scattering.

For these reasons Mie-theory parameters were not obtained for cloud-types 11 through 14. Instead, we idealized the droplets as being 40- μm radius water droplets and employed small-wavelength approximations as described at the end of Section 3-2.16.

Table 2-1. Cloud properties by type.

Type	Layer	Base (km)	Thick (km)	Top (km)	n (cm ⁻³)	\bar{r} (μ m)	σ_r (μ m)	Composition
1. Cumulus-1	Low	.5	.5	1	30	5.5	1.	Water
2. Cumulus-2	Low	1	3	4	70	8	2.	Water
3. Cumulus-3	Low	4	.5	4.5	30	6.5	1.	Water
4. Stratocumulus	Low	.3	2	2.3	100	4.5	1.	Water
5. Stratus	Low	.15	1	1.15	150	5	2.	Water
6. Cumulonimbus-1	Low	.5	.5	1	30	5.5	1.	Water
7. Nimbostratus	Low	1	3	4	70	5	0.5	Water
8. Altopcumulus	Mid	2	5(4)*	7(6)	30(40)	4.8	0.5	Water
9. Altostratus-1	Mid	2	4	6	70	6	0.6	Water
10. Cumulonimbus-2	Mid	1	9(5)	10(6)	70(120)	10	1.	Water
11. Cumulonimbus-3	High	10	2	12	1	40	10.	Ice
12. Altostratus-2	High	6	4	10	10	40	10.	Ice
13. Cirrus (Midlatitude)	High	6	3	9	.8	40	10.	Ice
14. Cirrostratus (Midlatitude)	High	6	4	10	2	40	10.	Ice

* Parenthetical values are used in the code calculations to facilitate providing for contiguous layers in the multilayer configuration; see discussion relating to Figure 2-7 and also see Section A-4.3.

The phase functions computed from Mie theory have been used to determine the average cosine of the scattering angle, $\bar{\mu}$. From the cross sections and $\bar{\mu}$ were constructed the macroscopic transport parameters which are used in the diffusion calculations. Ten wavelength values in the 2- to 5-micron range have been selected in such a way that the principal variations in cross section are retained when linear interpolation between these wavelength values is made. The chosen wavelengths are 2.0, 2.5, 2.55, 2.65, 2.75, 2.85, 3.2, 3.5, 4.0 and 5.0. For wavelengths between these values, linear interpolation is used on the macroscopic total cross-section, Σ , the macroscopic scattering cross-section, Σ_s , and the average cosine of the scattering angle, $\bar{\mu}$. Since the absorption cross-section, Σ_a , is the difference between the total cross-section and the scattering cross-section, the necessary quantities are available to determine the macroscopic transport cross-section, Σ_{tr} , the diffusion coefficient, D , and the relaxation rate, K , which are the constants required for solution of the diffusion equation. According to the "standard" evaluation of diffusion parameters in terms of macroscopic cross-sections, we have the relations

$$\Sigma_{tr} = \Sigma - \bar{\mu}\Sigma_s \text{ (km}^{-1}\text{)}, D = \frac{\Sigma_s}{3\Sigma_{tr}} \text{ (km)} \text{ and } K = \left(\frac{\Sigma_a}{D}\right)^{\frac{1}{2}} \text{ (km}^{-1}\text{)} .$$

However, that evaluation is strictly applicable only in the limit of small absorption. A more generally applicable evaluation, which we adopted for numerical results in this report, is described in Section A-1.2.

For the deterministic case the ellipsoidal boundary leads to great mathematical complexity in applying boundary conditions. The problem therefore has been treated by means of a Green's function and application of Green's theorem so that the problem is reduced to a two-dimensional surface problem. The surface integrals can conveniently be treated numerically by partition of the surface into a number of facets and summing. The general problem is treated in Section A-3.

A typical geometry for the deterministic cloud problem is shown in Figure 2-1. A point source S illuminates an ellipsoidal cloud and gives rise to radiance in the direction of a detector D . The cloud surface is naturally divided into four regions by the terminators

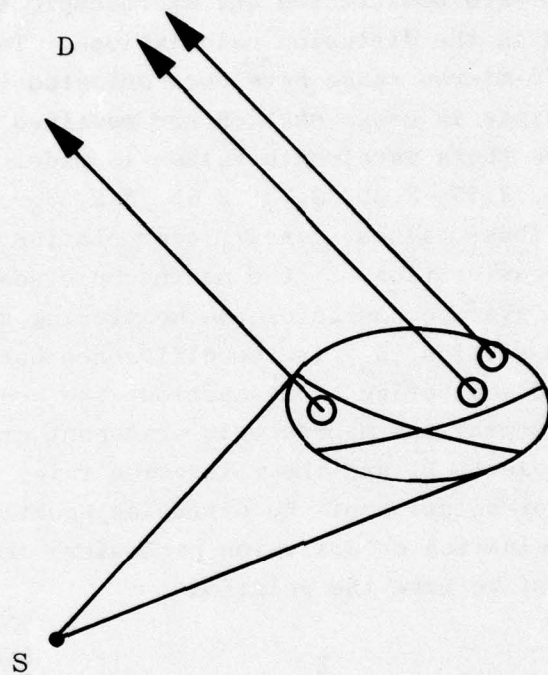


Figure 2-1. Deterministic ellipsoidal cloud model showing four regions produced by terminators.

corresponding to the source and detector points. Thus, there is an illuminated and a shadowed portion of the cloud and a visible and an invisible portion of the cloud. These combine to give four categories of cloud surface, only two of which are visible to the detector. Three lines-of-sight are shown in Figure 2-1, the lowest of which intersects an illuminated visible region while the two upper ones intersect a visible but non-illuminated region. Radiance from this latter region arises entirely from emergence of photons which have diffused through the cloud from the lower illuminated region. Although diffused photons contribute to the lowest line-of-sight also, it is in fact dominated by photons reflected from the surface. This sector of the cloud is therefore treated by bidirectional reflectance, taking into account the incident and emergent directions and the local normal to the cloud surface. Bidirectional reflectance coefficients for this purpose were calculated by Monte Carlo for a thick, flat cloud of stratocumulus (Sc) droplet density and size distribution. (This set of bidirectional reflectance coefficients is used as an approximation to the set for each of the other 13 cloud types.) The emergent photons at 45 directions in exit zenith angle and azimuth were calculated for four incident zenith angles. These tabular data of bidirectional reflectance coefficients are interpolated for use in the deterministic cloud model. The angular distribution for the photons emerging from diffusion transmission to the non-illuminated surfaces is taken to be diffuse (or Lambertian) in angular distribution.

For evaluation of the photons into and out of the deterministic cloud, the cloud is divided into facets as shown in Figure 2-2. The facets are constructed so as to lie between lines of constant θ and constant ϕ , with more facets of smaller area being concentrated near the regions of maximum curvature in the ellipsoid. In the cloud coordinate system, if \underline{a} is the semi-major axis lying in the horizontal plane and \underline{b} is the semi-minor axis, then the division of the azimuthal angle ϕ , where ϕ is measured from the direction of the long axis, is according to the prescription

$$\phi_{6-m} = \frac{\pi}{2} - \psi_m, \quad \Delta\phi = \Delta\psi, \quad m = 1, 2, \dots, 5$$

$$\psi_n = \psi_{n-1} + \Delta\psi \left(\frac{b}{a}\right)^{(n-2)\beta}, \quad \psi_1 = 0; \quad \psi_N = \frac{\pi}{2}, \quad 2 \leq n \leq N = 5$$

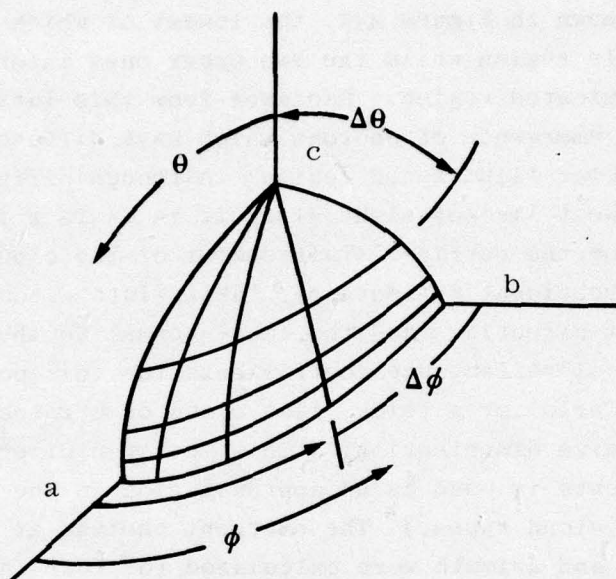


Figure 2-2. Subdivision of ellipsoidal cloud surface into facets.

Given β , this can be solved for $\Delta\phi$, the angular dimension of the first facet, and thus for each of the ϕ_n in a quadrant. Similarly the polar angle θ , measured from the zenith, is divided in a like manner according to the formula

$$\theta_n = \theta_{n-1} + \Delta\theta \left(\frac{c}{a}\right)^{(n-2)\alpha}, \quad \theta_1 = 0; \quad \theta_N = \frac{\pi}{2}, \quad 2 \leq n \leq N = 5.$$

The explicit formulas for θ_i and ϕ_i are given in Section 3 with the description of subroutine CLDGEOM. Here α and β are arbitrary exponents chosen to accentuate the grouping of facets at regions of high curvature. A value of $\alpha = \beta = 0.8$ has been used. These facets are then reflected through the principal planes into the other seven octants of the ellipsoid.

The area of facet i, j is given by the expression

$$A_{ij} = \int_{\phi_j}^{\phi_{j+1}} d\phi \int_{\theta_i}^{\theta_{i+1}} d\theta r^2 \sin\theta (1 + S^2 + T^2)^{\frac{1}{2}}$$

where

$$r^{-2} = \sin^2\theta \left(\frac{\cos^2\phi}{a^2} + \frac{\sin^2\phi}{b^2} \right) + \frac{\cos^2\theta}{c^2}$$

$$S = \sin\theta \cos\theta \left[\frac{r^2}{a^2} \cos^2\phi + \frac{r^2}{b^2} \sin^2\phi - \frac{r^2}{c^2} \right]$$

$$T = \sin\theta \sin\phi \cos\phi \left[-\frac{r^2}{a^2} + \frac{r^2}{b^2} \right].$$

This integration is performed numerically.

As discussed in Section A-3, the solution for the ellipsoid illuminated by a point source is in the form of the outgoing photon flux (radiant exitance), i.e., watts/kilometer², per watt emitted by an isotropic point source. Illumination by the source is converted to ingoing photon flux (irradiance) at each of the illuminated facets by computing

$$J_- = \frac{S \cos \theta_i}{4\pi R^2}$$

for a unit source. Specifically, if $J_+(\vec{r})$ and $J_-(\vec{r})$ are the outward and inward fluxes, respectively, then

$$\left. \begin{aligned} J_+(\vec{r}') &= S(\vec{r}') - \int_{\Sigma} J_+(\vec{r}) G_+(\vec{r}, \vec{r}') d\sigma(\vec{r}) \\ S(\vec{r}') &= -J_-(\vec{r}') - \int_{\Sigma} J_-(\vec{r}) G_-(\vec{r}, \vec{r}') d\sigma(\vec{r}) \end{aligned} \right\} \quad (55)*\&(59)*$$

$$G_{\pm}(\vec{r}, \vec{r}') = \frac{\hat{n}(\vec{r})}{2\pi} \cdot \text{grad } G(\vec{r}, \vec{r}') \pm \frac{a}{2\pi b} G(\vec{r}, \vec{r}') \quad (55)$$

$$G(\vec{r}, \vec{r}') = e^{-KR/R} \quad (53)$$

$$\text{grad } G(\vec{r}, \vec{r}') \equiv (\nabla G)_{\vec{r}} = G(\vec{r}, \vec{r}') (K+R^{-1}) \frac{\vec{r}' - \vec{r}}{R}$$

$$R = |\vec{r} - \vec{r}'|$$

where a and b are given in Table A-2. Note that the gradient of $G(\vec{r}, \vec{r}')$ is evaluated at the inward-flux position \vec{r} . In the application of this, we used, in our early work, the approximate solution, $J_{2,+}(\vec{r}')$:

$$J_{1,+}(\vec{r}') = S(\vec{r}') / \left[1 + \int_{\Sigma} G_+(\vec{r}, \vec{r}') d\sigma(\vec{r}) \right] \quad (60a)*+$$

$$J_{2,+}(\vec{r}') = J_{1,+}(\vec{r}') - \frac{\int_{\Sigma} (J_{1,+}(\vec{r}) - J_{1,+}(\vec{r}')) G_+(\vec{r}, \vec{r}') d\sigma(\vec{r})}{1 + \int_{\Sigma} G_+(\vec{r}, \vec{r}') d\sigma(\vec{r})} \quad (60b)*++$$

In the computation, the integrals are approximated by sums,

$$\begin{aligned} \xi(\vec{r}') &= \int_{\Sigma} f(\vec{r}) G_{\pm}(\vec{r}, \vec{r}') d\sigma \approx \sum_{j \neq i} f(\vec{r}_j) G_{\pm}(\vec{r}_j, \vec{r}_i) A_j \\ &\quad + f(\vec{r}_i) \sqrt{\frac{A_i}{\pi}} \left(-\frac{1}{2R_i} \pm \frac{a}{b} \right) \end{aligned}$$

*Equation numbers in Appendix A.

†The form of $J_{1,+}$ is obtained by ignoring the last term on the right-hand side of Equation (59) in Appendix A.

†† $J_{2,+}$ is obtained by combining Equations (59) and (60a).

where A_i is the area associated with the point \vec{r}_i , R_i is the average radius of curvature at that point, and $f(\vec{r})$ represents the multiplier of G_+ in the integrals.

Eventually we found an example of $J_{2,+}$ being negative. Accordingly, after considerable review of the situation, we have settled for using $J_{1,+}$ in the computer code until a better solution is found.

The geometry of the computation is summarized in Figure 2-3. A line-of-sight (LOS) of interest from detector to cloud surface has been established. The quantity of interest is the cloud radiance in the (antiparallel) direction of the LOS at the intersection of the LOS with the cloud. An irradiance-to-radiance transfer coefficient, TCOEF, of dimension sr^{-1} , is provided by the cloud routines which, when multiplied by the normal spectral irradiance at the transfer point on the cloud, gives the required spectral radiance.* Transfer point t_1 in Figure 2-3 is on an element of the surface which is visible to the detector D but is not directly illuminated by the source S. It is thus radiant because of an outward flux of photons supplied by diffusion. Assuming diffuse radiance, the spectral radiance L_λ is given by

$$L_\lambda = \frac{J_{+\lambda}(t_1)}{\pi} ,$$

where $J_{+\lambda}$ is a function of all the irradiances $J_{-\lambda}$'s over the illuminated facets (k), given by

$$J_{-\lambda k} = \frac{S_\lambda}{4\pi R_{sk}^2} \cos \theta_{ik} .$$

The transfer coefficient then is

$$\text{TCOEF}_\lambda = \frac{4\pi R_{st_1}^2}{S_\lambda} L_\lambda (\text{sr}^{-1}) .$$

Similarly, for points on cloud facets which are both illuminated and visible, such as t_2 in Figure 2-3, the radiance is dominated by directional reflectivity. By definition of bidirectional reflectance coefficient, ρ' , the required spectral radiance is

* In the deterministic model (in contrast with the statistical model) attenuation is not included along the air path. Such attenuation will be computed by the sight-path integration model.

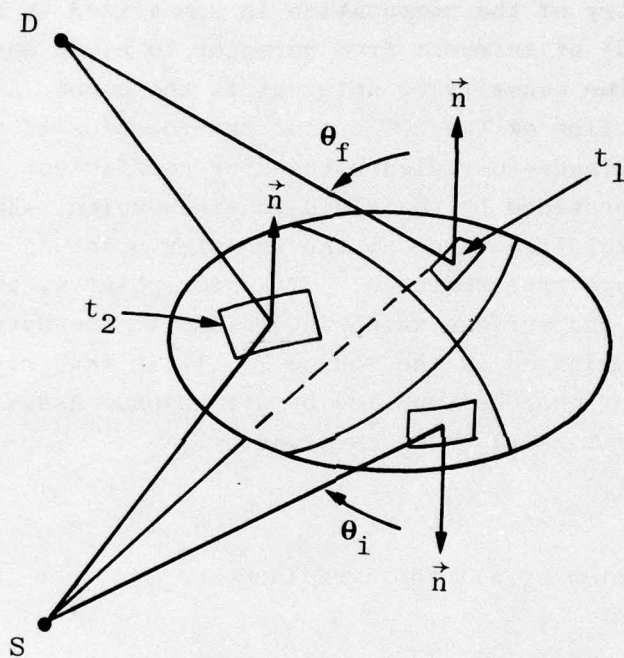


Figure 2-3. Deterministic cloud geometry.

$$L_{\lambda} = \rho'_{\lambda}(\theta_i, \theta_f, \phi) \frac{S_{\lambda} \cos \theta_i}{4\pi R_{st_2}^2} \text{ (watt km}^{-2} \text{ sr}^{-1} \mu\text{m}^{-1}) \quad .$$

The transfer coefficient then is again the quantity by which the normal irradiance* at the transfer point must be multiplied to give radiance in the direction of the detector and is given by

$$\text{TCOE}_{\lambda} = \frac{4\pi R_{st_2}^2}{S_{\lambda}} L_{\lambda} = \rho'_{\lambda}(\theta_i, \theta_f, \phi) \cos \theta_i \text{ (sr}^{-1}) \quad .$$

It should be noted that the bidirectional reflectance coefficient is dependent on the angle of incidence, the angle of reflection, and the azimuthal angle ϕ between the incidence and exit planes. This is the quantity which has been separately calculated by Monte Carlo and tabulated for use in the deterministic cloud problem.

The field-of-view of the detector is one of the specified quantities in the problem. The transfer coefficients are properly averaged over this field-of-view to give an average radiance along the line-of-sight. If the field-of-view is less than the facet area projected normal to the line-of-sight, then the facet radiance is the required average radiance. If, however, another facet lies within a distance equal to 0.7 times the square root of the area of the field-of-view, this facet also contributes to the average radiance and its radiance, weighted by the appropriate projected facet area in the field-of-view, is included in the calculation of the average radiance. When part of the field-of-view does not intersect the cloud, i.e., the cloud fills only a portion of the field-of-view, then the contribution of the off-cloud area to the average radiance is zero according to the cloud model. More properly, the line-of-sight integration module may arrange to provide the earth upwelling radiance in this off-cloud fraction.

In addition to the transfer coefficient which gives radiance resulting from the source, the cloud as an emitter of radiation must be considered. This self-emission radiance is calculated by assuming the cloud to be at the ambient atmosphere temperature at the altitude at which the LOS intersects the cloud and to emit a blackbody spectrum of that temperature with an appropriate emissivity in the direction of the

* See footnote on page 22.

line-of-sight. The directional emissivity is taken to be one minus the directional reflectance, $\rho_{d\lambda}$. The directional reflectance is computed by integrating the bidirectional reflectance coefficient, ρ'_λ , over the 2π solid angle, holding constant the incident direction equal to the angle between the LOS and the normal to the surface. That is, the emission spectral radiance at the transfer point in the direction of the detector, $L_{e\lambda}$, is given by

$$L_{e\lambda} = (1 - \rho_{d\lambda}) \frac{c}{4\pi} c_1 \lambda^{-5} \left(e^{c_2/\lambda T} - 1 \right)^{-1} \text{ (watt/(km}^2 \text{ sr } \mu\text{m))}$$

where

$$c_1 = 8\pi ch, \quad c_2 = ch/k, \text{ and}$$

$$\rho_{d\lambda}(\theta_i) = \int_{2\pi} \rho'_\lambda(\theta_i, \theta_f, \phi) \cos\theta_f d\Omega_f.$$

Since this radiance is independent of sources in the problem, it is not given as a transfer coefficient but is calculated as a spectral radiance (watt/(km² sr μ m)). Note that the emissivity of each of the 14 cloud types is taken to be that computed for cloud-type 4.

If the problem being examined is a daytime problem so that the sun also illuminates the cloud, a third source of cloud radiance exists. The solar reflected radiance is calculated exactly as though the sun were another point source and the transfer coefficient for that geometry is the output.

2-2 STATISTICAL CLOUD MODEL

The ROSCOE-IR statistical cloud model is based on the cloud descriptions and cloud occurrence data bank of Fowler et al. (Reference 1). The clouds are described as horizontal plane parallel slabs with a base altitude and a top altitude given for each cloud type, together with water-droplet average densities and droplet-distribution average radii. The occurrence data provide the probability that each such cloud type will occur singly or in multiple layers with other types. The data are further divided into coverage categories ranging

from clear (cover category 1) to full cloud cover (cover category 5) approximately by quarters (compare definitions of CCOVER in Section 4-2), so that the likelihood of a LOS being cloudy or cloud-free may be determined.

The data base is divided into the 30 geographic regions shown in Figure 2-4. Two regions of interest were selected. One of these is region 11 of the global data bank which is a temperate continental region and characterizes the northeast United States and western Europe. The second region is region 4 which is a tropical maritime region and includes, for example, the Hawaiian Islands. For each region, five subsets of the total data base have been selected for use in ROSCOE to provide a total of 10 user options. They are, for each region, the annual average, the winter day average, the winter night average, the summer day average, and the summer night average. For each of these options there is available the probability of occurrence of each of the 14 cloud types singly or in multiple layers, for each of the four cloud-coverage categories, and a probability for cloudless skies. An eleventh option permits the user to construct his own cloud-type occurrence probability table, it being required only that he utilize the same 14 cloud types for which physical descriptions exist. This option permits the user to examine the effect of any one of the cloud types and permits construction of cloud scenes characteristic of the information contained in weather reports or other cloud descriptions.

In the statistical cloud data base there are seven types of low-altitude clouds, three middle types, and four high types. Allowing only one cloud type in each altitude regime, the possible configurations include clear, the 14 types alone as a single layer, 61 combinations of two types in double layers, and 84 triple-layer combinations of three types. Thus 160 configurations are possible, neglecting the possibility of considering the four fractional cloud-coverage categories as the basis of a further factor of four.

This last consideration is avoided by treating only two aspects of each configuration, namely the possibilities of a cloud-free line-of-sight (CFLOS) along the ROSCOE user's LOS and of a LOS obscured by clouds. In the latter case, the clouds are assumed to be extensive in horizontal dimension so that the radiation transfer is the same as for plane parallel

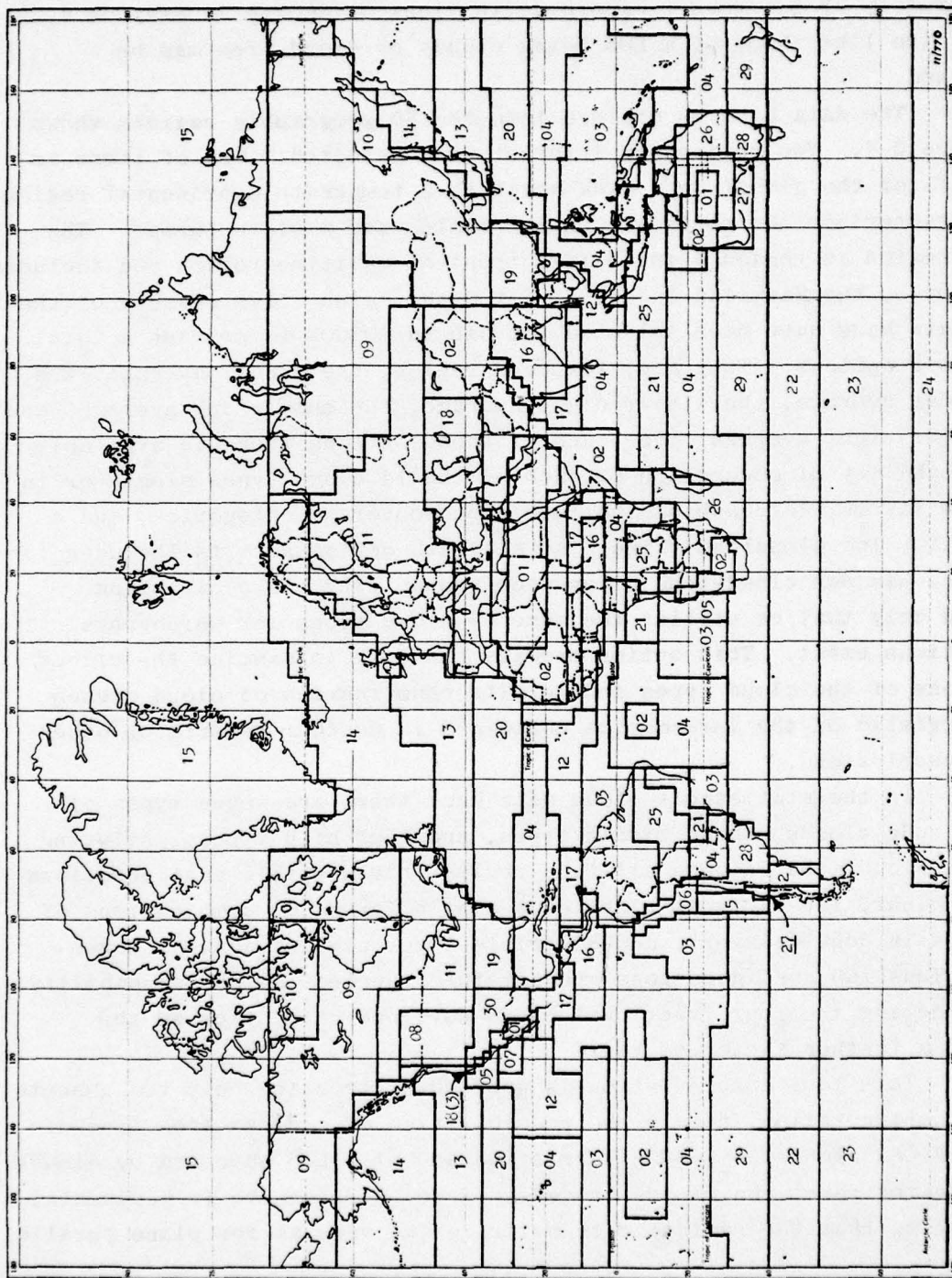


Figure 2-4. Geographic regions of the NASA worldwide cloud data bank.

layers of infinite extent. This is consistent physically with most fractional coverage cases, i.e., the cloud patches are large and the gaps are large. Thus only 160 possible configurations must be addressed.

For the ROSCOE-IR statistical cloud model it was required to provide spectral radiance quantities along the selected line-of-sight, namely radiance quantities arising from NUDET sources, solar reflection, and cloud emission. In order to retain an interface with the main program similar to that of the deterministic cloud model, the effects of NUDET and solar sources were to be returned separately as transfer coefficients, with units of sr^{-1} , and the emission was to be returned separately as a spectral radiance in units of $\text{watt km}^{-2} \text{sr}^{-1} \mu\text{m}^{-1}$.

Since the number of possible configurations of clouds is so large, it was decided not to transfer from the main program to the statistical cloud routine and back again for each possible cloud configuration but rather to loop through the configurations, each having its own probability, within the cloud routine and to return to the main program the probability distribution of radiance results.

The probability distribution is the result of the fact that each of the 159 cloudy configuration cases has a probability, or frequency weight, which can be determined from the ratio of the frequency of observed cases of this configuration to the total number of observations. These frequencies are in the data base.

The weights of each configuration are adjusted to take account of the probability of a CFLOS. The weight $W(i)$ for the LOS intersecting the i -th cloudy configuration is thus

$$W(i) = \sum_{cc=2}^5 W(i)_{r,cc} [1 - \text{CFLOS}_{cc}(\theta)]$$

where $W(i)_{r,cc}$ is the raw weight of the i -th configuration by type, layers, and coverage-category cc and $\text{CFLOS}_{cc}(\theta)$ is the probability for a CFLOS at the zenith angle θ and fractional coverage index cc . The CFLOS probabilities are derived from Lund's tables of CFLOS probability for all cloud types combined as a function of zenith angle and fractional coverage (Reference 3). The weight assigned to the clear line-of-sight is then

$$W(\text{clear}) = P(\text{cc}=1) + \sum_{i=1}^{159} [1-W(i)]$$

where $P(\text{cc}=1)$ is the weight of the clear cloud-coverage category (no clouds) and the sum represents the gap contributions from the partial coverage configurations. A more detailed treatment of these equations is given in the discussion of subroutine CLDWT in Section 3-2.

The statistical cloud routines then perform the appropriate calculation of radiation transmission for 159 configurations of cloud cover and for clear conditions and assign to each the probability weights, $W(160) = W(\text{clear})$ being the clear line-of-sight weight. The result is a distribution of 160 values of the radiance-related quantity calculated, each with its weight, or probability. The distribution is summed to provide an integral or cumulative distribution and radiance-related values from this cumulative distribution and provided as output at designated optional fractile values of probability provided as input in the call. $W(\text{clear})$, known in the code as PCFLOS, is also provided as an output, to be used as an approximation to the probability of a CFLOS to a NUDET source within the detector's field-of-view and below 12-km altitude.

The radiance-related quantities follow the same system as those of the deterministic cloud model, except that distributions rather than single values are the output. For NUDET sources and for the sun, the output is a distribution in transfer coefficients which, when multiplied by the (unattenuated) spectral irradiance at the transfer point from the source, results in a distribution of spectral radiances along the line-of-sight. The required spectral radiance L_λ and the transfer coefficient are related by the expressions

$$L_\lambda = \text{TCOE}_\lambda \cdot \begin{cases} \frac{S_\lambda}{4\pi R_{st}^2} & (\text{source}) \\ E_\lambda & (\text{sun}) \end{cases}$$

where S_λ is the isotropic point-source spectral power, R_{st} is the source-to-transfer-point distance, and E_λ is the solar irradiance. The cloud thermal emission output, however, is an actual radiance in units of $\text{watt km}^{-2} \mu\text{m}^{-1} \text{sr}^{-1}$ rather than a coefficient, because the thermal emittance is not related to NUDET or solar source strengths but depends solely on cloud temperature and emission properties. Again, as for the deterministic case, the NUDET, solar, and thermal emission outputs are provided separately.

Figure 2-5 is indicative of the geometry of the statistical cloud problem. One or more cloud layers for each of the 159 configurations will lie somewhere between 0.15-kilometer and 12-kilometer altitude. These are the base of the stratus and the top of the cumulonimbus-3 cloud models, respectively. In addition, a point source will be located somewhere in the figure such as at S1, S2, or S3. The source location will be either below the base of the lowest cloud, somewhere in the region occupied by one or more cloud types, or above the top of the highest cloud. A method has been developed for treating each of these cases. As a matter of fact, during the progression upward of a fireball from a low-altitude explosion, the source will progressively occupy each sort of location relative to the cloud region.

The statistical cloud program calculates the irradiance-to-radiance transfer coefficient along the reverse LOS at a transfer point, tp , which is chosen to be the intersection of the LOS with the 12-kilometer altitude plane, because all cloud tops lie at or below this point. By treating the atmospheric transmission problem in the cloud region within the cloud subroutines, as discussed later, it is possible to avoid having the main program integrate along the LOS to each of the 159 cloud-top altitudes in the entire statistical problem.

In addition to NUDET sources the sun as a radiation source is also indicated in Figure 2-5. For each of the 159 cloud configurations the sun illuminates the highest cloud top of the configuration and by reflectance contributes to the radiance along the LOS. The transfer coefficient corresponding to this solar reflected radiance is again a distribution of 160 points and is provided as a separate output distribution from that of a NUDET source. Note, however, in the 160-point distribution, there are only 10 different values (nine for clouds, one for Earth) because (a) there are only nine different cloud-top altitudes

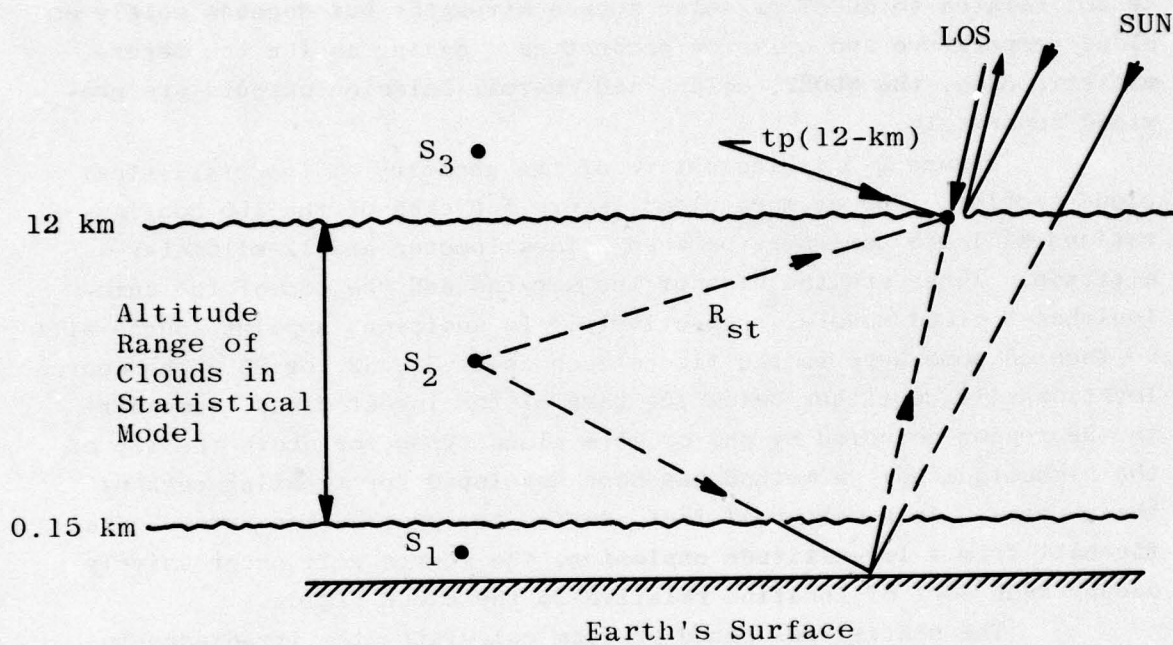


Figure 2-5. Statistical cloud geometry.

(cf. Table 2-1) and (b) the bidirectional reflectance of any cloud is assumed to be approximated by that for cloud-type 4 (stratocumulous).

In addition to the LOS intersecting cloud tops in the 159 cloud configurations, there is the probability of a CFLOS to the Earth's surface, which acts as a solar reflector and as an emitter. The surface may be sunlit or not, the probabilities depending on the probability of a CFLOS to the surface point from the sun. The contribution of the surface reflectance is weighted by the product probability of a two-leg CFLOS.

Finally, as in the case of the deterministic clouds, the statistical cloud tops are emitters which contribute to the radiance along the LOS. The cloud top for each configuration is treated as a blackbody-spectrum emitter at the temperature of the cloud top and with directional emissivity equal to $(1-\rho_d)$ as in the deterministic case. (The directional emissivity computed for cloud-type 4 (stratocumulous) is used for all cloud types.) This emission radiance distribution is again carried separately from the NUDET source and the solar distributions. The surface is again the 160th point in this distribution. As in the solar reflectance case, there are only 10 different values in the 160-point distribution.

A summary guide to the distributions available from the statistical cloud model is given in Table 2-2.

Figure 2-6 is a schematic of one of the calculations. A point source lies below a plane parallel cloud. By the solution of the diffusion problem in cylindrical geometry, described in Section A-2.1.3, the spectral flux leaving the cloud top is calculated and has a bell-shaped radial distribution as indicated in (a). The outgoing flux (radiant exitance or emittance) at the cloud top, J_+ , is given by a sum of weighted Bessel functions (Equation (30a), with $Q = S/2$) and the radiance, L , is just this flux divided by π , since the angular distribution is taken to be diffuse. The radiance at the point where the LOS intersects the cloud top is calculated and divided by the cloud-free normal irradiance at the transfer point, TP, to give a transfer coefficient with units of sr^{-1} as in the deterministic case. That is,

$$\text{TCOE}_{\lambda} = \frac{4\pi R_{st}^2 L_{\lambda} \tau_{\lambda}}{S_{\lambda}}$$

Table 2-2. Guide to distributions from the statistical cloud model.

IDX	LOS Terminates On	Thermal Emission, Radiance W/(km ² sr μm)	Solar Source Transfer Coeff., sr ⁻¹	Artificial Source Transfer Coeff., sr ⁻¹
1 to 159	Clouds	a	c	e
160	Earth	b	d	d

^aEach emission in the set of 159 is from the top of the uppermost cloud layer and is attenuated along the path to the transfer point at 12-km altitude. There are nine distinct values among the 159 values of such radiance corresponding to the nine different cloud-top altitudes.

^bThe emission is from the Earth's surface (the nature of which can be specified) and is attenuated along the path to the transfer point at 12-km altitude.

^cEach of the transfer coefficients in the set of 159 corresponds to the bidirectional reflectance of the uppermost cloud layer for the incident- and reflected-photon geometry and includes air transmittance along those portions of the incoming and reflected paths below 12-km altitude. The nine distinct values among the 159 values of such transfer coefficients correspond to the nine different cloud-top altitudes.

^dThe transfer coefficient corresponds to the bidirectional reflectance of the Earth's surface for the incident- and reflected-photon geometry and includes air transmittance along the incoming- and reflected-photon paths below 12-km altitude. The weight for this case includes the (product) probability of a two-leg CFLOS instead of a one-leg CFLOS as for the thermal emission case.

^eA given transfer coefficient may correspond to either (a) transmittance through cloud layers between the source and the transfer point or (b) bidirectional reflectance from the uppermost cloud layer below the source. Thus the distribution will include a combination of the above two types of transfer coefficients for a source above the lowest cloud-top altitude (1.0 km) and below the highest cloud-top altitude (12.0 km). For each transfer coefficient one includes air transmittance along those portions of (nominal) paths below 12-km altitude.

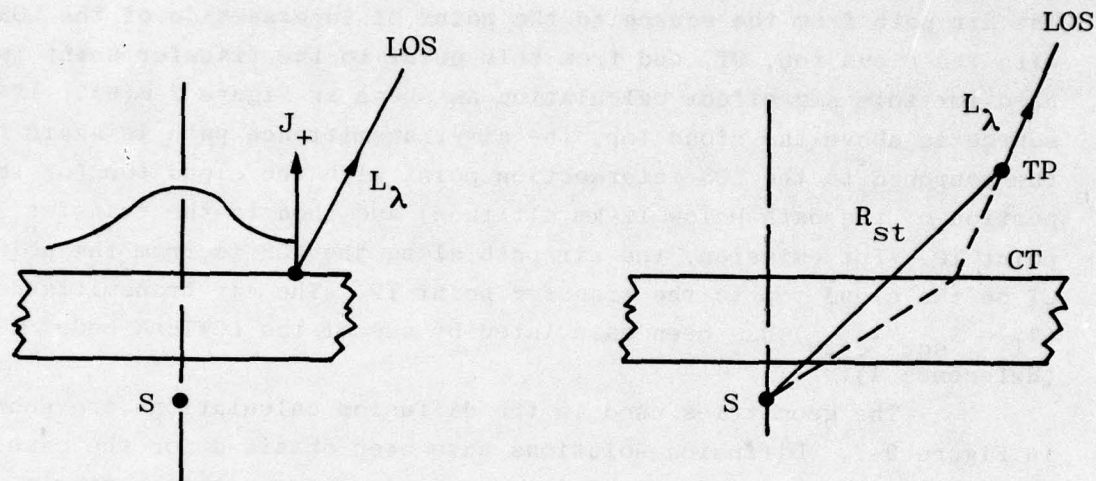


Figure 2-6. Typical statistical cloud geometry. (a) shows the bell-shaped radial distribution of flux, J_+ , leaving the cloud top and (b) shows the source-to-transfer-point distance R_{st} and the air transmittance path S-CT-TP.

Since, for statistical clouds in contrast with deterministic clouds, the main-program integration of radiance along the LOS does not extend below 12 kilometers, the air transmission reduction of the source radiance is approximated within the cloud model and reduces the cloud-top radiance, L_λ , prior to calculation of the transfer coefficient. The air path from the source to the point of intersection of the LOS with the cloud top, CT, and from this point to the transfer point is used for this air-effect calculation as shown in Figure 2-6(b). If the source is above the cloud top, the air-transmittance path is again from the source S to the LOS intersection point with the cloud top (or that portion of the path below 12-km altitude) and then to the transfer point TP. For emission, the air path along the LOS is from the point CT on the cloud top to the transfer point TP. The air transmittance ($\tau_\lambda = \tau_{\text{sct}} \tau_{\text{cttp}}$) has been calculated by use of the LOWTRAN code (Reference 4).

The geometries used in the diffusion calculations are shown in Figure 2-7. Diffusion solutions have been obtained for the case of a point source beneath a cloud (a), a point source within a single-layer cloud (b), and for a point source at or below the base of a multi-layered configuration of any number of layers (c). These three cases handle the necessary configurations with two exceptions. First, the cloud-type descriptions do not necessarily result in the base of an upper cloud coinciding with the top of a lower cloud so that gaps or overlaps exist between multiple layers. When this occurs the base of the higher layer is adjusted to coincide with the top of the layer below, the optical thickness of the upper layer being retained by adjustment of the particle number density. In this manner a continuous multi-layer medium is created which is compatible with the available diffusion solutions. Second, when the source lies within a cloud member of a multiple layer as shown in Figure 2-7(d), the cloud region below the source is neglected (truncated) so that the problem is reduced to that of Figure 2-7(c) with the source on the bottom surface. (The two adjustments are not commutative. In the code, we have implemented the second adjustment before the first.) The truncation modification is expected to cause about a 10% reduction in the cloud-top radiance, this being the approximate magnitude of the albedo* for these

* See function RHOEPS for a tabulation at 10 wavelengths of the hemispherical-directional reflectance, or equivalently, directional-hemispherical reflectance.

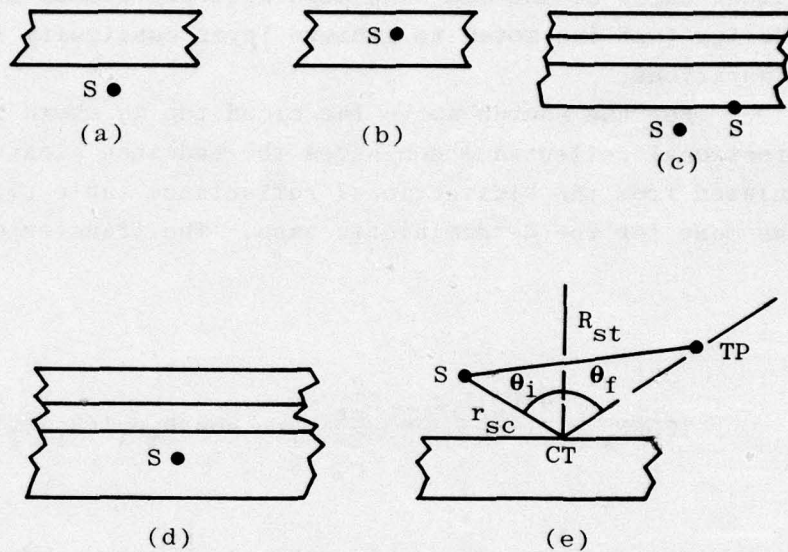


Figure 2-7. Diffusion and reflectance geometries for statistical clouds. Diffusion solutions have been obtained for Cases (a), (b), and (c). Case (d) is treated approximately by truncating the cloud region below the source, thereby converting it to Case (c) with source on surface. The solution for the transmitted photon flux is given by Equation (30a) for Case (a), by Equations (26b) and (40a) for Case (b), and by Equations (69) and (70) for Case (c). Note that Cases (a) and (b) become identical for the source on the surface ($h=0$). In this regard, one can verify that for $h=0$, Equation (40a) becomes identical to Equation (29a) provided Q in Equation (29a) is set equal to one-half of the isotropic source strength, S . In Equation (40a), S is tacitly unity.

clouds in the two- to five-micron region. A reflecting layer of albedo ω below the source increases the cloud-top radiance by a factor of about $1/(1-\omega)$, as shown at the end of Appendix D.

Figure 2-8 shows the assumed altitude range of each of the 14 cloud types for single-layer configurations. The dashed lines at the lower edges of the mid- and high-altitude clouds depict the boundaries that are moved to achieve layer contiguity in multilayer configurations.

For the source above the cloud top as shown in Figure 2-7(e), bidirectional reflectance dominates the radiance along the LOS and is calculated from the bidirectional reflectance table (Function CLDBDR) as was done for the deterministic case. The transfer coefficient is then

$$TCOE_{\lambda} = \frac{4\pi R_{st}^2 L_{\lambda} \tau_{\lambda}}{S} = \frac{R_{st}^2}{r_{sc}^2} \tau_i \tau_r \cos \theta_i \rho_{\lambda}'(\theta_i, \theta_r, \phi) \quad .$$

Here the air transmittance τ_{λ} is taken to be the product of the transmittances τ_i and τ_r along those portions of the incoming and reflected paths below 12-km altitude.

Examples of statistical cases are given in Section 4 and show both the radial distribution of radiance across the cloud tops and examples of the probabilistic distributions in radiance arising from the many possible cloud configurations.

Through use of the statistical cloud model the user may obtain three separate distributions for spectral radiance from NUDET sources, from the solar source, and from thermal emission backgrounds. It is rather obvious but perhaps worthy of note that these distribution data are more complex quantities than would be the three simple radiance values from a completely deterministic case. The three simple radiances, for example, can be added to give the total radiance which would be observed by a sensor. They can be divided to give ratios of signal-to-noise, signal-to-solar background, etc. Such quantities are often important measures of sensor effectiveness.

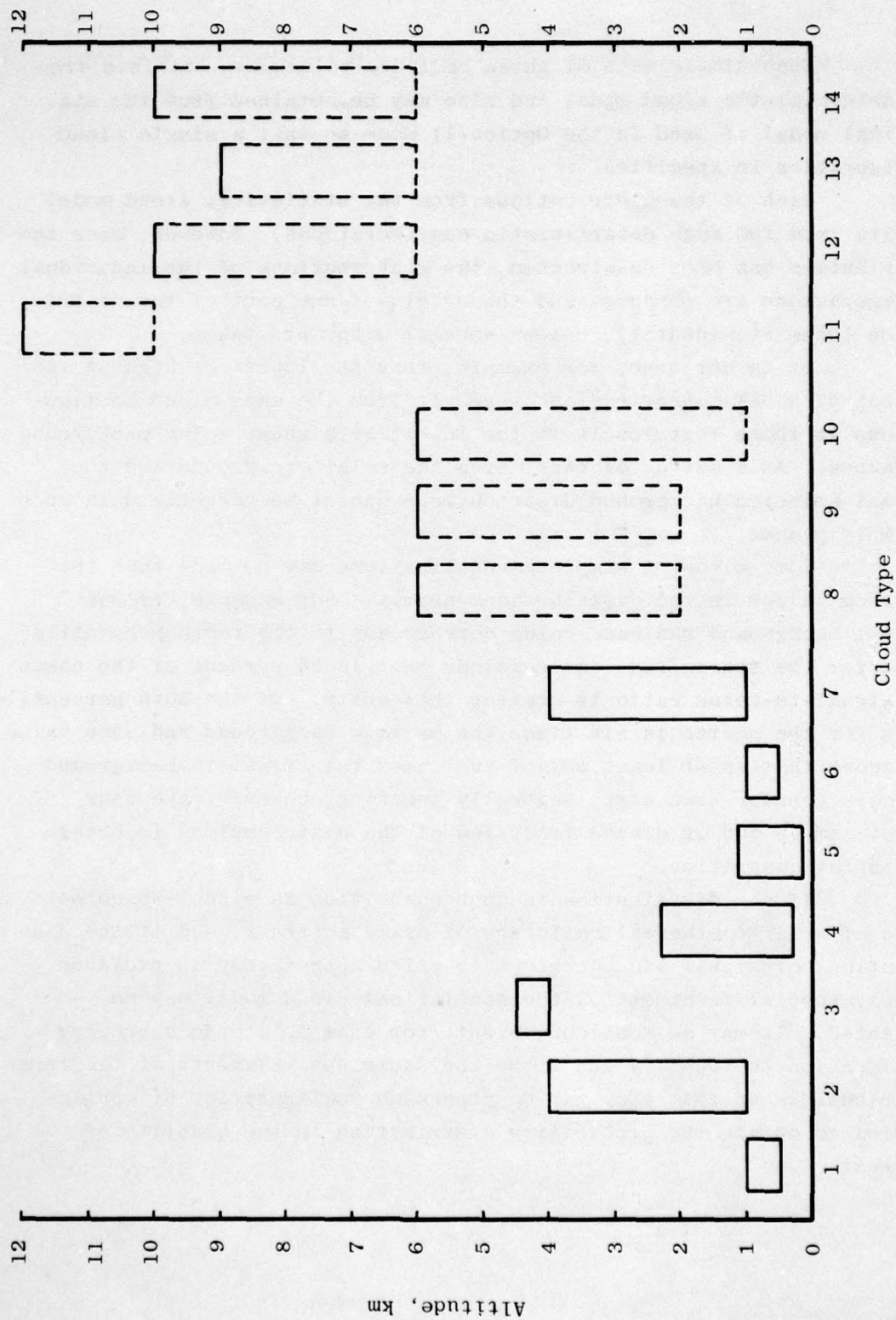


Figure 2-8. Altitude ranges of single-layer cloud types.

Such simple sets of three radiance values are obtained from the deterministic cloud model and also may be obtained from the statistical model if used in the Option-11 mode so that a single cloud configuration is specified.

Each of the distributions from the statistical cloud model results from 160 such deterministic configurations. However, once the distribution has been constructed, the contributions of the individual configurations are obscured and the origin of any part of the distribution loses its identity, unless special steps are taken.

It is not true, for example, that the lowest or highest ten percent of NUDET source radiances result from the same cloud configurations as those that result in the lowest or highest solar background radiances. As a matter of fact, even the solar background and the thermal emission background distributions cannot be correlated in such a simple manner.

Some kinds of simple generalizations may be made when the radiance values in the distributions permit. For example, if the highest background radiance value corresponds to the tenth percentile value for the source, one can conclude that in 90 percent of the cases the signal-to-noise ratio is greater than unity. If the 50th percentile value for the source is six times the maximum background radiance value, one knows that in at least 50% of the cases the signal-to-background ratio is greater than six. Generally speaking, however, the user cannot simply add or divide fractiles of the distributions to obtain meaningful quantities.

If the distribution in such quantities as signal-to-noise ratio of solar-to-thermal ratio are of prime interest, and if the distributions of signal and background overlap appreciably in radiance values, special treatment of the statistical cloud model may be warranted. It may be most convenient, for example, to do a program modification to identify and store the individual elements of the three distributions so that they may be processed configuration by configuration to obtain the probability distribution in the quantity of interest.

SECTION 3

COMPUTER PROGRAM DESCRIPTION

3-1 INTRODUCTION

The main (or driver) program ROSCOER is intended to demonstrate the utility of the ROSCOE-IR cloud computation procedure and to facilitate integration of the subroutines into ROSCOE-IR. All requirements of the computational procedure are met in ROSCOER to provide a stand-alone code and to provide a guide to the intended use of the subroutines. All overall program flow is illustrated in Figure 3-1.

Data provided by ROSCOE-IR (such as source, detector, and sun location) are read by the driver program ROSCOER or are entered via data statements. Calls to the deterministic and statistical cloud submodules are illustrated via ROSCOER. There is no preferential looping on lines-of-sight, wavelength, or cloud number. The calling program, ROSCOER, simply demonstrates how the code can be used. The deterministic check case (Problem 6 in Section 4) loops over the 64 possible lines-of-sight* at the second wavelength in the wavelength table, i.e., $\lambda = 2.5 \mu\text{m}$. A check case for the statistical cloud submodule (Problems 1 to 4, Section 4) loops over as many as 161 lines-of-sight at one-quarter kilometer intervals from the source normal to the lines-of-sight. The transfer coefficient is integrated with proper conversions to give a total transmission

Several parameters are initialized by statements in the main program only as a means of checking the code calculations and demonstrating its utility. The user will necessarily obtain this information by a replacement of this main program. A call to subroutine CLOUD0 obtains data that are required only by the cloud package and establishes the mode to be that of either a statistical cloud data base or a set of deterministic clouds. Deterministic cloud properties are still obtained from the preprogrammed data base; however, sizes and shapes, within the ellipsoidal constraint, and locations are to be provided by the user.

*The number of lines-of-sight returned by subroutine LOS has been reduced from a maximum of 64 to a maximum of 16 by incrementing the facet-center indexes by 2's, a procedure that appears to be adequate.

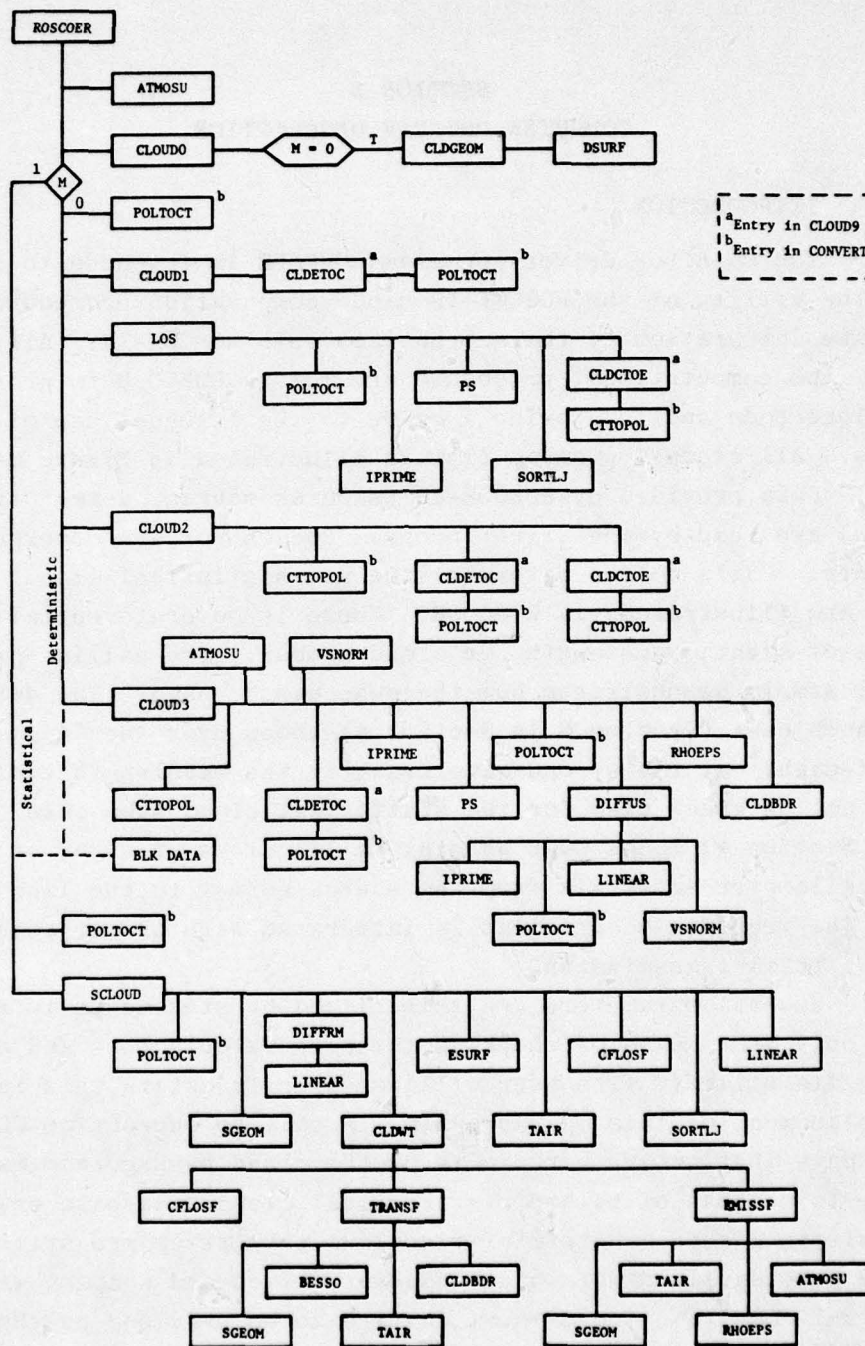


Figure 3-1. Flow chart of ROSCOE-IR cloud module.

The transfer coefficients for the calculations will, of course, be multiplied by a source irradiance to obtain a radiance in the direction of the detector at the transfer altitude of 12 kilometers (for statistical clouds). This coefficient, as well as the emission, has included in it the atmospheric transmission, in both directions, if appropriate, from the 1962 U.S. Standard Atmosphere as calculated from LOWTRAN 3 (Reference 4). No atmospheric attenuation is included in the deterministic case because it will be computed by the line-of-sight integration module in ROSCOE-IR.

Parameters such as lines-of-sight and wavelength are also user defined. A table of wavelengths is provided in common CDDATA at which cross sections are tabulated. This list provides a set of possible wavelengths to check out the code and to make specific calculations. The only restriction on wavelength is that it be between two and five microns.

A line-of-sight must be provided to both the deterministic and statistical subroutines. Possible lines-of-sight are provided for deterministic clouds by a call to subroutine LOS. These are, in turn, available in common LOS. A maximum of 64 lines-of-sight are returned. This table is terminated by zeros in the altitude array HLOS. Any or all of these lines-of-sight are appropriate for subsequent deterministic calculations.

Since a statistical cloud is infinite in lateral extent, there is no mechanism to relate the detector line-of-sight to the cloud. One usually has a particular scenario which directs which way the detector is looking and it is this consideration which gives rise to the input for statistical clouds. There is, however, little reason to make transmission calculations for horizontal distances in excess of five times the source to cloud-top distance. This situation may occur in statistical cases where the transmission is negligible; however, the code doesn't bother to eliminate the calculation.

The routines called to get an answer are CLOUD3 (UL,VL,WL,K, ALAM,TCOEF,EMISS,SINCLD) for deterministic clouds and SCLOUD(ALAM,UL, VL,WL,ISUN) for statistical clouds, where UL,VL,WL are the direction cosines of the LOS, ALAM is the wavelength in microns, TCOEF is the irradiance-to-radiance transfer coefficient at the intersection point of the LOS and cloud-K, EMISS is the thermal emission from the cloud

at the intersection point, and ISUN is a flag to distinguish between an artificial source and the sun. Common PTE variables must be initialized and utilized as follows:

(Input)

P1,P2,P3,P4 - four probability levels (fractiles) for which transfer coefficients and thermal emission are required.

(Output)

T1,T2,T3,T4 - four transfer coefficients corresponding to the P1,P2,P3,P4 above.

E1,E2,E3,E4 - thermal emission corresponding to P1, P2,P3,P4 above.

S1,S2,S3,S4 - four transfer coefficients corresponding to P1,P2,P3,P4 above for the sun as a source.

PCFLOS - probability of the detector seeing the artificial source, either with or without clouds being present, provided the source is within the field-of-view.

3-2 DESCRIPTION OF SUBROUTINES

A summary of the information necessary to execute each of the subroutines is provided in this section. Some of the subroutines are documented to a greater extent than others as the use of many is self-evident.

3-2.1 Program ROSCOER

The driver program ROSCOER is used to provide test cases for the deterministic and statistical cloud submodules. Data are read for the locations of the source and detector. A call to CLOUD0 reads the data which are required by the cloud module. Branching is directed by a mode flag to the submodules.

The deterministic mode is illustrated by a call to subroutine LOS and subsequent calls to subroutine CLOUD3 for the lines-of-sight determined by LOS. The statistical mode is illustrated by a series of lines-of-sight providing a function which is subsequently integrated across the cloud top to give total transmission.

3-2.2 Subroutine ATMOSU(JJ,ZH)

This subroutine, a dummy routine for the real one (see the ROSCOE Manual, Volume 14a-1), provides the atmospheric density (g/cm^3) and temperature (degrees K) as a function of altitude (km). The common ATMOUP is utilized with the fifth and sixth locations being the density and temperature. The calling sequence is (2,ZH), ZH being the altitude. The value of 2 for JJ denotes an operational call, allowed after ATMOSU has been initialized earlier with JJ=1. The density and temperature are provided by simple expressions:

$$\text{RHO} = 1.225\text{E-}3 * \text{EXP}(-\text{ZH}/9.)$$

$$\text{T} = 288. - \text{ZH} * 6.5$$

3-2.3 Function BESS0(X)

This routine provides the zero-order cylindrical Bessel function per formulas 9.4.1 and 9.4.3 in the NBS Handbook (Reference 5).

3-2.4 Block Data

This BLOCK DATA set contains the extinction (SIGT(10,14)) and scattering (SIGS(10,14)) cross-sections and the average cosine of the scattering angle (XMUBAR(10,14)) for the 14 cloud types. Units for the cross sections are square microns; cloud droplet number density is in reciprocal cm^3 . The code uses km^{-1} as macroscopic cross-section units with the conversion from microscopic cross-sections being

$$\sigma_x(\text{km}^{-1}) = \sigma_x(\mu\text{m}^2) \times N(\text{cm}^{-3}) \times \frac{10^{-8}\text{cm}^2}{\mu\text{m}^2} \times 10^5 \frac{\text{cm}}{\text{km}}.$$

SIGT, SIGS, and XMUBAR are tabulated at 10 wavelengths from 2 to 5 microns. The entries were calculated by Mie theory^a using cloud properties from Fowler (Reference 1) and given in Table 2-1.

Also tabulated are cloud coverage, CCOVER(5,11), and frequency, CFREQ(17,4,11), data for the statistical module.

^aSee the comment at the end of Section 3-2.16 for an exception to this statement.

CCOVER(1,K) is frequency of clear sky
 (2,K) is frequency of cloud-coverage category 2
 (3,K) is frequency of cloud-coverage category 3
 (4,K) is frequency of cloud-coverage category 4
 (5,K) is frequency of cloud-coverage category 5

where K is the model (i.e., time, region) discussed in Section 2-2.

CFREQ(I,J,K), I=1,17; J=1,4: K=1,11

CFREQ(1,J,K) is frequency of Cu1
 (2,J,K) is frequency of Cu2
 (3,J,K) is frequency of Cu3
 (4,J,K) is frequency of Sc
 (5,J,K) is frequency of St
 (6,J,K) is frequency of Cb1
 (7,J,K) is frequency of Ns
 (8,J,K) is frequency of Ac
 (9,J,K) is frequency of As1
 (10,J,K) is frequency of Cb2
 (11,J,K) is frequency of Cb3
 (12,J,K) is frequency of As2
 (13,J,K) is frequency of Ci
 (14,J,K) is frequency of Cs

where $\sum_{I=1}^{14} \text{CFREQ}(I,J,K) = 1$

CFREQ(15,J,K) is frequency of 1 layer
 (16,J,K) is frequency of 2 layers
 (17,J,K) is frequency of 3 layers

where $\sum_{I=15}^{17} \text{CFREQ}(I,J,K) = 1$

J is the cloud-coverage index and K is the model number.

3-2.5 Function CFLOSF(ICC,ANGLE)

This function obtains a value for the probability of a cloud-free line-of-sight from a table by Lund and Shanklin (Reference 3). The array is tabulated for cloud coverage (in 10ths) and for zenith angles in 10-degree increments from 0 to 90°. The table is for all cloud types combined.

The calling sequence requires the cloud-coverage index ICC to be an integer in 10ths and the angle in degrees.

INPUTS:

ICC-1 - cloud coverage (10ths)
ANGLE - zenith angle in degrees

OUTPUT:

CFLOSF - probability of a cloud-free line-of-sight
at a given zenith angle for the requested
cloud-coverage index ICC

Cloud coverages reported in tenths were grouped into five categories by the authors of Reference 1 (p.3):

Coverage category 1	0 tenths
Coverage category 2	1,2,3 tenths
Coverage category 3	4,5 tenths
Coverage category 4	6,7,8,9 tenths
Coverage category 5	10 tenths

In our cloud model the decimal cloud-coverage fractions of 0.0, 0.3, 0.5, 0.8, and 1.0 are assigned to the cloud-coverage categories 1,2,3,4 and 5, respectively.

3-2.6 Function CLDBDR (CTHIN,CTHOUT,CPHOUT,ALAM,KCLOUD)

This function contains tables of bidirectional reflectances for a stratocumulus cloud. The data are tabulated in forty-five equal solid angle bins at 10 wavelengths from 2 to 5 microns. The bi-directional reflectance has units of sr^{-1} . In the calling sequence the variables are:

CTHIN - cosine of incident zenith angle
 CTHOUT - cosine of exit zenith angle
 CPHOUT - cosine of the azimuthal angle between the
 incident and exit planes
 ALAM - wavelength, μm
 KCLLOUD - not used.

A linear interpolation is performed between wavelengths but no angular interpolation is utilized.

3-2.7 Subroutine CLDGEOM

Required bookkeeping for cloud "facets" is accomplished in this routine. See Figure 3-2 for a flow chart. A maximum of 20 deterministic clouds can be considered in a given job. Areas of the facets, radii to their centers, coordinates of the boundaries, and coordinates of the centers are evaluated and stored in common CDCORD for use by other routines. There is no requirement for user interaction with this subroutine, unless he wants to consider the irradiance on a particular facet and facet orientation to the source and detector. To do so would require a code modification.

Coordinates of the facets are computed according to the prescription:

$$\theta_1 = 0$$

$$\theta_2 = \frac{\pi}{2} \frac{1}{1 + (R1)^\alpha + (R1)^{2\alpha} + (R1)^{3\alpha}}$$

$$\theta_3 = [1 + (R1)^\alpha] \theta_2$$

$$\theta_4 = \frac{\pi}{2} - (R1)^{3\alpha} \theta_2$$

$$\theta_5 = \frac{\pi}{2}$$

$$\Delta = \frac{\pi}{2} \frac{1}{1 + (R2)^\beta + (R2)^{2\beta} + (R2)^{3\beta}}$$

$$\phi_1 = 0$$

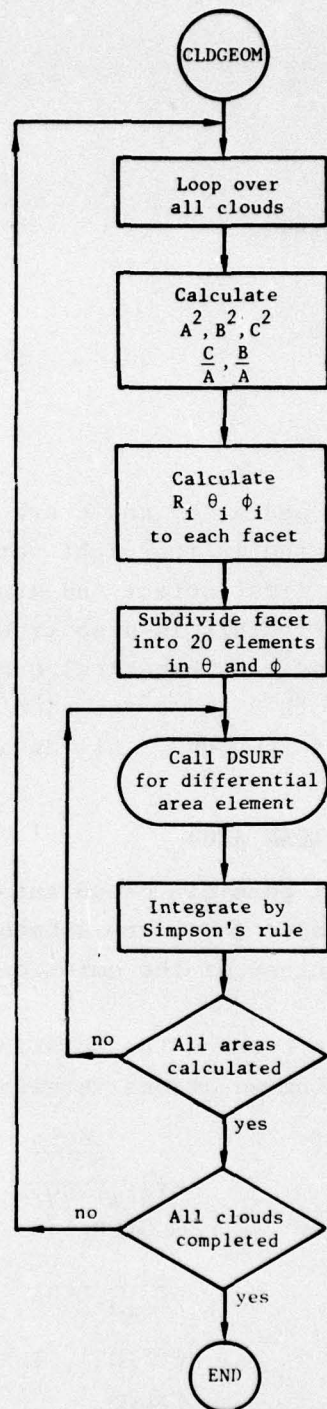


Figure 3-2. Flow chart of subroutine CLDGEOM.

$$\phi_2 = (R2)^{3\beta} \Delta$$

$$\phi_3 = \frac{\pi}{2} - [1 + (R2)^\beta] \Delta$$

$$\phi_4 = \frac{\pi}{2} - \Delta$$

$$\phi_5 = \frac{\pi}{2}$$

where R1 is c/a, R2 is b/a, and a, b, and c are the semi-axis lengths. These coordinates are reflected in the eight octants; consequently, they are calculated only for the first octant and are mapped to the other seven by the function IPRIME. This is also true of areas and radii.

Areas are evaluated by a numerical quadrature (Simpson's rule) using twenty intervals in both θ and ϕ for each facet. Differential area elements are calculated in DSURF. All data obtained from, and returned to, common arrays.

3-2.8 Subroutine CLDWT(ALAM,ANG)

Weightings for all possible cloud and cloud-layer combinations are evaluated in this routine. These are subsequently assigned to the transfer coefficients and values of the emission as calculated by calls to TRANSF and EMISSF.

The correspondence between the notation used in Section 2-2 and that used in the following equations is given below:

<u>Section 2-2</u>	<u>Here</u>
W(clear)	WT _{new} (160)
P(cc=1)	CCOVER(1)
$\sum_{i=1}^{159} [1-W(i)]$	WT _{old} (160)
W(i), i=1,159	WT(IDX), IDX=1,159
CFLOS _{cc} (θ)	CFLOS _c

For any of the 10 location-season averaged cloud models (KMODEL = 1,10), WT(IDX) is the probability that (a) the cloud-configuration set indicated by the index IDX occurs and (b) the LOS at zenith angle θ_e intersects the cloud-configuration set. The total probability of the LOS intersecting clouds is

$$\sum_{IDX = 1}^{159} WT(IDX) \quad .$$

The probability that the LOS does not intersect the clouds but "sees through" the clouds is

$$WT_{old} (160) \quad .$$

The probability of seeing the ground without any clouds being present is

$$CCOVER (1) \quad .$$

(For brevity we have suppressed the index KMODEL on which the array CCOVER depends.) The probability of seeing the ground either with or without clouds being present is

$$WT_{new} (160) = WT_{old} (160) + CCOVER (1) \quad .$$

The probability of seeing either clouds or the ground (with or without clouds being present) is

$$\sum_{IDX = 1}^{159} WT(IDX) + WT_{new} (160) = 1 \quad .$$

$$WT(I) = \sum_{C=1}^4 CCOVER(C+1) (1-CFLOS_c)$$

$$\left\{ \begin{array}{l} \cdot CF(15,C) \cdot \left\{ \begin{array}{l} TL \cdot \frac{CF(L,C)}{TL} \\ TM \cdot \frac{CF(7+M,C)}{TM} \\ TH \cdot \frac{CF(10+H,C)}{TH} \end{array} \right. \\ \cdot CF(16,C) \cdot \left\{ \begin{array}{l} \frac{TL \cdot TM}{DEN} \cdot \frac{CF(L,C) \cdot CF(7+M,C)}{TL \cdot TM} \\ \frac{TL \cdot TH}{DEN} \cdot \frac{CF(L,C) \cdot CF(10+H,C)}{TL \cdot TH} \\ \frac{TM \cdot TH}{DEN} \cdot \frac{CF(7+M,C) \cdot CF(10+H,C)}{TM \cdot TH} \end{array} \right. \\ \cdot CF(17,C) \cdot 1 \cdot \frac{CF(L,C) \cdot CF(7+M,C) \cdot CF(10+H,C)}{TL \cdot TM \cdot TH} \end{array} \right.$$

$L=1,7 \quad I=1,7$
 $M=1,3 \quad I=8,10$
 $H=1,4 \quad I=11,14$
 $L=1,7 \quad I=15,35$
 $M=1,3$
 $L=1,7 \quad I=36,63$
 $H=1,4$
 $M=1,3 \quad I=64,75$
 $H=1,4$
 $L=1,7 \quad I=76,159$
 $M=1,3$
 $H=1,4$

where

$$\begin{aligned} CF &\equiv CFREQ \\ TL &\equiv TOTL \\ TM &\equiv TOTM \\ TH &\equiv TOTH \\ DEN &\equiv TL \cdot TM + TL \cdot TH + TM \cdot TH \end{aligned}$$

The probability of seeing the ground through the clouds is

$$\begin{aligned}
 WT_{old}(160) &= \sum_{C=1}^4 CCOVER(C+1) \cdot CFLOS_c \cdot \sum_{\ell=1}^3 CF(14+\ell, C) \\
 &\cdot \left\{ \begin{aligned}
 &\sum_{j=1}^3 U(j|\ell=1, C) \cdot \sum_{K=KMIN_j}^{KMAX_j} \frac{CF(K|j, C)}{T_j} \\
 &\quad \text{DO-loops } 101, 102, 103 \quad \ell=1 \\
 &\sum_{j=1}^2 \sum_{j'>j}^3 V(j, j'|\ell=2, C) \sum_{K=KMIN_j}^{KMAX_j} \sum_{K'=KMIN_{j'}}^{KMAX_{j'}} \frac{CF(K|j, C)}{T_j} \cdot \frac{CF(K'|j', C)}{T_{j'}} \\
 &\quad \text{DO-loops } 200, 201, 202 \quad \ell=2 \\
 &W(1, 2, 3|\ell=3, C) \sum_{K=1}^7 \sum_{K'=8}^{10} \sum_{K''=11}^{14} \frac{CF(K|1, C)}{T_1} \cdot \frac{CF(K'|2, C)}{T_2} \cdot \frac{CF(K''|3, C)}{T_3} \\
 &\quad \text{DO-loops } 300 \quad \ell=3
 \end{aligned} \right. \\
 &= \sum_{C=1}^4 CCOVER(C+1) \cdot CFLOS_c = \sum_{C=1}^4 \frac{CFLOS_c}{1-CFLOS_c} \sum_{I=1}^{159} WT(I, C)
 \end{aligned}$$

Here, $U(j|\ell=1, C)$ is the probability of layer j , given one layer and cloud-coverage index C

$V(j, j'|\ell=2, C)$ is the probability of layers j and j' , given two layers and index C

$W(1, 2, 3|\ell=3, C)$ is the probability of layers 1, 2, 3, given three layers and index C

These probabilities satisfy the following relations:

$$\sum_{j=1}^3 U(j|\ell=1, C) = \sum_{j=1}^3 T_j = \sum_{j=1}^3 \sum_{K=KMIN_j}^{KMAX_j} CF(K|j, C) = 1$$

$$\sum_{j=1}^2 \sum_{j'>j}^3 V(j, j'|\ell=2, C) = \frac{\sum_{j=1}^2 \sum_{j'>j}^3 T_j T_{j'}}{\sum_{j=1}^2 \sum_{j'>j}^3 T_j T_{j'}} = 1; \quad W(1, 2, 3|\ell=3, C) = 1$$

$$\text{The probability of seeing clouds} = \sum_{I=1}^{159} WT(I)$$

$$= \sum_{C=1}^4 CCOVER(C+1) \cdot (1-CFLOS_C) \sum_{\ell=1}^3 CF(14+\ell, C)$$

$$\cdot \left\{ \begin{array}{l} \sum_{j=1}^3 U(j|\ell=1, C) \sum_{K=KMIN_j}^{KMAX_j} \frac{CF(K|j, C)}{T_j} \quad \ell=1 \\ \\ \sum_{j=1}^2 \sum_{j'>j}^3 V(j, j'|\ell=2, C) \sum_{K=KMIN_j}^{KMAX_j} \sum_{K'=KMIN_{j'}}^{KMAX_{j'}} \frac{CF(K|j, C)}{T_j} \frac{CF(K'|j', C)}{T_{j'}} \quad \ell=2 \\ \\ W(1, 2, 3|\ell=3, C) \sum_{K=1}^7 \sum_{K'=8}^{10} \sum_{K''=11}^{14} \frac{CF(K|1, C)}{T_1} \cdot \frac{CF(K'|2, C)}{T_2} \cdot \frac{CF(K''|3, C)}{T_3} \quad \ell=3 \end{array} \right.$$

$$= \sum_{C=1}^4 \text{CCOVER}(C+1) \cdot (1 - \text{CFLOS}_c) \quad .$$

The probability of seeing either clouds or the ground (with or without clouds)

$$= \sum_{I=1}^{159} \text{WT}(I) + \text{WT}_{\text{old}}(160) + \text{CCOVER}(1)$$

$$= \sum_{C=1}^4 \text{CCOVER}(C+1) [1 - \text{CFLOS}_c + \text{CFLOX}_c] + \text{CCOVER}(1) = 1 \quad .$$

3-2.9 Subroutine CLOUD0(MODE)

For a detailed description of CLOUD0 see Section 4-2.

3-2.10 Subroutine CLOUD1

Coordinates of the source (XI,ETA,ZETA) and detector (XID, ETAD,ZETAD) are calculated in the Cartesian coordinate system of each cloud with the quantities stored in common CDCORD. Entry CLD E TO C in subroutine CLOUD9 is used to transform from earth to cloud coordinates.

3-2.11 Subroutine CLOUD2(UL,VL,WL)

The altitude (ALTLK(K)) and geographic coordinates (THETALK(K), PHILK(K)) of the intersection of the line-of-sight and the Kth deterministic cloud are calculated in this routine and outputted in common INTRCPT. These results are not used by other cloud-model routines. However, this routine is a convenience to the user. The sight-path integration module can use results of this routine to avoid calling the cloud transfer-coefficient routine (CLOUD3) until the sight-path integration has reached the cloud top.

The input to this subroutine are the direction cosines (UL,VL,WL) of the line-of-sight. The point of intersection is calculated for all clouds which fall in the path. A flow chart is shown in Figure 3-3.

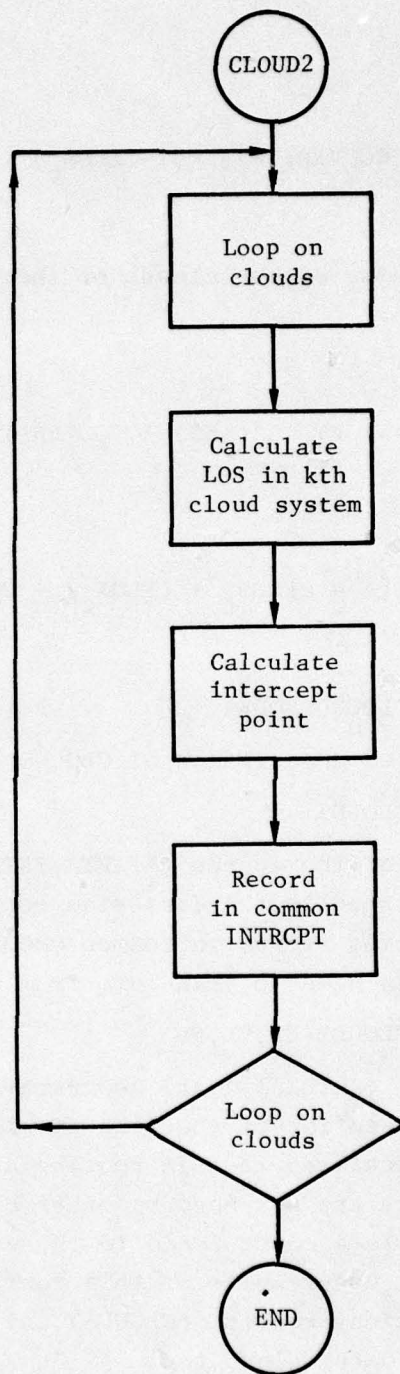


Figure 3-3. Flow chart of subroutine CLOUD2.

3-2.12 Subroutine CLOUD3(UL,VL,WL,K,ALAM,TCOEF,EMISS,SINCLD)

When all of the bookkeeping has been accomplished, CLOUD3 is called to calculate the transfer coefficient (TCOEF) and the emission (EMISS). Branching is required depending upon whether or not the point of intersection of the LOS with the cloud is visible to the source. For those LOS-intersection points which are also illuminated, the bidirectional reflectance is obtained from tables in function CLDBDR. The tabulated values are functions of incident and exit zenith angles and the exit azimuthal angle. The bidirectional reflectance is picked from a bin with no interpolation. The tables are, however, interpolated linearly as a function of wavelength.

The irradiance to all illuminated facets is evaluated. A diffusion calculation is then performed in subroutine DIFFUS to get the radiance exiting the facet of interest.

The thermal emission is calculated from the Planck distribution for the temperature at the point of intersection of the cloud top and line-of-sight.

Before the source irradiation of a cloud is computed, a check is made to determine whether or not the source is either inside the cloud or on its surface. If the source is not outside the cloud, a warning message is printed and, without further calculation, the routine returns a logical variable (SINCLD = TRUE.) to the main program (ROSCOER) which then proceeds to the next case.

We have also devised a prescription which is used if the artificial (point) source is closer to the cloud surface than (approximately) the radius R_s that is assigned to the finite-size artificial source. Let \vec{RP} be the position of the source in the cloud coordinate system and \vec{RS} be the radial distance to the intersection point S of the ray RP with the cloud surface. At point S the outward unit normal is $\hat{n}(\vec{RS})$. Then, for the purpose of this routine, if

$$(\vec{RP} - \vec{RS}) \cdot \hat{n}(\vec{RS}) < R_s ,$$

the source is moved in the direction of $\hat{n}(\vec{RS})$ an amount δP given by

$$\delta P = 0.5 [R_s - (\vec{RP} - \vec{RS}) \cdot \hat{n}(\vec{RS})] .$$

A message is printed with the original and altered coordinates of the source.

3-2.13 Subroutine CLOUD9(RTP1,RTP2,RTP3,EC1,EC2,EC3,K)

Transformations are made between the earth-centered polar coordinate system and the cloud-centered Cartesian system of the Kth cloud. This routine has two entry points. Entries CLD E TO C and CLD C TO E transform from earth to cloud and cloud to earth, respectively.

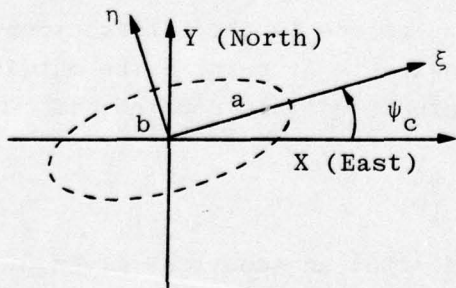
The cloud geometry is most easily described in the cloud principal-axis system (ξ, η, ζ) in which the equation of the cloud surface is

$$\frac{\xi^2}{a^2} + \frac{\eta^2}{b^2} + \frac{\zeta^2}{c^2} = 1 \quad .$$

The location of the cloud center (earth-centered polar coordinates) is (R_c, θ_c, ϕ_c) where

$$\begin{aligned} R_c &= R_{\text{earth}} + H_c, \quad H_c = \text{H CLOUD (km)} \\ \theta_c &= \text{THETCD (degrees)} \\ \phi_c &= \text{PHICD (degrees)}. \end{aligned}$$

Looking from above the cloud toward the earth center:



$$\left. \begin{aligned} \psi_c &= \text{CLDPSI} \\ \xi &= X \cos \psi_c + Y \sin \psi_c \\ \eta &= Y \cos \psi_c - X \sin \psi_c \\ \zeta &= Z \end{aligned} \right\} (1)$$

The transformation from the earth-centered Cartesian system (x,y,z) to the non-rotated ($\psi_c=0$) Cartesian system (X,Y,Z) in the cloud can be performed with two rotations and one translation.

The first intermediate coordinate system (x',y',z') is obtained by making a counterclockwise (positive) rotation

$$\phi = \phi_c + \pi/2$$

about the z -axis such that the x' -axis is normal to the vector \vec{R}_c to the cloud center. The $(\pi/2)$ -term is introduced to make the positive X -axis of the cloud point east. The transformation is

$$\begin{pmatrix} x' \\ y' \\ z' \end{pmatrix} = R_1(\phi) \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

where the transformation matrix R_1 is given by

$$R_1(\phi) = \begin{pmatrix} \cos \phi & \sin \phi & 0 \\ -\sin \phi & \cos \phi & 0 \\ 0 & 0 & 1 \end{pmatrix}.$$

The second intermediate coordinate system (x'',y'',z'') is obtained by making a counterclockwise (positive) rotation θ_c about the x' -axis such that the z'' -axis lies along the vector \vec{R}_c . The transformation is

$$\begin{pmatrix} x'' \\ y'' \\ z'' \end{pmatrix} = R_2(\theta) \begin{pmatrix} x' \\ y' \\ z' \end{pmatrix}$$

where

$$R_2(\theta) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & \sin \theta \\ 0 & -\sin \theta & \cos \theta \end{pmatrix}.$$

Finally, the non-rotated cloud system (X,Y,Z) is related to the (x'',y'',z'') system by a translation along the z'' -axis:

$$Z = z'' - R_c$$

where

$$R_c = R_{\text{earth}} + H_c .$$

Collating our results we have

$$\begin{pmatrix} X \\ Y \\ Z+R_c \end{pmatrix} = \begin{pmatrix} x'' \\ y'' \\ z'' \end{pmatrix} = R_2(\theta)R_1(\phi) \begin{pmatrix} x \\ y \\ z \end{pmatrix} \quad (2a)$$

with

$$R_2(\theta)R_1(\phi) = \begin{pmatrix} -\sin \phi_c & \cos \phi_c & 0 \\ -\cos \theta_c \cos \phi_c & -\cos \theta_c \sin \phi_c & \sin \theta_c \\ \sin \theta_c \cos \phi_c & \sin \theta_c \sin \phi_c & \cos \theta_c \end{pmatrix} . \quad (2b)$$

Thus, an arbitrary point in earth-centered polar coordinates (R, θ, ϕ) has earth-centered Cartesian coordinates (x,y,z) and cloud principal-axis coordinates (ξ, η, ζ) where

$$(x,y,z) = (R \sin \theta \cos \phi, R \sin \theta \sin \phi, R \cos \theta)$$

and the coordinates (X,Y,Z) and (x,y,z) are related by Equations (2a) and (2b). Finally (ξ, η, ζ) and (X,Y,Z) are related by Equation (1), or equivalently

$$\begin{pmatrix} \xi \\ \eta \\ \zeta \end{pmatrix} = R_1(\psi_c) \begin{pmatrix} X \\ Y \\ Z \end{pmatrix} .$$

The transformation from the cloud system to the earth system may be done by doing the same steps in reverse order and using the transposed transformation matrices.

3-2.14 Subroutine CONVERT(R,TH,PH,X,Y,Z)

This subroutine has entry points to transform from polar to Cartesian and Cartesian to polar coordinates. The entry points are POL TO CT and CT TO POL with arguments as follows:

Y - Cartesian X-coordinate
Y - Cartesian Y-coordinate
Z - Cartesian Z-coordinate
R - Radius in spherical coordinate system
TH - Polar angle in spherical coordinate system
PH - Azimuthal angle in spherical coordinate system.

3-2.15 Subroutine DIFFUS(K,ALAM)

The computations involved in subroutine DIFFUS are those from Appendix A and as described in Section 2-1. Communication with this routine is from CLOUD3.

3-2.16 Subroutine DIFPRM(ALAM)

Given a wavelength between two and five microns, this subroutine interpolates microscopic scattering and extinction cross-sections in μm^2 , converts to macroscopic cross-sections in units of km^{-1} , and records the modified diffusion parameters, as defined in Section A-1.2, for each of the 14 cloud types of the data base.

INPUT:

ALAM: wavelength of photon (μm)

OUTPUT: (common DIFFUS, arrays of 14-word length)

DALFA \equiv a in Appendix A Equation (2) (dimensionless)

DBETA \equiv b in Appendix A Equation (2) (km)

DKAPPA \equiv K in Appendix A Equation (19) (km^{-1})

For large-particle-size clouds (i.e., cloud-types 11,12,13 and 14), the small wavelength approximations $\sigma_T = 2\pi r^2$ and $\sigma_S = (1+W)\pi r^2$ are used. Here, 1 and W are, respectively, the diffracted and specular-reflected components of the scattering.

3-2.17 Function DSURF(THETA,PHI,K)

Differential area elements on the surface of an ellipsoid are calculated in this routine as a function of θ and ϕ . The cloud number K must also be transmitted to the function as it obtains the ellipsoidal parameters from common CDCORD.

3-2.18 Function EMISSF(ALAM,LL,MM,HH)

This function provides the thermal emission ($W/(km^2 \text{ sr } \mu m)$) from clouds, attenuated by clear air to an altitude of 12 km.

3-2.19 Subroutine ESURF(THI,THR,PSI,ZKM,MSM,DD,SPCULR,ZLAM,IDAY,IFIRES,ESURFI,SFR,EPST,TKS)

This subroutine, a dummy routine for the real one, provides the surface upwelling radiation and earth bidirectional reflectance. The description is given in Reference 6.

3-2.20 Function IPRIME(II)

This function provides a mapping of the facet areas and radii onto those of the first octant. This symmetry is utilized to obviate storing redundant data.

3-2.21 Subroutine LINEAR(XD,FXD,XX,FXX,NX)

LINEAR performs a linear interpolation with an expeditious technique to find the pair of tabular points which bound the point of interest. The interpolation is then

$$Y = Y_{i-1} + \frac{Y_i - Y_{i-1}}{X_i - X_{i-1}} (X - X_{i-1})$$

INPUTS:

XX: array of points in independent variable
FXX: array of points in dependent variable
NX: number of points in the table
X0: value of independent variable for which dependent variable is desired.

OUTPUTS:

FX0: dependent variable at value of X0 in independent variable.

3-2.22 Subroutine LOS(K)

Possible lines-of-sight from which the user can select directions are computed and stored in common LOS. There are selection rules based on several criteria. A line-of-sight must obviously intercept a cloud facet; however, the facet is not necessarily illuminated. Facets which would fall within the same field-of-view are not duplicated. See Figure 3-4 for a flow chart.

The first criterion selects first the facets which are both visible and illuminated and orders these from smallest to largest scattering angle. Those facets which are visible but not illuminated are then ordered according to their being closest to the edge of the cloud. The rationale for this ordering is that the cloud will be thinnest along the line-of-sight near the edge.

This routine can produce a maximum of 16 possible lines-of-sight. For a small cloud and large field-of-view, there could possibly be only one.

3-2.23 Function PS(X1,ET1,ZET1,THETA,PHI,K)

This function evaluates a quantity which is proportional to the dot product of the normal to the ellipsoid and a vector from the surface point to the external point. If the quantity is negative, the point is shadowed from the line-of-sight; if positive, the point is visible.

3-2.24 Function RHOEPS(ALAM,CTHETA)

This function evaluates the hemispherical-directional reflectance from the (horizontal) surface of cloud-type 4 (stratocumulus) for radiation of wavelength ALAM reflected into zenith angle \cos^{-1} (CTHETA).

Tabulated in an array called RHO is a set of hemispherical-directional reflectances for the stratocumulus cloud model at wavelengths between 2 and 5 microns and for exit zenith angles whose cosines are 1.0, 0.866, 0.5, and 0.0. The value of 0.0 is a fictitious endpoint to the table to accommodate interpolation. Interpolation is linear in wavelength and cosine theta.

INPUT:

ALAM: wavelength of photon (μm)
CTHETA: cosine of zenith angle for which emissivity is desired.

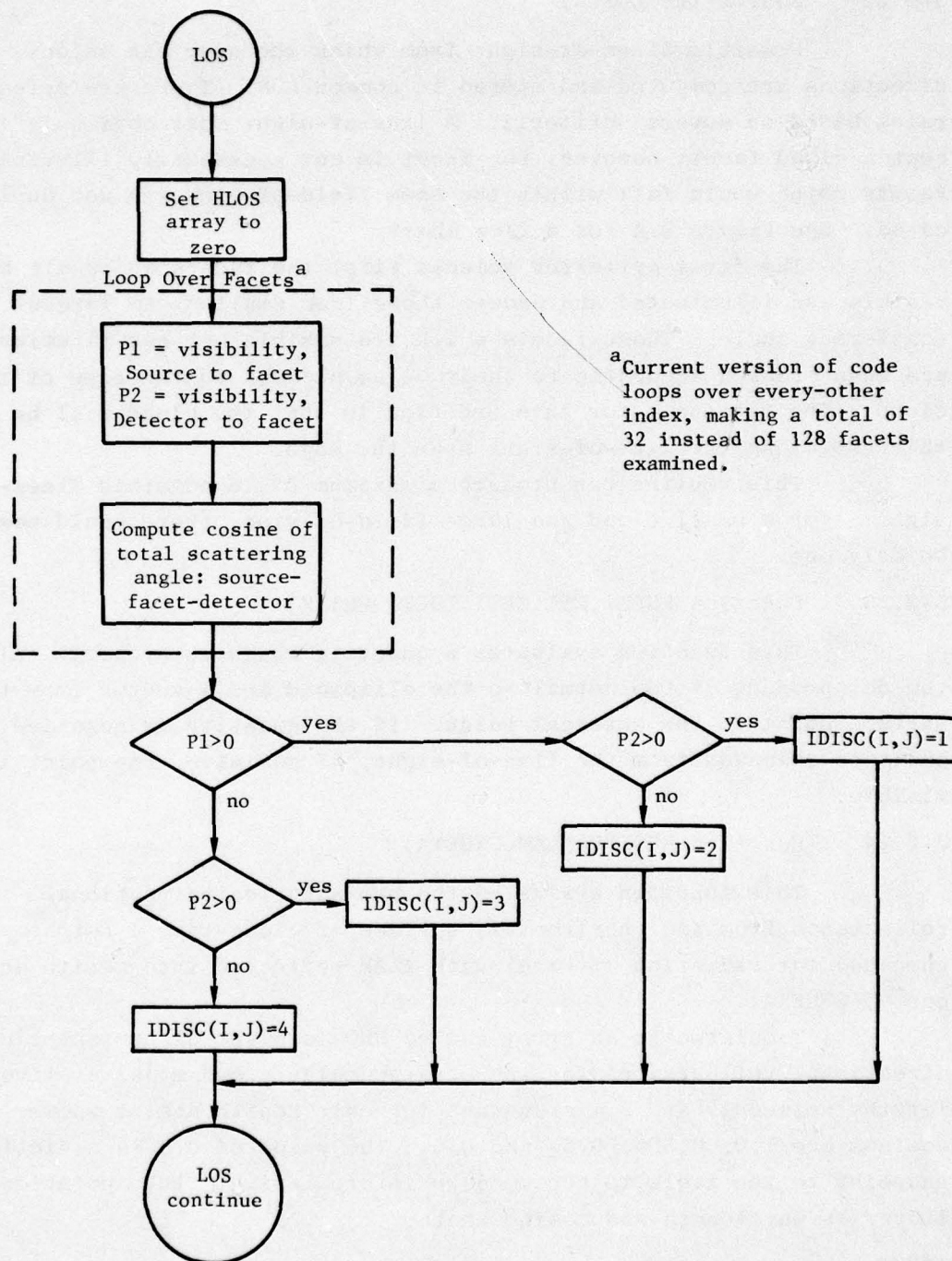


Figure 3-4. Flow chart of subroutine LOS.

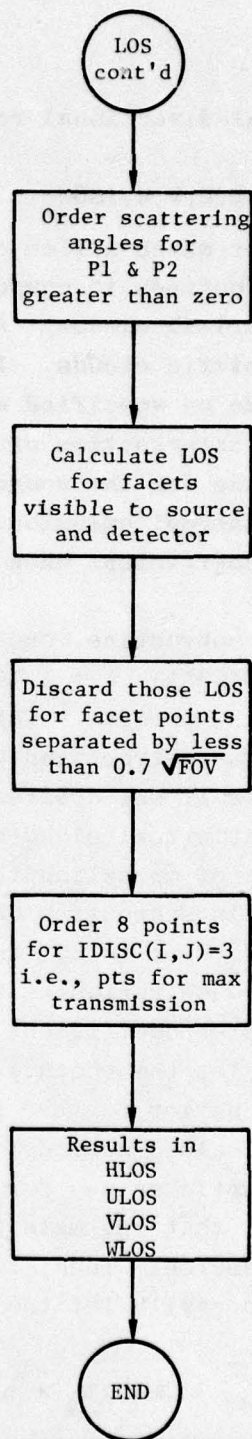


Figure 3-4. Flow chart of subroutine LOS (Cont.).

OUTPUT:

RHOEPS: hemispherical-directional reflectance .

3-2.25 Subroutine SCLLOUD(ALAM,U,V,W,ISUN)

Subroutine SCLLOUD, for which a flow chart is given in Figure 3-5, calls in the required subroutines to compute transfer coefficients and thermal emission for statistical clouds. A source position must be specified, just as for deterministic clouds. It is also required that the solar longitude and latitude be specified when the solar position is above the local horizon at the intersection of the line-of-sight with the earth. Calculations are made for the source (burst) and solar transfer coefficients and the thermal emission. Calculations are bypassed for the solar transfer coefficient when the sun is below the local horizon.

By interrupting this subroutine, one has access to the entire cumulative arrays (TRANS(I), EMISS(I), $I = 1, 160$) in addition to the four fractiles returned to the calling program. This could easily become a normal mode of operation for system-type studies. Also, this (non-implemented) mode is appropriate if one desires calculations for a specific realization of the statistical cloud configurations without going to the deterministic mode of operating the code.

Subroutine SCLLOUD calls subroutine CLDWT to obtain TRANS(I), EMISS(I), and WT(I) for $I=1, 159$. For $I=160$, when the LOS is cloud-free and terminates on the ground, these variables are evaluated in subroutine SCLLOUD. In computing the transfer coefficient for $I=160$, one could get arbitrarily large values if he let the (point) source get arbitrarily close to the ground (cf. the equation for the reflectance transfer coefficient for the statistical cloud submodel near the end of Section 2). To prevent getting such unrealistic values for the transfer coefficient, we have imposed the requirement that the main program assign a radius R_s to the finite-size artificial source. Then, if the altitude h_s of the source is less than R_s , we temporarily let the effective altitude of the finite-size source be

$$h_{\text{eff}} = 0.5 (R_s + h_s) .$$

Thus, if the source is initially placed on the ground so that $h_s = 0$, our prescription places the effective altitude at $0.5 R_s$.

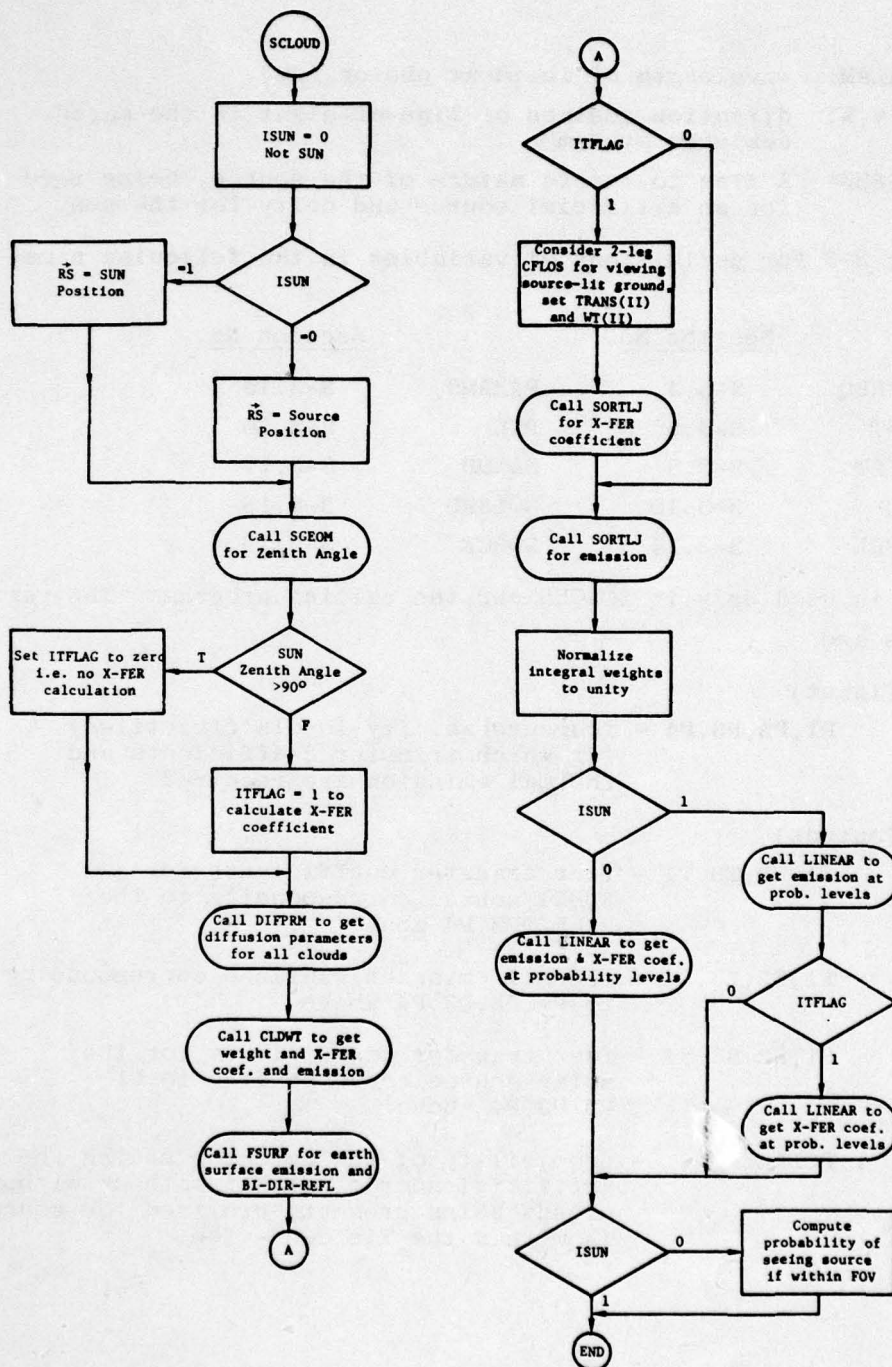


Figure 3-5. Flow chart of subroutine SCLOUD.

INPUTS:

ALAM: wavelength of incident photon (μm)
U,V,W: direction cosines of line-of-sight in the earth-centered system
ISUN: A flag to denote nature of the source, being zero for an artificial source and unity for the sun.

See Section 3-3 for definitions of variables in the following name commons:

	<u>Section No.</u>		<u>Section No.</u>
CLDFREQ	3-3.4	PARAMS	3-3.15
CLDWT	3-3.5	PTE	3-3.16
DETECT	3-3.8	SANDD	3-3.17
FLAGS	3-3.10	SOLARP	3-3.18
MATERL	3-3.14	SORCE	3-3.19

Common PTE is used only in SCLLOUD and the calling program. The variable definitions are

(input)

P1,P2,P3,P4 - four probability levels (fractiles) for which transfer coefficients and thermal emission are required.

(output)

T1,T2,T3,T4 - four transfer coefficients for a NUDET source corresponding to the P1,P2,P3,P4 above

E1,E2,E3,E4 - thermal emission radiance corresponding to P1,P2,P3,P4 above

S1,S2,S3,S4 - four transfer coefficients for the solar source corresponding to P1, P2,P3,P4 above

PCFLOS - probability of the detector seeing the artificial source, either with or without clouds being present, provided the source is within the field-of-view.

3-2.26 Subroutine SGEOM(UL,VL,WL,CLDTOP,XD,YD,ZD,XS,YS,ZS,RDIST,SDIST,THETI,THETE,PHIE)

Subroutine SGEOM, for which a flow chart is given in Figure 3-6, computes the incident and exit zenith angles and the azimuthal scattering angle for a specified source and detector geometry and a given line-of-sight. Also evaluated is the distance (SDIST) from the source to the cloud-LOS intersection point and the horizontal component thereof (RDIST).

INPUTS:

UL,VL,WL: direction cosines of the line-of-sight in the earth-centered coordinate system

CLDTOP: altitude of top of cloud or other specified altitude (km)

XD,YD,ZD: rectangular components of detector position vector in earth-centered system (km)

XS,YS,ZS: rectangular components of source position vector in earth-centered system (km)

OUTPUTS:

SDIST: distance from source to intersection of line-of-sight with cloud top (km)

RDIST: horizontal component of SDIST (km)

THETI: zenith angle to source position at intersection point of LOS with CLDTOP-altitude (degrees)

THETE: zenith angle to detector position (degrees)

PHIE: azimuthal angle of scattering of photon (degrees)

3-2.27 Subroutine SORTLJ(A,B,C,N,LOHI)

This subroutine sorts an array in either ascending or descending order and carries two additional arrays with the ordering. The argument-list variables are as follows:

A is the array to be sorted

B array carried along with the sorting on A

C array carried along with the sorting on A

N is the number of elements in arrays A,B, and C

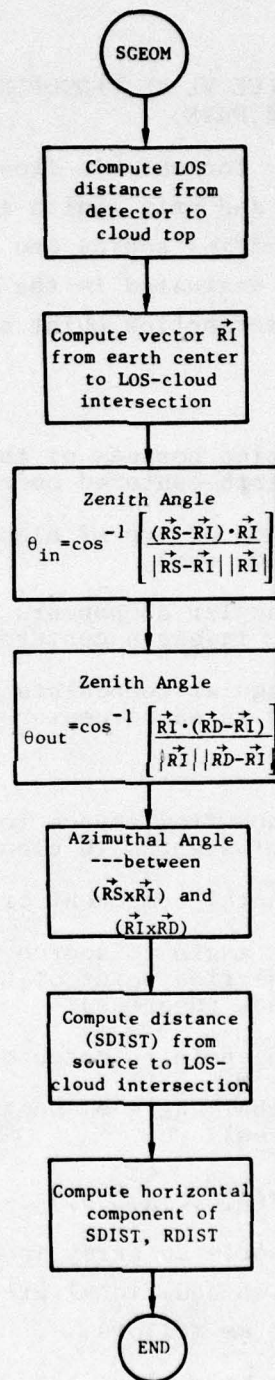


Figure 3-6. Flow chart of subroutine SGEOM.

LOHI is the ordering flag

>0 sorts from high to low

≤0 sorts from low to high.

3-2.28 Function TAIR(ALAM,THETA,ALT)

Air transmittance, T , for radiation of wavelength λ from altitude h to 12 km along a path at zenith angle θ was calculated using LOWTRAN 3 for the U.S. 1962 Standard Atmosphere. The data are cataloged in this function.

The independent variables are:

wavelength: $2 \leq \lambda \leq 5$ microns

zenith angle: $0 \leq \theta \leq 85$ degrees

altitude: $1 < h < 12$ kilometers.

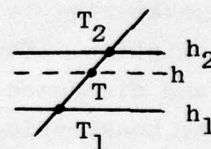
The interpolation (and extrapolation for $\theta > 85$ degrees and $h < 1$ km) used is linear in (T, λ) -, $(\ln T, \sec \theta)$ -, and $(\ln T, h)$ -space. More explicit formulas follow:

Altitude

$$T = ae^{bh}$$

$$b = \ln \left(\frac{T_2}{T_1} \right) / (h_2 - h_1)$$

$$a = T_1 e^{-bh_1} ,$$



which implies

$$\ln T = \ln T_1 - (\ln T_1 - \ln T_2) \frac{h - h_1}{h_2 - h_1} .$$

Angle

$$T = ab^{\sec \theta}$$

$$b = (T_2/T_1)^{(\sec \theta_2 - \sec \theta_1)^{-1}}$$

$$a = T_1 / b^{\sec \theta_1} ,$$

which implies

$$\ln T = \ln T_1 + (\ln T_2 - \ln T_1) \left[\frac{\sec\theta - \sec\theta_1}{\sec\theta_2 - \sec\theta_1} \right] .$$

For $\theta > 85$ degrees, we redefine $\sec\theta$ by a parabolic approximation to the Chapman function,

$$\sec\theta = \sec(85 \text{ deg}) + 1.1 (\theta - 85)^2 .$$

Wavelength

$$T = T_1 + (T_2 - T_1) \frac{\lambda - \lambda_1}{\lambda_2 - \lambda_1} .$$

3-2.29 Function TRANSF(ALAM,LL,MM,HH)

This function evaluates the transfer coefficient for the set of statistical clouds whose indexes are in the calling sequence: Considerable bookkeeping is accomplished to assign the calculation to the proper prescription. The prescriptions are adequately documented in Appendix A and discussed in Section 2-2.

The bookkeeping, in general, evaluates the diffusion parameters for the appropriate layer number and stores them according to the required variable name for the prescription. The first steps are to determine how many layers are involved in the problem, whether the source is inside or outside, and whether the cloud layers are continuous. These questions are answered and control transferred to the equation for

reflection,
 1-layer transmission for source inside,
 1-layer transmission for source below,
 2-layer transmission for source below,
 or 3-layer transmission for source below.

The results are then normalized to get a transfer coefficient, TRANSF, which is returned to subroutine CLDWT.

If the altitude ALT of an artificial source above the top of the topmost layer is less than the radius R_s assigned to the finite-size source, the effective altitude of the source in computing the reflectance transfer coefficient is reset to

$$h_{\text{eff}} = \text{CLDTOP} + 0.5 (\text{ALT} + R_s) \quad .$$

3-2.30 Subroutine VSNORM(X,Y,Z,EN1,EN2,EN3,K)

This subroutine computes a unit vector \hat{n} normal to the surface of the ellipsoid at the Cartesian coordinates x,y,z in cloud K.

$$\hat{n} = \frac{1}{Q} \left[\frac{x}{a^2} \hat{i} + \frac{y}{b^2} \hat{j} + \frac{z}{c^2} \hat{k} \right]$$

$$Q = \left[\left(\frac{x}{a^2} \right)^2 + \left(\frac{y}{b^2} \right)^2 + \left(\frac{z}{c^2} \right)^2 \right]^{\frac{1}{2}} \quad .$$

3-3 LABELED COMMON VARIABLE DEFINITIONS

Variables in labeled common are described in this section. Since the subroutines which use these variables are designed to be utilized as part of other codes, i.e., the subroutines are submodules, names are located in labeled commons which will tend to minimize their conflict with other code variable names. A list of the names of labeled commons and the subroutines in which they are found is located in Table 3-1.

The name of each common and the variables which are contained therein will be listed just as they are found in the subroutines. A brief description and the variable units follow the statement.

3-3.1 COMMON/ATMOUP/DUM1(4),RHO,TT,DUM2(22)

RHO: $\text{RHO}(\text{g/cm}^3)$, the air density at altitude $z(\text{km})$, is used by the main program ROSCOER to scale the radius of the artificial source with altitude.

TT: TT (degrees Kelvin), the air temperature at altitude $z(\text{km})$, is used by the cloud routines.

(RHO and TT, the only two variables from this common, are obtained by a call to ATMOSU(2,ZH), where ZH is the altitude of interest, (km)).

Table 3-1. List of subroutines and labeled commons.

SUBROUTINE	COMMON															
	ATMOUP	CDCORD	CDDATA	CLDFREQ	CLDWT	CLOUD	CONFIG	DETECT	DIFFUS	FLAGS	FLUX	INTRCPT	LOS	MATERL	PARAMS	PTE
ROSCOER	X					X		X				X	X	X	X	X
ATMOSU	X															
BLKDAT			X	X												
CLDBDR			X													
CLDGEOM		X				X								X		
CLDWT				X	X		X									
CLOUD0				X		X	X							X		
CLOUD1		X				X		X						X		X
CLOUD2		X				X		X				X		X		
CLOUD3	X	X				X		X			X			X		X
CLOUD9						X								X		
DIFFUS		X	X			X					X			X		
DIFPRM			X						X					X		
DSURF		X														
EMISSF	X		X											X		X
LOS		X				X		X					X	X		
PS		X												X		
SCLLOUD				X	X			X		X				X	X	X
SGEOM														X		
TRANSF			X						X	X				X		X
VSNORM		X														

3-3.2 COMMON/CDCORD/XI(1,20),ETA(1,20),ZETA(1,20),XID(20),ETAD(20),
ZETAD(20),ASQ(20),BSQ(20),CSQ(20),CPH(5,20),CTH(5,20),CPHBAR
(16,20),CTHBAR(8,20),CRBAR(4,4,20),CAREA(4,4,20)

Variables in this common provide communication between the geometry routines of the deterministic cloud calculations. Calculations relative to a given cloud are made in a coordinate system centered on that cloud and results, if required, are transformed back to the earth-centered system. Ellipsoidal elemental areas used in integration are referred to as facets.

XI,ETA,ZETA: Cartesian coordinates of the Nth source in the Kth cloud-centered system. N currently is restricted to one. (km)

XID,ETAD,ZETAD: Cartesian coordinates of the detector in the Kth cloud-centered system. (km)

ASQ,BSQ,CSQ: Values of the squares of the semi-axes of an ellipsoid. (km²)

CPH: Cloud-centered azimuthal angle bounding a facet or area on the surface of the cloud. (radians)

CTH: Cloud-centered polar angle bounding a facet on the surface of the cloud. (radians)

CPHIBAR: Cloud-centered azimuthal angle locating a facet center in the Kth cloud. Symmetry is taken into account in the eight octants. (degrees)

CTHBAR: Cloud-centered polar angle locating a facet center in the Kth cloud. (degrees)

CRBAR: Distance from the cloud center to the facet center, utilized in calculating fluxes. All symmetry is taken into account and the function IPRIME locates the element in the CRBAR array which has the proper distance to one of the 128 facets when there are 16 azimuthal angles and 8 polar angles. (km)

CAREA: Areas of the facets are calculated by a 2-dimensional Simpson's rule of integration in subroutine CLDGEOM with the differential area element being calculated in DSURF. Again, function IPRIME returns the proper index to obtain the desired area element. (km²)

3-3.3 COMMON/CDDATA/ALAMT(10),SIGT(10,14),SIGS(10,14),W(10),
 XMUBAR(10,14),DNO(14),RAD(14),CLDBASE(14),CLDTHK(14)

Data in this common are physical and optical properties of the cloud data base. Physical properties are taken from the NASA cloud data base and optical properties for cloud types 1 through 10 are from Mie theory calculations. There are 14 types of clouds in this data base for which data are tabulated at ten wavelengths.

ALAMT: ALAMT is a table of wavelengths for which microscopic cross-sections and mean cosines of scattering angles are tabulated. Values are 2.0, 2.5, 2.55, 2.65, 2.75, 2.85, 3.2, 3.5, 4.0, and 5.0. (μm)

SIGT: Microscopic extinction cross-sections for the 14 cloud types are tabulated at the 10 wavelengths of the ALAMT table. (μm^2)

SIGS: Scattering cross-sections for the 14 cloud types are tabulated at the 10 wavelengths of the ALAMT table. (μm^2)

W: (Normalized) contribution of specularly-reflected radiation to scattered radiation, with the diffracted radiation contributing unity; used only for the large-particle-size clouds, types 11 through 14. (dimensionless)

XMUBAR: Cosine of the scattering angle averaged over the particle size distribution of the cloud type and tabulated at the 10 wavelengths. (dimensionless)

DNO: Droplet density of the given cloud type. (droplets/ cm^3)

RAD: Mean droplet radius for the cloud type. (μm)

CLDBASE: Cloud-base altitudes for the 14 cloud types. (km)

CLDTHK: Cloud thickness. (km)

3-3.4 COMMON/CLDFREQ/KMODEL,CCOVER(5,11),CLDFREQ(17,4,11)

Common CLDFREQ has its origin in block data. The index KMODEL selects one of the ten sets of data present in data statements or allows a user-supplied set of data to be input as the eleventh set of data.

KMODEL: A variable which selects the cloud data base to be used in the calculations.

- =1 for dry annual average
- =2 for dry winter average night
- =3 for dry winter average day
- =4 for dry summer average night
- =5 for dry summer average day
- =6 for moist annual average
- =7 for moist winter average night
- =8 for moist winter average day
- =9 for moist summer average night
- =10 for moist summer average day
- =11 for array supplied by the user.

See Section 4 for a detailed illustration of using
KMODEL = 11.

CCOVER: This array provides the probability of the Lth cloud-coverage category for the Kth model, K being defined above, where

$$\sum_{L=1}^5 \text{CCOVER}(L,K) = 1 \quad .$$

For the K = 11 base, the input instructions in Section 4 illustrate the use of the table. CCOVER(L,K) is a frequency of occurrence of the Lth coverage category.

CLDFREQ: With the indexes (I,L,K), CLDFREQ(I,L,K) is the frequency of the Ith cloud type for I less than fifteen. For I = 15,16,17 it is the frequency of occurrence of 1-layer, 2-layers, or 3-layers, respectively. For K-values between 1 and 10 (inclusive) the array elements are from the model as defined under KMODEL above. For K = 11, the use of the table is described in Section 4. Basically, however, each element is the frequency of the Ith type of cloud:

- | | |
|-------------|--------------|
| I=1 for Cu1 | I=8 for Ac |
| I=2 for Cu2 | I=9 for As1 |
| I=3 for Cu3 | I=10 for Cb2 |
| I=4 for Sc | I=11 for Cb3 |
| I=5 for St | I=12 for As2 |
| I=6 for Cb1 | I=13 for Ci |
| I=7 for Ns | I=14 for Cs |

3-3.5 COMMON/CLDWT/IDX,WT(160),TRANS(160),EMISS(160)

The common array WT contains the probability of a given statistical cloud configuration, i.e., the product of the probability of a given cloud-coverage category, the probability of the number of layers in that coverage category, and the probability of an occurrence of a cloud type in that layer and category configuration. This configuration is ultimately weighted by one minus the cloud-free line-of-sight for this cloud coverage and zenith angle.

There are 160 combinations of layer-type-coverage configurations. Subsets of restrictions on any of the components, e.g., coverage category, reduces the 160 to a fewer number of cases.

IDX: This is the total number of configurations which is always less than 160. With a maximum constraint, it can be as few as two, i.e. the cloud type (with coverage category specified) and the cloud-free line-of-sight component.

WT: WT(IDX) is the probability of the IDXth configuration. IDX is less than or equal to 160.

TRANS: TRANS(IDX) is the transfer coefficient for the IDXth configuration. It corresponds to either a transmission or a reflection and includes attenuation by the atmosphere (1962 U.S. standard via LOWTRAN-3) to an altitude of 12 km. (sr^{-1})

EMISS: EMISS(IDX) is the thermal emission spectral radiance attenuated to 12-km altitude. ($\text{W}/(\text{km}^2 \text{ sr } \mu\text{m})$)

3-3.6 COMMON/CLOUD/NCLOUD,HCLOUD(20),THETCD(20),PHICD(20),CLOUDA(20),CLOUDB(20),CLOUDC(20),CLDPSI(20),KCLOUD(20)

Input deterministic cloud descriptions are read into these arrays by subroutine CLOUD0. As many as twenty clouds can be part of the calculations; however, there are no interacting clouds, i.e., reflections of one cloud to another are not considered.

NCLOUD: Number of deterministic clouds for which altitude, orientation, and semiaxes are to be read into the arrays. This variable is used as the upper limit on DO-loops throughout the code.

THETCD: Colatitude of the cloud. (degrees)

PHICD: East longitude of the cloud. (degrees)

CLOUDA: Semiaxis of the longer cloud axis in horizontal plane. (km)

CLOUDB: Semiaxis of the shorter cloud axis in the horizontal plane. (km)

CLOUDC: Semiaxis of the cloud in vertical direction. (km)

The values of a, b, and c are those in the equation of an ellipsoid:

$$\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 + \left(\frac{z}{c}\right)^2 = 1$$

CLDPSI: Azimuthal angle, measured counterclockwise looking down, orienting cloud about (vertical) z-axis. Clouds are normally oriented with (+a)-axis eastward (psi = 0). (degrees)

KCLOUD: Index for Kth cloud, representing one of the 14 cloud types from the data bank.

3-3.7 COMMON/CONFIG/CTYPL(8),CTYPM(4),CTYPH(5),CFLAG,C1,C2

This common is a bit unwieldy but is used in the input routine CLOUD0. The entries are the Hollerith names of the cloud types in the low, middle, or high layer.

CTYPL(LL): Type of cloud LL ($1 \leq LL \leq 7$) or no cloud (LL=8) in the low layer. The variable is left-justified in 5-column fields.

CTYPM(MM): Type of cloud MM ($1 \leq MM \leq 3$) or no cloud (MM=4) in the middle layer.

CTYPH(HH): Type of cloud HH ($1 \leq HH \leq 4$) or no cloud (HH=5) in the high layer.

CFLAG: CFLAG is a coverage category flag. (Not utilized)

C1: C1 is the (integer) index for the first cloud-coverage category being utilized. Normally C1 is 2.

C2: C2 is the upper limit counterpart of C1. Normally C2 is 5.

3-3.8 COMMON/DETECT/HD, THETAD, PHID, FOV

This common contains the location of the detector in an earth-centered polar coordinate system.

HD: Altitude of the detector. (km)

THETAD: Colatitude of detector. (degrees)

PHID: East longitude of detector. (degrees)

FOV: Field-of-view (FOV) of the detector (km^2).
Radiances in the deterministic cloud calculations are averaged over the field-of-view. The FOV is also used in subroutine LOS, as potential lines-of-sight are separated by the order of the square root of the FOV.

3-3.9 COMMON/DIFFUS/DALFA(14), DBETA(14), DKAPPA(14)

This common contains the coefficients in the diffusion equation for photon flux transmitted through clouds. They are generated for all fourteen clouds by a single call to DIFPRM for a specified wavelength.

DALFA: Diffusion parameter defined in Appendix A-1.2. (unitless)

DBETA: Diffusion parameter defined in Appendix A-1.2. (km)

DKAPPA: Diffusion parameter defined in Appendix A-1.2. (km^{-1})

3-3.10 COMMON/FLAGS/ITFLAG

This common is currently used only to avoid calculation of the transfer coefficient in function TRANSF in the statistical calculations when only the thermal emission is needed.

ITFLAG: ITFLAG turns off the transfer coefficient computation as described above.

3-3.11 COMMON/FLUX/FIN(8,16), FOUT(8,16)

This common provides communication between subroutine CLOUD3, which generates the input FIN to subroutine DIFFUS and uses the output FOUT, and the subroutine DIFFUS. DIFFUS effects the diffusion solution to get the photon flux output at each of the facets, given the input flux.

FIN: This is 4π times the photons $\text{km}^{-2} \text{sec}^{-1}$ that are incident normally on each of the cloud facets which are visible to the unit strength, isotropic source.

FOUT: This is 4π times the photon flux (radiant emittance) that is transmitted by each facet, according to the diffusion theory approximation. (4π photons/ $\text{km}^2 \text{sec}$), for unit-strength source).

3-3.12 COMMON/INTRCPT/ALTLK(20),THETALK(20),PHILK(20)

This common provides communication between subroutine CLOUD2 and the calling program which is requesting the geographic location of the intersection of the line-of-sight and the cloud.

ALTLK: The altitude at which the line-of-sight intercepts the Kth cloud. (km)

THETALK: The colatitude of the Kth cloud intercept. (degrees)

PHILK: The east longitude of the Kth cloud intercept. (degrees)

3-3.13 COMMON/LOS/HLOS(1,64),ULOS(1,64),VLOS(1,64),WLOS(1,64)

This common contains lines-of-sight to all facets of deterministic clouds which provide reflectance and to those facets which have the highest transmission. These are provided following a call to subroutine LOS with the argument K for the Kth cloud.

HLOS: Altitude at which the line-of-sight from the detector intercepts the Jth facet in the Kth cloud. (km, above mean sea level)

ULOS,VLOS,WLOS: Direction cosines in the earth-centered Cartesian system, of the above-described lines-of-sight.

Each of the vectors (ULOS,VLOS,WLOS) provides to the code user a potential line-of-sight which is separated by approximately the square root of the field-of-view from another possible line-of-sight.

3-3.14 COMMON/MATERL/MSM,DDM(7),SRFALT

MSM: Integer defining surface type.

=1 for Lambertian diffuse surface with spectrally-independent reflectance set by DD(1) and emissivity by (1.-DD(1)).

=2 for water

=3 for snow

=4 for sand
 =5 for soil
 =6 for foilage
 =7 for urban material

DDM(M): Additional descriptor for selected surface material.
 See comments in subroutine ESURF, a routine provided by the model documented in Reference 6.

SRFALT: Surface altitude. (km)

3-3.15 COMMON/PARAMS/IN,IOUT,PI,RE,DTR,RTD

This common contains program constants, set in program ROSCOER, which are frequently used in numerous routines. The constants can be replaced by equivalencing or renaming variables.

IN: The integer variable name used to identify the input file unit. It is not used consistently.

IOUT: The integer variable name which identifies the output file unit. It is not used consistently.

PI: The value of PI as used throughout the program. It has the numerical value of 3.14159265.

RE: The value used for the Earth's radius and has a numerical value of 6371.03 km.

DTR: This is the conversion factor to convert from degrees to radians and has a numerical value of 0.01745329251994.

RTD: This is the conversion factor from radians to degrees and has a numerical value of 57.2957795131.

3-3.16 COMMON/PTE/P1,P2,P3,P4,T1,T2,T3,T4,S1,S2,S3,S4,E1,E2,E3,E4

P1...P4: Probability fractiles at which transfer coefficients and emission radiances are desired. Set in program ROSCOER.

T1...T4: Transfer coefficients at 12-km altitude for point source. This is the ratio of a radiance to an irradiance. (sr^{-1})

S1...S4: Transfer coefficients at 12-km altitude for sun as a source. (sr^{-1})

E1...E2: Thermal emission (spectral radiance) from top layer of clouds or the ground (for the cloud-free line-of-sight). ($\text{W}/(\text{km}^2 \text{ sr } \mu\text{m})$)

PCFLOS: Probability of the detector seeing the artificial source, either with or without clouds being present, provided the source is within the field-of-view.

3-3.17 COMMON/SANDD/XS,YS,ZS,XD,YD,ZD,UL,VL,WL

The common SANDD contains the Cartesian coordinates of the location of both the source and detector, and the direction cosines of the line-of-sight.

XS,YS,ZS: Cartesian coordinates of the source location in the earth-centered system. The x-direction points to zero degrees longitude and ninety degrees colatitude. The z-direction is through the north pole. (km)

XD,YD,ZD: Cartesian coordinates of the detector location in the earth-centered system. (km)

UL,VL,WL: Direction cosines of the line-of-sight vector in the earth-centered system.

3-3.18 COMMON/SOLARP/SOLLAT,SOLLON

SOLLAT: Solar latitude in earth-centered polar coordinates with positive being north of the equator. (radians)

SOLLON: Solar (east) longitude in earth-centered polar coordinates. (radians)

3-3.19 COMMON/SORCE/NSORCE,HSORCE(1),THETAS(1),PHIS(1),RSORCE(1)

NSORCE: This variable is not utilized in this version of the code, and it is always set to one.

HSORCE: Altitude of source. (km)

THETAS: Colatitude of source. (degrees)

PHIS: East longitude of source. (degrees)

RSORCE: Radius of source. (km)

3-3.20 COMMON/XX1111/KCLDK,CLDLAM

KCLDK: A test-flag used in subroutine CLOUD3 to determine whether CLOUD3 is now being called with the same cloud-number K as for its last call.

CLDLAM: A test quantity used in subroutine CLOUD3 to determine whether CLOUD3 is now being called with the same wavelength ALAM as for its last call.

Note: If K and ALAM inputted to subroutine CLOUD3 have the same values as in the last call, the subroutine bypasses its call to subroutine DIFFUS(K,ALAM). Both KCLDK and CLDLAM are initialized in the main program to the arbitrary, out-of-range values of 99 and -99., respectively.

SECTION 4

DATA REQUIREMENTS AND SAMPLE PROBLEMS

4-1 DATA REQUIRED FOR STATISTICAL AND DETERMINISTIC CLOUDS

Required user-supplied data for transmission of IR signatures through clouds are read by CLOUD0. Many of the data, as outlined in the following paragraphs, are stored in the program and the code need only be directed by an appropriate flag to use them. Consequently, only a few directives need be inputted to run standard cases. Data cataloged in the program are described first, followed by descriptions and illustrations for user-supplied data.

Data which are cataloged are accessible to both the statistical and deterministic submodules. Only a limited number of sets of data are included in the code to demonstrate the utility of the code without its becoming unwieldy.

Cloud descriptions in terms of mean water droplet radius (μm), droplet density (cm^{-3}), base altitude (km), and thickness (km) are incorporated into the code via BLOCK DATA. These data are tabulated in Table 2-1. Microscopic extinction and scattering cross-sections (μm^2) and average cosine of the scattering angle, averaged (as described in Reference 2) over droplet size distributions from Table 2-1, are also included in BLOCK DATA for 14 cloud types and 10 wavelengths in the 2- to 5- μm range. No provision has been made to replace or adjust these parameters for user-supplied data. A modification could be implemented to provide such an option.

The only bidirectional reflectance data that are in the code are those for a stratocumulus cloud, a frequently occurring cloud type according to the NASA cloud-data bank. The tables in function CLDBDR are rather lengthy. Some considerable effort has been expended to fit the bidirectional reflectance data for inclusion in the code; however, the code contains only tabulated data.

The cloud-frequency data are stored in an array (CFREQ) in BLOCK DATA dimensioned $(14 + 3)$ by 4 by $(10 + 1)$. For each of the 10 (or 11 including the user-option case) region-averaged data sets, there

are 14 cloud-frequency numbers and three layer-frequency numbers for each of the four nonclear coverage categories. Each specification requires five coverage categories, of which four are independent, ranging from completely clear to complete cloud-cover.

Nominal statistical-cloud data sets are included in the program which include averages over summer, winter, day, night, and annual for a dry and a moist region. They are arranged as in Table 4-1.

4-2. USER-REQUIRED AND USER-OPTIONAL DATA FOR NATURAL CLOUD MODULES

For utilizing the ROSCOE-IR natural cloud module in a stand-alone mode, several data are required to be read by the driver program ROSCOER. ROSCOE-IR will provide these data to the natural cloud module as implemented in the ROSCOE-IR code. The requirements for the driver program will be described first, followed by the description of inputs read by subroutine CLOUD0. Sufficient information is included to illustrate the options and to provide test cases for the stand-alone mode.

Detector and source locations are read by the driver program ROSCOER. The first input record contains H , θ , ϕ , and FOV for the detector; the second record contains the same information (less the FOV) for the source. H is the altitude in kilometers, ϕ is the colatitude (degrees), and θ is the east longitude (degrees). FOV is the field-of-view (km^2) for the detector. The third input record contains the flag ISUN which is zero if the only source to be considered is the artificial source and which is unity if the sun is to be considered as a source in addition to the artificial source. The solar location is specified in a data statement in ROSCOER. The fourth input record is the wavelength ALAM.

Subroutine CLOUD0, for which a flow diagram is shown in Figure 4-1, reads all of the user-supplied data and sets the proper flags for subsequent code execution. For the statistical case, only data are read; the deterministic mode (MODE=0) also causes the geometry routines (CLDGEOM, and, in turn, DSURF) to be called.

The flags are set by Card 1 and Card 2.

Card 1: MODE (I10 format)
 = 0 Deterministic model
 = 1 Statistical model
(branch here to required submodule)

Table 4-1. Cloud data bank contained in ROSCOE natural cloud program.

Index for Statistical Cloud Set	Region	Type of Average
1	Dry ^a	Annual
2	Dry ^a	Winter night
3	Dry ^a	Winter day
4	Dry ^a	Summer night
5	Dry ^a	Summer day
6	Moist ^b	Annual
7	Moist ^b	Winter night
8	Moist ^b	Winter day
9	Moist ^b	Summer night
10	Moist ^b	Summer day
11	Array reserved for user-supplied data	

^{a, b} Regions 4 and 11 in Reference 1 nomenclature, i.e., continental and maritime.

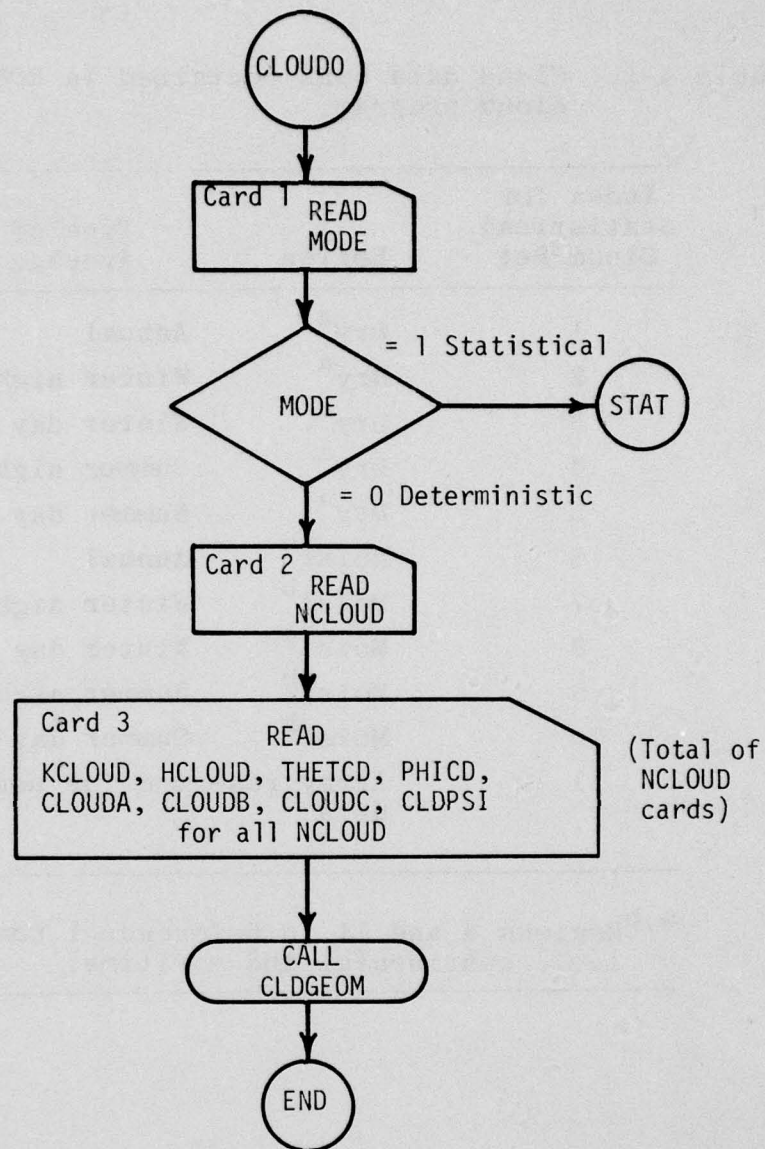


Figure 4-1. Flow chart of subroutine CLOUD0.
(Continued on next page.).

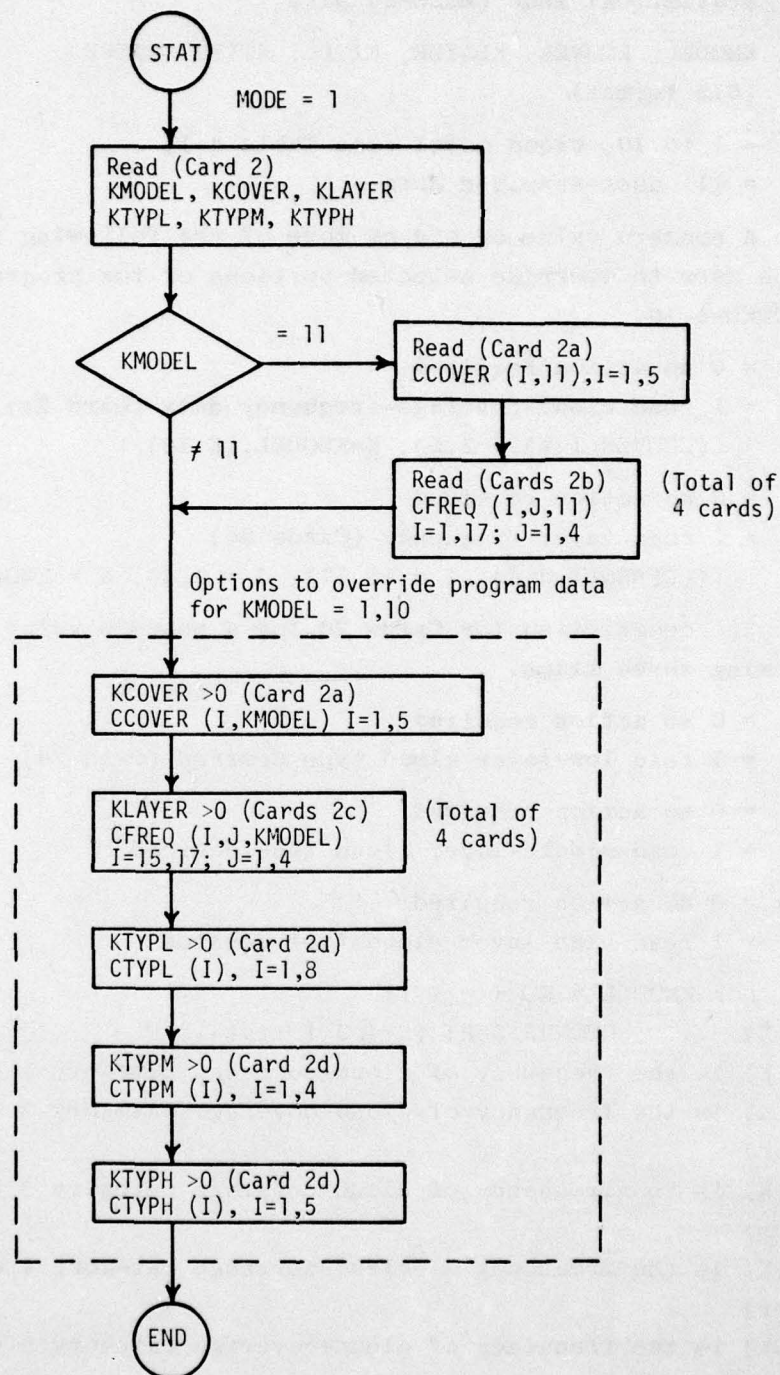


Figure 4-1. Flow chart of subroutine CLOUDO (Cont.).

4-2.1 Statistical Mode (MODE=1) Data

Card 2: KMODEL, KCOVER, KLAYE R, KTYPL, KTYPM, KTYPH
(6I5 format)

KMODEL = 1 to 10, cloud model (see Table 4-1)
= 11, user-supplied data

A nonzero value of one or more of the following five flags allows the user to override selected portions of the program data for a given KMODEL=1,10.

KCOVER = 0 no action required
= 1 read cloud-coverage-frequency data (Card 2a)
((CCOVER(I,K), I=1,5), K=KMODEL.LE.10)

KLAYE R = 0 no action required
= 1 read layer frequency (Cards 2c)
(((CFREQ(I,J,K), I = 15,17), J = 1,4), K = KMODEL.LE.10)

See description for Cards 2d for a nonzero value of any of the following three flags.

KTYPL = 0 no action required
= 1 read low-layer cloud type desired (Card 2d)

KTYPM = 0 no action required
= 1 read middle-layer cloud type desired

KTYPH = 0 no action required
= 1 read high-layer cloud type desired

Card 2a: for KMODEL = K, K = 1,11

CCOVER(1,K), ... , CCOVER(5,K) (5F4.3 format)

CCOVER(1,K) is the frequency of cloud-coverage category 1 (clear)

CCOVER(2,K) is the frequency of cloud-coverage category 2 (0.3 cloud cover)

CCOVER(3,K) is the frequency of cloud-coverage category 3 (0.5 cloud cover)

CCOVER(4,K) is the frequency of cloud-coverage category 4 (0.8 cloud cover)

CCOVER(5,k) is the frequency of cloud-coverage category 5 (complete cover)

$$\text{where } \sum_{I=1}^5 \text{CCOVER}(I,K) = 1.0 \quad .$$

Cards 2b: for KMODEL = 11 (four cards)

CFREQ(I,J,11)	$1 \leq I \leq 17, 1 \leq J \leq 4$	(17F4.3 format)
CFREQ(1,J,K)	is frequency of CU1	} low-altitude clouds
CFREQ(2,J,K)	is frequency of CU2	
CFREQ(3,J,K)	is frequency of CU3	
CFREQ(4,J,K)	is frequency of SC	
CFREQ(5,J,K)	is frequency of ST	
CFREQ(6,J,K)	is frequency of CB1	
CFREQ(7,J,K)	is frequency of NS	
CFREQ(8,J,K)	is frequency of AC	} mid-altitude clouds
CFREQ(9,J,K)	is frequency of AS1	
CFREQ(10,J,K)	is frequency of CB2	
CFREQ(11,J,K)	is frequency of CB3	} high-altitude clouds
CFREQ(12,J,K)	is frequency of AS2	
CFREQ(13,J,K)	is frequency of CI	
CFREQ(14,J,K)	is frequency of CS	

where

$$\sum_{I=1}^{14} \text{CFREQ}(I,J,K) = 1.$$

CFREQ(15,J,K)	is frequency of 1 layer
CFREQ(16,J,K)	is frequency of 2 layers
CFREQ(17,J,K)	is frequency of 3 layers

where

$$\sum_{I=15}^{17} \text{CFREQ}(I,J,K) = 1.$$

Cards 2c: for K = KMODEL = 1,10 (3F4.3 format) (four cards)

Cards 2c provide a mechanism to change layer frequencies for KMODEL < 11, i.e., (((CFREQ(I,J,KMODEL), I=15,17), J=1,4), KMODEL < 11) without changing the individual cloud-type frequencies.

CFREQ(I,J,K), I=15,16,17 and J=1,2,3,4

I=15 is the frequency of 1 layer
=16 is the frequency of 2 layers
=17 is the frequency of 3 layers

Cards 2d: cloud-type specification (8A5 format)
(one, two, or three cards)
Read under 8A5 format (a blank field rejects that cloud type). Data must be left-justified.

For KTYPL = 1 (one card):

CTYPL(I), I=1,8
CTYPL(1) = CU1
CTYPL(2) = CU2
CTYPL(3) = CU3
CTYPL(4) = SC
CTYPL(5) = ST
CTYPL(6) = CB1
CTYPL(7) = NS
CTYPL(8) = CLR = clear

For KTYPM = 1 (one card):

CTYPM(I), I = 1,4
CTYPM(1) = AC
CTYPM(2) = AS1
CTYPM(3) = CB2
CTYPM(4) = CLR

For KTYPH = 1 (one card):

CTYPH(I), I = 1,5
CTYPH(1) = CB3
CTYPH(2) = AS2
CTYPH(3) = CI
CTYPH(4) = CS
CTYPH(5) = CLR

By utilizing combinations of Card 1 through Cards 2d, one can accomplish any degree of specification desired. However, for a complete specification, the problem reduces to that of a deterministic calculation where the thicknesses and altitudes come from the program data bank and the cloud is infinite in lateral extent.

4-2.2 Deterministic Mode (MODE=0) Data

Card 2: N CLOUD (I10 format)

Card 3: K CLOUD(I), H CLOUD(I), THETCD(I), PHICD(I)
CLOUDA(I), CLOUDB(I), CLOUDC(I), CLDPSI(I)
where $1 \leq I \leq \text{N CLOUD}$
(I2, E8.3, 6E10.4 format)

K CLOUD(I) = Cloud-type index of Ith cloud (1,2,...,14)

H CLOUD(I) = Altitude of Ith cloud (km)

THETCD(I) = Colatitude of Ith cloud (degrees)

PHICD(I) = East longitude of Ith cloud (degress)

CLOUDA(I) = Semi-axis in x-direction of Ith cloud (km)

CLOUDB(I) = Semi-axis in y-direction of Ith cloud (km)

CLOUDC(I) = Semi-axis in z-direction of Ith cloud (km)

CLDPSI(I) = Orientation of the a-axis with respect to
the east-west direction, i.e., ψ orients
the longest (a-axis) at an angle of ψ
degrees north of east.

4-3. SAMPLE PROBLEMS

A number of sample computer runs have been made using the ROSCOE natural cloud program. Several of these are included here to facilitate subsequent code comparisons. Listings of input cards necessary for each problem are provided.

Some modifications of the code were required to obtain the data output shown in the samples. Code calculations were affected only as outlined below. Print statements were placed in the code to intercept calculations in a convenient manner for presentation. These are given in Appendix C to facilitate reproducing the output for each problem.

4-3.1 Problems 1 to 4: Use of the Statistical Cloud Submodel in a Limited, Deterministic Mode (with KMODEL=1,10)

The purpose of these four problems, which form a set, is (1) to illustrate use of the statistical cloud submodel in a limited, deterministic mode (with KMODEL=1,10) and (2) to show that diffusion calculations performed by the code for a point source beneath either (a) single-layer (planar) clouds or (b) multilayer (planar) clouds are in good agreement with exact, analytic diffusion calculations.

To help provide the motivation for a portion of these problems, we note that the total transmittance T for a planar slab is given by Equation (31a) of Appendix A, i.e.,

$$T = Q \left[\cosh KL + \frac{1}{2} \left(\frac{a}{Kb} + \frac{Kb}{a} \right) \sinh KL \right]^{-1}$$

where Q , the total flux into the slab, can be set to unity. To get a computer code result that can be compared with this transmittance, we must take several steps:

- a. Instruct the code to treat a single planar cloud above a point source.
- b. Compute the radial distribution of the transmission transfer coefficients, without including air attenuation.
- c. Convert this distribution of transfer coefficients to a radial distribution of radiant exitance.
- d. Integrate this radial distribution of radiant exitance across the cloud top and divide by the spatially-integrated flux into the slab to obtain a total transmittance.

The quantity that the code was actually instructed to compute is one we shall refer to as a modified transfer coefficient, TC' , in units of $\text{km}^{-2} \text{sr}^{-1}$. These units are those of the transfer coefficient (sr^{-1}) divided by the square of the distance from the source to the 12-km altitude transfer point. These units are equivalent to describing TC' as being 4π times the radiance ($\text{W km}^{-2} \text{sr}^{-1}$) directed toward the downward-looking radial-scanning detector, for a unit strength isotopic source. (Alternatively, TC' is 4 times the radiant exitance.) This modified transfer coefficient, $4\pi L$, was divided by 4π and multiplied by π to obtain the radiant exitance and was subsequently integrated across the cloud-top radial distribution. Division by the source power incident on the underside of the cloud gave the total transmittance T :

$$T = \frac{1}{(\frac{1}{2} \text{ source power})} \int_0^\infty \left(\frac{4\pi L}{4\pi} \pi \right) 2\pi r dr$$

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THE ROSCOE MANUAL. VOLUME 24. NATURAL CLOUDS (PHYSICAL AND OPTI--ETC(U)

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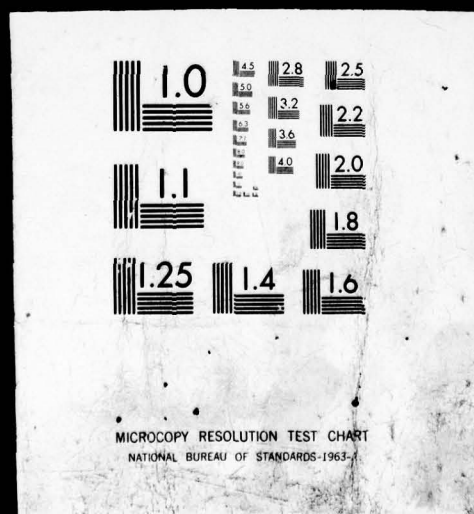


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The information on the input cards read by ROSCOER for the detector, source, and wavelength and by subroutine CLOUD0 for Cards 1,2 and 2d (cf. Figure 4-1 and corresponding text) is given in Figure 4-2 for the four sample problems. Each of the first three problems treats a different single cloud type, namely, Type 4 (Sc), Type 8 (Ac), and Type 13 (Ci), respectively; the fourth problem treats the three-layer configuration of these same cloud types. We shall discuss the input cards later.

For each of the four problems, and for a range of lateral displacements in 0.25-km steps, the values of the modified transfer coefficient, $4\pi L$, are given in Columns 2 to 5 of Table 4-2. These quantities are plotted in Figure 4-3. Columns 6 to 9 of Table 4-2 give the corresponding values of the radial integrals for the transmittance.

In Figure 4-3 the curve for cloud Sc is not shown at larger distances because it soon develops wiggles and, starting at 35.75 km, an occasional negative value. These features result from limitations of the internal integration scheme which is intended to be efficient in the lateral range of importance but not at very large distances. The curve for cloud Ac begins to wiggle a bit at about 20 km, that for cloud Ci at about 30 km, and that for the combined set of clouds (Sc + Ac + Ci) at 7 km.

The analytic results for the transmittance and reflectance of each of the three layers are:

$$\begin{aligned} T(\text{Sc}) &= 0.820 \times 10^{-2} & R(\text{Sc}) &= 0.653 \\ T(\text{Ac}) &= 0.113 \times 10^{-1} & R(\text{Ac}) &= 0.637 \\ T(\text{Ci}) &= 0.127 \times 10^{-6} & R(\text{Ci}) &= 0.0761 \end{aligned}$$

The analytic result for the transmittance of the three-layer configuration is

$$T(\text{Sc} + \text{Ac} + \text{Ci}) = 0.211 \times 10^{-10}$$

which was evaluated from the formula, derived in Appendix D,

$$T_{123} = \frac{T_1 T_2 T_3}{(1 - R_1 R_2)(1 - R_2 R_3) - R_1 R_3 T_2^2}$$


```

***** PROBLEM 1 *****
HD      THETAD  PHID  FOV      DETECTOR
35793.  90.00001 -90.0001 1.
HSORCE(1) THETAS(1) PHIS(1) WKT      SOURCE
0.01    90.000001 -90.00 1000.

ISUN
1

ALAM
2.50

MODE
1

KMODEL  KLAYE  KTYPM
KCOVER  KTYPL  KTYPH
1 0 0 1 1 1

SC
CLR

WAVELENGTH
STATISTICAL CARD 1
USER CLOUD MODEL CARD 2
LAYER 1 CARD 2D
LAYER 2 CARD 2D
LAYER 3 CARD 2D

***** PROBLEM 2 *****
HD      THETAD  PHID  FOV      DETECTOR
35793.  90.00001 -90.0001 1.
HSORCE(1) THETAS(1) PHIS(1) WKT      SOURCE
0.01    90.000001 -90.00 1000.

ISUN
1

ALAM
2.50

MODE
1

KMODEL  KLAYE  KTYPM
KCOVER  KTYPL  KTYPH
1 0 0 1 1 1

CLR

AC

WAVELENGTH
STATISTICAL CARD 1
USER CLOUD MODEL CARD 2
LAYER 1 CARD 2D
LAYER 2 CARD 2D
LAYER 3 CARD 2D

***** PROBLEM 3 *****
HD      THETAD  PHID  FOV      DETECTOR
35793.  90.00001 -90.0001 1.
HSORCE(1) THETAS(1) PHIS(1) WKT      SOURCE
0.01    90.000001 -90.00 1000.

ISUN
1

ALAM
2.50

MODE
1

KMODEL  KLAYE  KTYPM
KCOVER  KTYPL  KTYPH
1 0 0 1 1 1

CLR

CI

WAVELENGTH
STATISTICAL CARD 1
USER CLOUD MODEL CARD 2
LAYER 1 CARD 2D
LAYER 2 CARD 2D
LAYER 3 CARD 2D

***** PROBLEM 4 *****
HD      THETAD  PHID  FOV      DETECTOR
35793.  90.00001 -90.0001 1.
HSORCE(1) THETAS(1) PHIS(1) WKT      SOURCE
0.01    90.000001 -90.00 1000.

ISUN
1

ALAM
2.50

MODE
1

KMODEL  KLAYE  KTYPM
KCOVER  KTYPL  KTYPH
1 0 0 1 1 1

SC
CLR

AC

CI

WAVELENGTH
STATISTICAL CARD 1
USER CLOUD MODEL CARD 2
LAYER 1 CARD 2D
LAYER 2 CARD 2D
LAYER 3 CARD 2D

```

Figure 4-2. Input data for Problems 1 to 4.

Table 4-2. Data output for sample problems 1 to 4. Columns 2 to 4 give the cloud-top radiance L times 4 π as a function of lateral displacement (km) from a unit-strength source at 0.01-km altitude. Wavelength is 2.5 μ m.

RANGE	SC	AC	CI	SC-AC-CI	INT(SC)	INT(AC)	INT(CI)	INT(TOTAL)
0.00	22476-02	33156-03	10700-08	11858-11	2130026-03	3244326-04	1050076-09	-1169766-12
0.25	21655-02	32988-03	10674-08	11798-11	8069928-03	1286708-03	4102248-09	-4596772-12
0.50	19416-02	32498-03	10605-08	11608-11	1666572-02	2850358-03	8355438-09	-1020022-11
0.75	16248-02	31688-03	10498-08	11298-11	2646642-02	4993038-03	1650258-08	1779102-11
1.00	12778-02	30608-03	10338-08	10848-11	3616932-02	7633118-03	2553238-08	2713042-11
1.25	95448-03	29278-03	10138-08	10338-11	4469728-02	1070518-02	3633228-08	3793128-11
1.50	68618-03	27758-03	98918-09	97218-12	5224128-02	1413168-02	4877138-08	4907042-11
1.75	48048-03	26078-03	96208-09	93088-12	5814002-02	1783098-02	6270408-08	6260302-11
2.00	33068-03	24298-03	92208-09	83028-12	6619058-02	2572708-02	7797398-08	7528142-11
2.25	22468-03	22458-03	89948-09	75328-12	7070968-02	3381038-02	1110708-07	8906162-11
2.50	15128-03	20608-03	86528-09	67478-12	7717438-02	4162358-02	1301648-07	1146082-10
2.75	10218-03	18708-03	82938-09	59638-12	8069928-02	5038858-02	1491408-07	1251058-10
3.00	70308-04	17018-03	79258-09	51978-12	7717438-02	6117478-02	1606448-07	1374032-10
3.25	49488-04	15348-03	75528-09	44658-12	7419108-02	7052158-02	1805318-07	1472292-10
3.50	36138-04	13728-03	71778-09	37798-12	7419108-02	8057748-02	2086708-07	1559152-10
3.75	26208-04	12328-03	68058-09	31478-12	7524218-02	9038858-02	2289418-07	1634372-10
4.00	19218-04	10998-03	64008-09	25798-12	7524218-02	1032348-02	2492308-07	1696228-10
4.25	14548-04	97098-04	60048-09	20798-12	7626602-02	1174782-02	2694698-07	1751308-10
4.50	11738-04	87028-04	57398-09	16498-12	7626602-02	1337718-02	2895578-07	1794918-10
4.75	98898-05	77288-04	54088-09	13808-12	7660928-02	1593182-02	3094368-07	1830082-10
5.00	82308-05	68308-04	50928-09	99328-13	7717438-02	1864448-07	3290538-07	1858328-10
5.25	65758-05	60388-04	47928-09	75998-13	7717438-02	2124458-02	3483658-07	1881098-10
5.50	52298-05	53958-04	45088-09	58198-13	7737158-02	2384498-02	3672378-07	1899818-10
5.75	44668-05	47058-04	42408-09	45108-13	7737158-02	2624658-02	3859458-07	1915778-10
6.00	41548-05	42458-04	39808-09	36168-13	7776348-02	2824658-02	4041608-07	1930068-10
6.25	38018-05	37688-04	37528-09	30318-13	7810278-02	3031818-02	4211928-07	1943548-10
6.50	33608-05	33408-04	35318-09	24998-13	7810278-02	3236658-02	4394058-07	1956798-10
6.75	27198-05	29408-04	33248-09	21278-13	7835882-02	3480988-02	4563998-07	1970168-10
7.00	22468-05	26578-04	31298-09	24128-13	7835882-02	3739108-02	4729688-07	1983748-10
7.25	21078-05	23768-04	29478-09	23278-13	7848098-02	4010248-02	4891008-07	1997418-10
7.50	21308-05	21328-04	27778-09	22248-13	7848098-02	4244258-02	5040178-07	2010098-10
7.75	20318-05	19198-04	26168-09	22448-13	7872078-02	4480178-02	5200938-07	2023798-10
8.00	16978-05	17338-04	24668-09	21168-13	7881778-02	4739578-02	5349368-07	2035678-10
8.25	13498-05	15708-04	23248-09	19308-13	7881778-02	4980178-02	5493478-07	2046118-10
8.50	11908-05	14278-04	21918-09	16878-13	7881778-02	5232298-02	5633298-07	2054718-10
8.75	11948-05	13018-04	20668-09	13978-13	7898108-02	5480448-02	5768898-07	2065478-10
9.00	12778-05	11878-04	19488-09	10768-13	7915758-02	5739108-02	5900328-07	20765478-10
9.25	12208-05	10858-04	18378-09	74278-14	7923898-02	6027688-02	6027688-07	2084748-10
9.50	99458-06	99278-05	17348-09	41698-14	7930488-02	6270768-02	6151078-07	2093798-10
9.75	75208-06	90898-05	16378-09	11808-14	7930488-02	6527688-02	6270768-07	2103798-10
10.00	71998-06	83308-05	15468-09		7942188-02	6770768-02	6370628-07	2113798-10
10.25	79988-06	76468-05	14628-09		7942188-02	7027688-02	6469708-07	2123798-10
10.50	84758-06	70348-05	13838-09		7955708-02	7270768-02	6569708-07	2133798-10
10.75	74288-06	64908-05	13108-09		7955708-02	7527688-02	6669708-07	2143798-10
11.00	60168-06	60108-05	12428-09		7964602-02	7770768-02	6769708-07	2153798-10
11.25	45358-06	55978-05	11702-09		7964602-02	8027688-02	6869708-07	2163798-10
11.50	47438-06	52148-05	11202-09		7970358-02	8270768-02	6969708-07	2173798-10
11.75	58758-06	48078-05	10658-09		7970358-02	8527688-02	7069708-07	2183798-10
12.00	58528-06	45918-05	10148-09		7975118-02	8770768-02	7169708-07	2193798-10
12.25	49678-06	43228-05	96638-10		7975118-02	9027688-02	7269708-07	2203798-10
12.50	37558-06	40708-05	92168-10		7989982-02	9270768-02	7369708-07	2213798-10
12.75	28608-06	38328-05	87958-10		7989982-02	9527688-02	7469708-07	2223798-10
13.00	32108-06	36038-05	83978-10		7996338-02	9770768-02	7569708-07	2233798-10
13.25	41138-06	33728-05	80198-10		8000118-02	10027688-02	7669708-07	2243798-10
13.50	43098-06	31428-05	76598-10		8004548-02	10270768-02	7769708-07	2253798-10
13.75	33448-06	29738-05	73168-10		8008638-02	10527688-02	7869708-07	2263798-10
14.00	27578-06	27888-05	69808-10		8011678-02	10770768-02	7969708-07	2273798-10
14.25	20218-06	26198-05	66748-10		8014048-02	11027688-02	8069708-07	2283798-10
14.50	24898-06	24688-05	63758-10		8016598-02	11270768-02	8169708-07	2293798-10

Table 4-2. (Continued)

14.75	3254E-06	2336E-05	6069E-10	801990E-02	972738E-02	792073E-07	209221E-10
15.00	3274E-06	2221E-05	5817E-10	802371E-02	975399E-02	799027E-07	209380E-10
15.25	2248E-06	2121E-05	5540E-10	802690E-02	977077E-02	805783E-07	209377E-10
15.50	1467E-06	2033E-05	5316E-10	802922E-02	980464E-02	812348E-07	209223E-10
15.75	1522E-06	1952E-05	5047E-10	803106E-02	982928E-02	818731E-07	208938E-10
16.00	2312E-06	1876E-05	4872E-10	803339E-02	985315E-02	824938E-07	208551E-10
16.25	2445E-06	1801E-05	4671E-10	803647E-02	987644E-02	830980E-07	208101E-10
16.50	2465E-06	1724E-05	4483E-10	803975E-02	989910E-02	836866E-07	207628E-10
16.75	1445E-06	1645E-05	4309E-10	804243E-02	992110E-02	842651E-07	207177E-10
17.00	9915E-07	1565E-05	4146E-10	804417E-02	994237E-02	848207E-07	206707E-10
17.25	1343E-06	1484E-05	3993E-10	804580E-02	996237E-02	853680E-07	206493E-10
17.50	1896E-06	1405E-05	3851E-10	804783E-02	998257E-02	859031E-07	206323E-10
17.75	2163E-06	1330E-05	3716E-10	805045E-02	100015E-01	864268E-07	206209E-10
18.00	1709E-06	1263E-05	3589E-10	805335E-02	100197E-01	869195E-07	206403E-10
18.25	1097E-06	1203E-05	3467E-10	805641E-02	100372E-01	874178E-07	206654E-10
18.50	6701E-07	1151E-05	3350E-10	805968E-02	100542E-01	879355E-07	207024E-10
18.75	9523E-07	1112E-05	3236E-10	806308E-02	100708E-01	884328E-07	207469E-10
19.00	1558E-06	1078E-05	3126E-10	806665E-02	100870E-01	888666E-07	208013E-10
19.25	1744E-06	1055E-05	3018E-10	807021E-02	101031E-01	893482E-07	208558E-10
19.50	1278E-06	1027E-05	2912E-10	807402E-02	101189E-01	897994E-07	209068E-10
19.75	6266E-07	9940E-06	2809E-10	807803E-02	101345E-01	902403E-07	209558E-10
20.00	5370E-07	9652E-06	2708E-10	808227E-02	101498E-01	906780E-07	209941E-10
20.25	8741E-07	9308E-06	2610E-10	808673E-02	101647E-01	910911E-07	210209E-10
20.50	1394E-06	8969E-06	2515E-10	809145E-02	101794E-01	915011E-07	210347E-10
20.75	1453E-06	8518E-06	2423E-10	809636E-02	101935E-01	919010E-07	210347E-10
21.00	8538E-07	8111E-06	2336E-10	807198E-02	102072E-01	922911E-07	210215E-10
21.25	3954E-07	7766E-06	2253E-10	807490E-02	102203E-01	926718E-07	209965E-10
21.50	4650E-07	7338E-06	2176E-10	807562E-02	102330E-01	930436E-07	209621E-10
21.75	9394E-07	6908E-06	2103E-10	807682E-02	102452E-01	934069E-07	209214E-10
22.00	1248E-06	6740E-06	2035E-10	807870E-02	102570E-01	937423E-07	208779E-10
22.25	1166E-06	6531E-06	1972E-10	808079E-02	102685E-01	941105E-07	208354E-10
22.50	6454E-07	6374E-06	1914E-10	808240E-02	102799E-01	944520E-07	207974E-10
22.75	2637E-07	6191E-06	1860E-10	808322E-02	102910E-01	947873E-07	207671E-10
23.00	4442E-07	6139E-06	1810E-10	808386E-02	103021E-01	951170E-07	207472E-10
23.25	8985E-07	6043E-06	1763E-10	808508E-02	103132E-01	954144E-07	207392E-10
23.50	1102E-06	5897E-06	1717E-10	808692E-02	103241E-01	957608E-07	207440E-10
23.75	8251E-07	5701E-06	1674E-10	808871E-02	103350E-01	960755E-07	207613E-10
24.00	4315E-07	5610E-06	1632E-10	809088E-02	103456E-01	963854E-07	207898E-10
24.25	1617E-07	5436E-06	1590E-10	809344E-02	103561E-01	966905E-07	208276E-10
24.50	3610E-07	5171E-06	1548E-10	809695E-02	103663E-01	969908E-07	208716E-10
24.75	7085E-07	4932E-06	1506E-10	809704E-02	103760E-01	972860E-07	209188E-10
25.00	9382E-07	4738E-06	1463E-10	809735E-02	103855E-01	975760E-07	209653E-10
25.25	6024E-07	4588E-06	1421E-10	809527E-02	103946E-01	978603E-07	210042E-10
25.50	2007E-07	4288E-06	1378E-10	809607E-02	104033E-01	981374E-07	210444E-10
25.75	1172E-07	4135E-06	1336E-10	809638E-02	104118E-01	984125E-07	210708E-10
26.00	3874E-07	4031E-06	1294E-10	809689E-02	104201E-01	986978E-07	210860E-10
26.25	7166E-07	3965E-06	1253E-10	809707E-02	104283E-01	989417E-07	210860E-10
26.50	8038E-07	3877E-06	1214E-10	809771E-02	104364E-01	991966E-07	210798E-10
26.75	1456E-07	3890E-06	1177E-10	810100E-02	104445E-01	994467E-07	210598E-10
27.00	9858E-08	3855E-06	1142E-10	810154E-02	104527E-01	996914E-07	210304E-10
27.25	1504E-07	3796E-06	1109E-10	810181E-02	104609E-01	999312E-07	209947E-10
27.50	4936E-07	3751E-06	1079E-10	810250E-02	104690E-01	100166E-06	209547E-10
27.75	7232E-07	3657E-06	1052E-10	810382E-02	104770E-01	100390E-06	209148E-10
28.00	6804E-07	3558E-06	1027E-10	810536E-02	104849E-01	100625E-06	208778E-10
28.25	3139E-07	3384E-06	1004E-10	810648E-02	104926E-01	100849E-06	208469E-10
28.50	4927E-08	3227E-06	9832E-11	810690E-02	104999E-01	101071E-06	208246E-10
28.75	1770E-07	3106E-06	9639E-11	810716E-02	105071E-01	101290E-06	208127E-10
29.00	4485E-07	2922E-06	9409E-11	810787E-02	105139E-01	101507E-06	208164E-10
29.25	6737E-07	2803E-06	9307E-11	810915E-02	105204E-01	101722E-06	208352E-10
29.50	5471E-07	2711E-06	8994E-11	811054E-02	105268E-01	101934E-06	208666E-10

Table 4-2. (Continued)

29.75	.2052E-07	.2640E-06	.4917E-11	.011143E-02	.105330E-01	.102143E-06	.20013E-10
30.00	.1130E-08	.2628E-06	.8736E-11	.011169E-02	.105392E-01	.102350E-06	.209795E-10
30.25	.1623E-07	.2521E-06	.0530E-11	.011189E-02	.105454E-01	.102555E-06	.209711E-10
30.50	.4021E-07	.2588E-06	.0333E-11	.011266E-02	.105515E-01	.102756E-06	.210112E-10
30.75	.6188E-07	.2626E-06	.0142E-11	.011399E-02	.105578E-01	.102954E-06	.210499E-10
31.00	.4245E-07	.2594E-06	.7933E-11	.011525E-02	.105641E-01	.103149E-06	.210853E-10
31.25	.1087E-07	.2578E-06	.7682E-11	.011590E-02	.105705E-01	.103340E-06	.211089E-10
31.50	.6141E-09	.2527E-06	.7466E-11	.011694E-02	.105767E-01	.103527E-06	.211186E-10
31.75	.2162E-07	.2465E-06	.7286E-11	.011632E-02	.105829E-01	.103710E-06	.211217E-10
32.00	.5021E-07	.2374E-06	.7079E-11	.011722E-02	.105890E-01	.103890E-06	.211181E-10
32.25	.5517E-07	.2230E-06	.6852E-11	.011858E-02	.105948E-01	.104065E-06	.211009E-10
32.50	.3123E-07	.2148E-06	.6673E-11	.011985E-02	.106004E-01	.104237E-06	.210723E-10
32.75	.4172E-08	.2038E-06	.6508E-11	.012104E-02	.106057E-01	.104406E-06	.210385E-10
33.00	.2553E-08	.1928E-06	.6354E-11	.012019E-02	.106109E-01	.104572E-06	.210019E-10
33.25	.2713E-07	.1867E-06	.6212E-11	.012057E-02	.106158E-01	.104736E-06	.209445E-10
33.50	.5066E-07	.1827E-06	.6101E-11	.012159E-02	.106206E-01	.104897E-06	.209107E-10
33.75	.4760E-07	.1826E-06	.5997E-11	.012289E-02	.106254E-01	.105057E-06	.209042E-10
34.00	.2142E-07	.1804E-06	.5869E-11	.012381E-02	.106303E-01	.105215E-06	.208819E-10
34.25	.2403E-09	.1822E-06	.5781E-11	.012410E-02	.106351E-01	.105371E-06	.208651E-10
34.50	.6758E-08	.1868E-06	.5728E-11	.012418E-02	.106401E-01	.105526E-06	.208423E-10
34.75	.3217E-07	.1855E-06	.5649E-11	.012471E-02	.106452E-01	.105681E-06	.208239E-10
35.00	.4950E-07	.1855E-06	.5569E-11	.012583E-02	.106503E-01	.105834E-06	.208051E-10
35.25	.3959E-07	.1825E-06	.5464E-11	.012706E-02	.106553E-01	.105987E-06	.207921E-10
35.50		.1785E-06	.5381E-11	.012792E-02	.106603E-01	.106137E-06	.207828E-10
35.75		.1719E-06	.5289E-11	.012796E-02	.106652E-01	.106286E-06	.207692E-10
36.00		.1608E-06	.5184E-11	.012810E-02	.106699E-01	.106434E-06	.210272E-10
36.25		.1549E-06	.5084E-11	.012872E-02	.106744E-01	.106580E-06	.210647E-10
36.50		.1465E-06	.4971E-11	.012996E-02	.106787E-01	.106723E-06	.211000E-10
36.75		.1379E-06	.4852E-11	.013109E-02	.106828E-01	.106865E-06	.211296E-10
37.00		.1337E-06	.4699E-11	.013165E-02	.106867E-01	.107003E-06	.211473E-10
37.25		.1306E-06	.4574E-11	.013175E-02	.106906E-01	.107138E-06	.211515E-10
37.50		.1317E-06	.4476E-11	.013198E-02	.106944E-01	.107271E-06	.211495E-10
37.75		.1307E-06	.4356E-11	.013281E-02	.106983E-01	.107401E-06	.211414E-10
38.00		.1330E-06	.4223E-11	.013302E-02	.107022E-01	.107529E-06	.211215E-10
38.25		.1378E-06	.4123E-11	.013303E-02	.107063E-01	.107654E-06	.210921E-10
38.50		.1374E-06	.4036E-11	.013354E-02	.107104E-01	.107777E-06	.210594E-10
38.75		.1382E-06	.3952E-11	.013351E-02	.107146E-01	.107898E-06	.210249E-10
39.00		.1366E-06	.3879E-11	.013388E-02	.107188E-01	.108018E-06	.209899E-10
39.25		.1338E-06	.3822E-11	.013368E-02	.107230E-01	.108136E-06	.209598E-10
39.50		.1289E-06	.3786E-11	.013306E-02	.107270E-01	.108254E-06	.209379E-10
39.75		.1200E-06	.3718E-11	.013382E-02	.107309E-01	.108371E-06	.209204E-10
40.00		.1155E-06	.3681E-11	.0133930E-02	.107346E-01	.108486E-06	.209003E-10

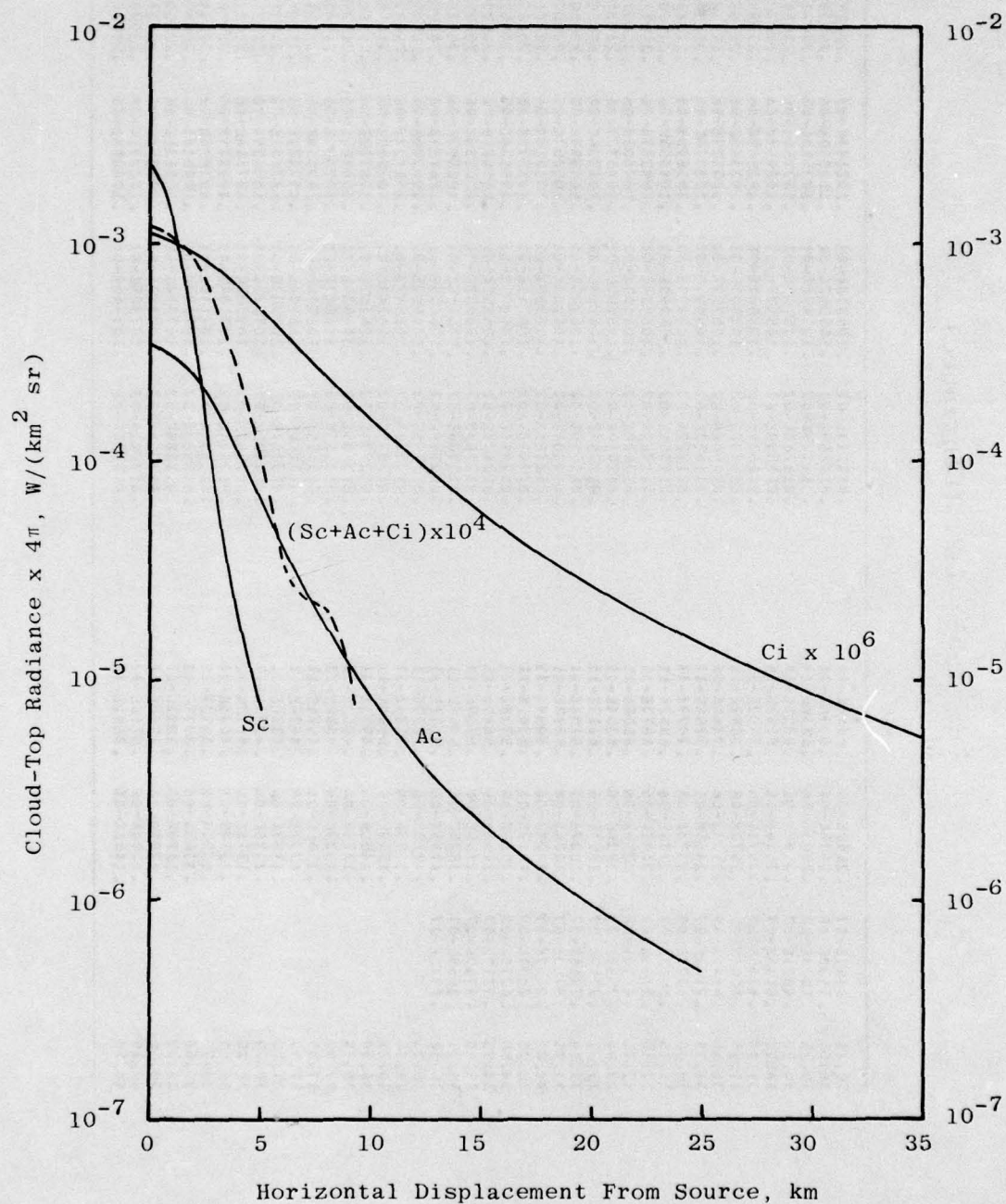


Figure 4-3. Output for sample Problems 1 to 4

where

T_i = transmittance of i th layer

R_i = reflectance of i th layer.

The total reflectance R for a planar slab is given by Equation (31b) of Appendix A as

$$R = T \cdot \frac{1}{2} \left(\frac{a}{Kb} - \frac{Kb}{a} \right) \sinh KL .$$

We can now compare our code results with the analytical results. This comparison is given in Table 4-3 where we give, as a function of the lateral displacement from the source, the ratio of the code-computed integrated-transmittance to the analytic integrated-transmittance. We see that for cloud Sc the code result is less than the analytic result by only 7%, 3%, and 2% at distances of 5, 10, and 15 km. For cloud Ac and cloud Ci the code results are small by 5% and 15% even at 40 km. For the three-layer configuration, the code result is small by only 15% at 5 km and 2% at 10 km.

We conclude that, whereas the comparisons between the code results and the analytic results for the integrated transmittance are not perfect for these examples, the comparison is of sufficiently high quality for the radial distances of importance that one can have a high confidence in the diffusion calculations performed in the statistical cloud submodel.

We return now to the input cards for Problems 1 to 4. We have two general choices for KMODEL which can be either (a) any value in the range from 1 to 10 or (b) a value of 11.

If KMODEL is less than 11, it doesn't matter, for Problems 1 to 4, which of the allowed values we choose. We can understand that fact by reviewing how the code operates for, say, Problem 1:

- (1) ROSCOER reads the detector, source, and wavelength cards.
- (2) Subroutine CLOUD0 reads the Type-1 and Type-2 cards and three Type-2d cards.
- (2.1) On the Type-2 card we set KCOVER and KLAYER to 0 since we have no need to override the stored data for either the CCOVER or CFREQ arrays; in fact, we really don't use the stored data for these arrays.

Table 4-3. Ratio of T(code)- to T(analytic)-results for sample Problems 1 to 4.

Distance (km)	Cloud Configuration			
	Sc	Ac	Ci	Sc + Ac + Ci
5	0.934	0.543	0.228	0.850
10	0.968	0.792	0.485	0.979
15	0.978	0.866	0.630	
20		0.901	0.714	
25		0.922	0.769	
30		0.936	0.806	
35		0.946	0.834	
40		0.953	0.855	

- (2.2) On the Type-2 card we set KTYPL, KTYPM, and KTYPH to 1 to allow the code to read in three Type-2d cards.
- (3) The three Type-2d cards specify that the only cloud configuration of interest is that for which the low-altitude layer has cloud Type-4 (Sc) and the mid- and high-altitude layers are clear.
- (4) ROSCOER calls subroutine SCLLOUD.
- (5) Subroutine SCLLOUD calls subroutine CLDWT.
- (6) Subroutine CLDWT's calculations are very much restricted compared with a normal run.
- (6.1) Consider Pass-1 through the DO-500 loop (II=2). In the DO-101 loop, the tests are satisfied only for LL=4. PIJKL is computed and IDX is set to 1. TRANS(1) and WT(160) are also computed (but never used). None of the loops after DO-101 becomes effective.
- (6.2) Consider Pass-2 through the DO-500 loop (II=3). Again, in DO-101 loop, tests are satisfied only for LL=4. PIJKL is computed and IDX is again set to 1. This time, computations of TRANS(1) and EMISS(1) are skipped because they were computed on Pass-1. The Pass-1 values of WT(1) and WT(160) are augmented with the Pass-2 values (but, again, will never be used).
- (6.3) Pass-3 and Pass-4 through DO-500 loop are just like Pass-2.
- (6.4) Subroutine CLDWT returns to subroutine SCLLOUD values for TRANS(1), EMISS(1), WT(1), and WT(2) = WT(160).
- (7.1) In subroutine SCLLOUD we exploit common PTE by arbitrarily setting T4 equal to TRANS(1), the modified transfer coefficient.

- (7.2) The code effectively returns to ROSCOER without doing any of the usual calculations or sorting in subroutine SCLLOUD.
- (8) ROSCOER then performs the radial integration over the cloud-top surface.

We now consider what would happen if we inputted 11 for KMODEL. First, we note that the code would expect to read a Type-2a card and four Type-2b cards. The natural selection of values for these cards would be as follows:

For Problems 1 to 4:

$$CCOVER(I,11) = \begin{cases} 0.0, & I=1,4 \\ 1.0, & I=5 \end{cases}$$

$$CFREQ(I,J,11) = 0.0 \quad (I=1,17), \quad J=1,3$$

and

	<u>Problem</u>
$CFREQ(I,4,11) = \left\{ \begin{array}{l} 1.0 \text{ } I=4 \text{ \& } 15 \\ 0.0 \text{ Otherwise} \end{array} \right\}$	1
$\left\{ \begin{array}{l} 1.0 \text{ } I=8 \text{ \& } 15 \\ 0.0 \text{ Otherwise} \end{array} \right\}$	2
$\left\{ \begin{array}{l} 1.0 \text{ } I=13 \text{ \& } 15 \\ 0.0 \text{ Otherwise} \end{array} \right\}$	3
$\left\{ \begin{array}{l} 1.0 \text{ } I=4,8,13 \text{ \& } 17 \\ 0.0 \text{ Otherwise} \end{array} \right\}$	4

However, it really wouldn't matter what is read in for CCOVER and CFREQ since we do not use them in Problems 1 to 4.

Subroutine CLDWT will return the complete arrays for TRANS and EMISS but the WT array will have zeros except that:

WT(4)≠0 and WT(160)≠0 for Problem 1
 WT(8)≠0 and WT(160)≠0 for Problem 2
 WT(13)≠0 and WT(160)≠0 for Problem 3
 WT(114)≠0 and WT(160)≠0 for Problem 4

Of course, we are interested in TRANS(IDX) for selected values of IDX: i.e., IDX = 4,8,13, and 114 for Problems 1,2,3, and 4, respectively. These members of the TRANS array can and should be intercepted in subroutine SCLOUD immediately after the return from subroutine SCLOUD immediately after the return from subroutine CLDWT. Failure to intercept at this point would allow the TRANS array to be sorted, with the loss of identity of the particular member of TRANS that is of interest.

4-3.2 Problem 5: Use of the statistical cloud submodel in the optional mode with KMODEL=11

The purpose of this problem is the illustrate (1) use of the statistical cloud submodel in the optional mode with KMODEL=11 and (2) a detailed printout of the complete results for a statistical cloud problem.

Use of the cloud model with KMODEL=11 requires the user to read in the Type-2a card for (CCOVER(I,11), I=1,5) and four Type-2b cards for (CFREQ(I,J,11), I=1,17; J=1,4), as seen from Figure 4-1. The input data deck is shown in Figure 4-4.

Selection of appropriate data for use with KMODEL=11, i.e., for the CCOVER and CFREQ arrays, is always the user's responsibility. For the authors' convenience, and for illustration, we have arbitrarily selected the data from that given for KMODEL=1, as can be seen by comparing with BLOCK DATA. (In this instance, because we have used data from KMODEL=1, we could get the same results more directly by not inputting 11 for KMODEL and the associated Type-2a and Type-2b cards but instead inputting 1 for KMODEL.)

Because we have inputted a 1 for the source-type flag ISUN, the code will first do the problem with the artificial source as specified and then do the problem with the sun as the source. The emission radiance will be calculated in each case.

The output results for the artificial source are shown in Tables 4-4a through 4-4d and those for the solar source are shown in Table 4-5a through 4-5c.

The quantities in the various columns in Tables 4-4a and 4-5a are described in Table 4-6. The results for IDX=1,159 are provided by subroutine CLDWT for the 159 different cloud configurations. The entries for TRANS=TCOEF with values of $\sim 10^{-51}$ occur when the argument of the sinh and cosh functions in the integral being evaluated

```

***** PROBLEM 5 *****
HD      THETAD    PHID    FUV      DETECTOR
35793.   90.00001  -90.0001  1.0
MSOURCE(1) THETAS(1) PHIS(1) WKT
0.01     90.000001 -90.00   1000.

ISUN
1
ALAM
2.50
MUDE
1
KMUDEL  KCOVER  KLAYR  KTYPL  KTYPH
11      0      0      0      0
I=1 I=2 I=3 I=4 I=5
.235.150.070.201.343

CCOVER(I,11) CARD 2A
CFREQ(I,1,11) CARD 2B
I=1 I=2 I=3 I=4 I=5 I=6 I=7 I=8 I=9 10 11 12 13 14 15 16 17
.046.046.046.102.006.005.001.217.005.005.005.005.222.293.768.212.019
CFREQ(I,2,11) CARD 2B
I=1 I=2 I=3 I=4 I=5 I=6 I=7 I=8 I=9 10 11 12 13 14 15 16 17
.055.055.055.121.006.008.001.243.009.008.008.009.164.260.542.377.081
CFREQ(I,3,11) CARD 2B
I=1 I=2 I=3 I=4 I=5 I=6 I=7 I=8 I=9 10 11 12 13 14 15 16 17
.038.038.038.169.015.010.000.276.012.010.010.012.104.266.415.435.150
CFREQ(I,4,11) CARD 2B
I=1 I=2 I=3 I=4 I=5 I=6 I=7 I=8 I=9 10 11 12 13 14 15 16 17
.010.010.010.336.155.010.030.197.023.010.010.023.017.158.448.423.128

```

Figure 4-4. Input data for Problem 5.

Table 4-4a. Initial arrays for artificial source transfer-coefficients, emission radiances, and weights in sample Problem 5. Wavelength = 2.5 μ m.

IDX	LL	MM	HH	TRANS	EMISS	CC=2	CC=3	CC=4	CC=5	WT	WT(SUM)
1	1	1	1	.3798E-01	.2553E+03	.6889E-03	.4799E-03	.1648E-02	.1414E-02	.4231E-02	.4231E-02
2	2	2	2	.6990E-08	.1473E+03	.6889E-03	.4799E-03	.1648E-02	.1414E-02	.4231E-02	.8462E-02
3	3	3	3	.1276E+00	.1208E+03	.6889E-03	.4799E-03	.1648E-02	.1414E-02	.4231E-02	.1239E-01
4	4	4	4	.4617E-01	.2227E+03	.1528E-02	.1056E-02	.7331E-02	.4750E-01	.5741E-01	.7011E-01
5	5	5	5	.1158E+00	.2529E+03	.8986E-04	.5236E-04	.6506E-03	.2719E-01	.2271E-01	.9281E-01
6	6	6	6	.3798E-01	.2553E+03	.7488E-04	.6981E-04	.4338E-03	.1414E-02	.1992E-02	.9480E-01
7	7	7	7	.4801E-02	.1473E+03	.1498E-04	.8726E-05	0.	.4241E-02	.4265E-02	.9907E-01
8	8	1	1	.6812E-02	.6389E+02	.3250E-02	.2120E-02	.1197E-01	.2785E-01	.4519E-01	.1443E+00
9	9	2	2	.4550E-05	.6389E+02	.7488E-04	.7854E-04	.5205E-03	.3252E-02	.3925E-02	.1482E+00
10	10	3	3	.6135E-37	.6389E+02	.7488E-04	.6981E-04	.4338E-03	.1414E-02	.1992E-02	.1502E+00
11	11	1	1	.1150E-06	.1126E+01	.7488E-04	.6981E-04	.4338E-03	.1414E-02	.1992E-02	.1522E+00
12	12	2	2	.4365E-51	.5296E+01	.7488E-04	.7854E-04	.5205E-03	.3252E-02	.3925E-02	.1561E+00
13	13	3	3	.2199E-07	.1073E+02	.3325E-02	.1431E-02	.4511E-02	.2403E-02	.1167E-01	.1678E+00
14	14	4	4	.1826E-23	.5296E+01	.4388E-02	.2269E-02	.1154E-01	.2234E-01	.4053E-01	.2083E+00
15	15	1	1	.6281E-02	.6389E+02	.1337E-03	.2491E-03	.1448E-02	.8958E-03	.2726E-02	.2110E+00
16	16	1	1	.5278E-05	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2112E+00
17	17	1	1	.4506E-37	.6389E+02	.1337E-03	.2491E-03	.1448E-02	.8958E-03	.2726E-02	.2112E+00
18	18	2	2	.9333E-10	.6389E+02	.1337E-03	.2491E-03	.1448E-02	.8958E-03	.2726E-02	.2112E+00
19	19	2	2	.7280E-51	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2112E+00
20	20	2	2	.1280E-51	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2112E+00
21	21	3	3	.1901E-02	.6389E+02	.1337E-03	.2491E-03	.1448E-02	.8958E-03	.2726E-02	.2112E+00
22	22	3	3	.3300E-06	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2112E+00
23	23	3	3	.3597E-38	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2112E+00
24	24	4	4	.2231E-03	.6389E+02	.6389E-05	.2030E-04	.2800E-03	.3010E-01	.3738E-01	.2547E+00
25	25	4	4	.1553E-06	.6389E+02	.6389E-05	.2030E-04	.2800E-03	.3010E-01	.3738E-01	.2547E+00
26	26	4	4	.7280E-51	.6389E+02	.6389E-05	.2030E-04	.2800E-03	.3010E-01	.3738E-01	.2547E+00
27	27	5	1	.9948E-04	.6389E+02	.1744E-04	.2717E-04	.5715E-03	.1528E-02	.1786E-02	.2603E+00
28	28	5	2	.8978E-07	.6389E+02	.4018E-06	.1006E-05	.2485E-04	.1621E-02	.1450E-01	.2748E+00
29	29	5	3	.7280E-51	.6389E+02	.4018E-06	.1006E-05	.2485E-04	.1621E-02	.1450E-01	.2748E+00
30	30	6	1	.6291E-02	.6389E+02	.1451E-04	.3623E-04	.3810E-03	.8958E-03	.1328E-02	.2772E+00
31	31	6	2	.5278E-05	.6389E+02	.3348E-06	.1342E-05	.1657E-04	.1046E-03	.1228E-03	.2787E+00
32	32	6	3	.4506E-37	.6389E+02	.3348E-06	.1342E-05	.1657E-04	.1046E-03	.1228E-03	.2787E+00
33	33	7	1	.6474E-04	.6389E+02	.2906E-05	.4529E-05	.1381E-04	.4547E-04	.6080E-04	.2814E+00
34	34	7	2	.3119E-07	.6389E+02	.6696E-07	.1677E-06	0.	.3137E-03	.2695E-02	.2817E+00
35	35	7	3	.7280E-51	.6389E+02	.6696E-07	.1677E-06	0.	.3137E-03	.2695E-02	.2817E+00
36	36	1	1	.4614E-06	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1366E-03	.2819E+00
37	37	1	2	.4365E-51	.5296E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1366E-03	.2819E+00
38	38	1	3	.6192E-07	.1073E+02	.1368E-03	.9226E-05	.5456E-03	.7730E-04	.1798E-03	.2822E+00
39	39	1	4	.7354E-23	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.9278E-03	.2831E+00
40	40	2	1	.3637E-51	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1366E-03	.2855E+00
41	41	2	2	.4365E-51	.5296E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1366E-03	.2855E+00
42	42	2	3	.4851E-51	.1073E+02	.1368E-03	.9226E-05	.5456E-03	.7730E-04	.1798E-03	.2855E+00
43	43	2	4	.4365E-51	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.9278E-03	.2855E+00
44	44	3	1	.1482E-06	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1366E-03	.2855E+00
45	45	3	2	.4365E-51	.5296E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1366E-03	.2855E+00
46	46	3	3	.1394E-07	.1073E+02	.1368E-03	.9226E-05	.5456E-03	.7730E-04	.1798E-03	.2906E+00
47	47	3	4	.1200E-23	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.9278E-03	.2932E+00
48	48	4	1	.1033E-07	.1126E+01	.6389E-05	.1804E-04	.2333E-03	.1528E-02	.1786E-02	.2950E+00
49	49	4	2	.4365E-51	.5296E+01	.6389E-05	.1804E-04	.2333E-03	.1528E-02	.1786E-02	.2950E+00
50	50	4	3	.1491E-08	.1073E+02	.3033E-03	.3699E-03	.2426E-02	.2597E-02	.5697E-02	.3045E+00
51	51	4	4	.4365E-51	.5296E+01	.4002E-03	.5864E-03	.6206E-02	.2414E-01	.3133E-01	.3358E+00
52	52	5	1	.5835E-08	.1126E+01	.4018E-06	.9946E-06	.2071E-04	.7048E-03	.7268E-03	.3366E+00
53	53	5	2	.4365E-51	.5296E+01	.4018E-06	.9946E-06	.2071E-04	.7048E-03	.7268E-03	.3366E+00
54	54	5	3	.8534E-09	.1073E+02	.1784E-04	.1834E-04	.2154E-03	.1119E-02	.1647E-02	.3382E+00
55	55	5	4	.4365E-51	.5296E+01	.2354E-04	.2908E-04	.2550E-03	.1114E-01	.1450E-02	.3397E+00
56	56	6	1	.4614E-06	.1126E+01	.3348E-06	.1193E-05	.1381E-04	.4547E-04	.6080E-04	.3515E+00
57	57	6	2	.4365E-51	.5296E+01	.3348E-06	.1193E-05	.1381E-04	.4547E-04	.6080E-04	.3515E+00
58	58	6	3	.6192E-07	.1073E+02	.1487E-04	.2445E-04	.1436E-03	.7730E-04	.2602E-03	.3518E+00
59	59	6	4	.7354E-23	.5296E+01	.1962E-04	.3877E-04	.3672E-03	.7184E-03	.1144E-02	.3510E+00

Table 4-4a. (Continued)

60	7	1	-3062E-08	-1126E+01	-6696E-07	-1491E-06	0.	-1364E-03	-3531E+00
61	7	2	-4355E-51	-5296E+01	-6696E-07	-1677E-06	0.	-3117E-03	-3514E+00
62	7	3	-2334E-09	-1073E+02	-2973E-05	-3057E-05	0.	-2319E-03	-3537E+00
63	7	4	-4365E-51	-5296E+01	-3924E-05	-4846E-05	0.	-2155E-02	-3558E+00
64	7	1	-7400E-08	-1126E+01	-1453E-04	-1623E-04	-3810E-03	-9958E-03	-3572E+00
65	6	1	-4365E-51	-5296E+01	-6452E-03	-7438E-03	-3963E-03	-2060E-02	-3597E+00
66	6	2	-8133E-09	-1073E+02	-6452E-03	-7438E-03	-3963E-03	-1523E-02	-3666E+00
67	6	3	-4365E-51	-5296E+01	-8515E-03	-1178E-02	-1014E-01	-1415E-01	-3929E+00
68	6	4	-3637E-51	-1126E+01	-3348E-06	-1342E-05	-1657E-04	-1046E-03	-3931E+00
69	2	1	-4355E-51	-5296E+01	-1487E-04	-1751E-04	-1938E-04	-1778E-03	-3937E+00
70	2	2	-4365E-51	-5296E+01	-1964E-06	-4361E-04	-4407E-03	-1652E-02	-3959E+00
71	2	3	-4365E-51	-5296E+01	-3348E-06	-1193E-05	-1381E-04	-4547E-04	-3960E+00
72	2	4	-4365E-51	-5296E+01	-3348E-06	-1342E-05	-1657E-04	-1046E-03	-3963E+00
73	3	1	-4851E-51	-1073E+02	-1487E-04	-2445E-04	-1436E-03	-7730E-03	-3974E+00
74	3	2	-4365E-51	-5296E+01	-1962E-04	-3877E-04	-3672E-03	-7184E-03	-3975E+00
75	3	3	-4365E-51	-5296E+01	-6157E-06	-4040E-05	-4570E-04	-2985E-04	-3977E+00
76	1	1	-4365E-51	-5296E+01	-6157E-06	-4545E-05	-5484E-04	-6819E-04	-3983E+00
77	1	2	-4365E-51	-5296E+01	-2734E-04	-8282E-04	-4753E-03	-5040E-04	-4001E+00
78	1	3	-4365E-51	-5296E+01	-3608E-04	-1313E-03	-1216E-02	-4684E-03	-4002E+00
79	1	4	-4365E-51	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-4002E+00
80	1	1	-4365E-51	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-4002E+00
81	1	2	-4365E-51	-5296E+01	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-4002E+00
82	1	3	-4365E-51	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-4003E+00
83	1	4	-4365E-51	-5296E+01	-1419E-07	-1330E-06	-1656E-05	-1505E-05	-4003E+00
84	1	1	-4365E-51	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-4003E+00
85	1	2	-4365E-51	-5296E+01	-6299E-06	-2727E-05	-1722E-04	-2559E-05	-4003E+00
86	1	3	-4365E-51	-5296E+01	-8314E-06	-4323E-05	-4405E-04	-7298E-04	-4004E+00
87	1	4	-4365E-51	-5296E+01	-1419E-07	-4040E-05	-4570E-04	-7961E-05	-4005E+00
88	2	1	-4365E-51	-5296E+01	-1419E-07	-4545E-05	-5484E-04	-6819E-04	-4006E+00
89	2	2	-4365E-51	-5296E+01	-1419E-07	-4863E-05	-5285E-04	-5469E-04	-4006E+00
90	2	3	-4365E-51	-5296E+01	-1419E-07	-4323E-05	-4405E-04	-7298E-04	-4006E+00
91	2	4	-4365E-51	-5296E+01	-1419E-07	-4040E-05	-4570E-04	-7961E-05	-4006E+00
92	2	1	-4365E-51	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-4011E+00
93	2	2	-4365E-51	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-4011E+00
94	2	3	-4365E-51	-5296E+01	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-4011E+00
95	2	4	-4365E-51	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-4011E+00
96	2	1	-4365E-51	-5296E+01	-1419E-07	-1330E-06	-1656E-05	-1505E-05	-4033E+00
97	2	2	-4365E-51	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-4033E+00
98	2	3	-4365E-51	-5296E+01	-6299E-06	-2727E-05	-1722E-04	-2559E-05	-4033E+00
99	2	4	-4365E-51	-5296E+01	-8314E-06	-4323E-05	-4405E-04	-7298E-04	-4033E+00
100	3	1	-2590E-08	-1126E+01	-6157E-06	-4040E-05	-4570E-04	-7961E-05	-4035E+00
101	3	2	-4365E-51	-5296E+01	-1419E-07	-4545E-05	-5484E-04	-6819E-04	-4035E+00
102	3	3	-2307E-09	-1073E+02	-2734E-04	-8282E-04	-4753E-03	-5040E-04	-4042E+00
103	3	4	-4365E-51	-5296E+01	-3608E-04	-1313E-03	-1216E-02	-4684E-03	-4061E+00
104	3	1	-3637E-51	-1126E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-4061E+00
105	3	2	-4365E-51	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-4061E+00
106	3	3	-4365E-51	-5296E+01	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-4061E+00
107	3	4	-4365E-51	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-4062E+00
108	3	1	-3637E-51	-1126E+01	-1419E-07	-1330E-06	-1656E-05	-1505E-05	-4062E+00
109	3	2	-4365E-51	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-4062E+00
110	3	3	-4365E-51	-5296E+01	-6299E-06	-2727E-05	-1722E-04	-2559E-05	-4062E+00
111	3	4	-4365E-51	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-4062E+00
112	4	1	-3637E-51	-1126E+01	-1419E-07	-1330E-06	-1656E-05	-1505E-05	-4075E+00
113	4	2	-4365E-51	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-4075E+00
114	4	3	-4365E-51	-5296E+01	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-4075E+00
115	4	4	-4365E-51	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-4075E+00
116	4	1	-3637E-51	-1126E+01	-1419E-07	-1330E-06	-1656E-05	-1505E-05	-4358E+00
117	4	2	-4365E-51	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-4358E+00
118	4	3	-4365E-51	-5296E+01	-6299E-06	-2727E-05	-1722E-04	-2559E-05	-4361E+00
119	4	4	-4365E-51	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-4361E+00
									-4364E+00
									-4384E+00

Table 4-4a. (Continued)

120	4	3	1	126E+01	3146E-07	2926E-06	7364E-05	5057E-04	5826E-04	4385E+00
121	4	3	2	5296E+01	3146E-07	3292E-06	8337E-05	1163E-03	1255E-03	4386E+00
122	4	3	3	1073E+02	1397E-05	5999E-05	7659E-04	5977E-04	1699E-03	4388E+00
123	4	3	4	5296E+01	1843E-05	9510E-05	1359E-03	7990E-03	1006E-02	4398E+00
124	5	1	1	1126E+01	8031E-07	4407E-06	1804E-04	4596E-03	4781E-03	4403E+00
125	5	1	2	5296E+01	8031E-07	4958E-06	2165E-04	1057E-02	1079E-02	4414E+00
126	5	1	3	1073E+02	3566E-05	9035E-05	1876E-03	7812E-03	9815E-03	4423E+00
127	5	1	4	5296E+01	4706E-05	1432E-04	4799E-03	7261E-02	7760E-02	4501E+00
128	5	2	1	1126E+01	1851E-08	1632E-07	7844E-06	5365E-04	5446E-04	4502E+00
129	5	2	2	5296E+01	1851E-08	1836E-07	9412E-06	1234E-03	1244E-03	4503E+00
130	5	2	3	1073E+02	8216E-07	3346E-06	8157E-05	9121E-04	9978E-04	4504E+00
131	5	2	4	5296E+01	1084E-06	5305E-06	2086E-04	8477E-03	8692E-03	4512E+00
132	5	3	1	1126E+01	1851E-08	1451E-07	6336E-06	2333E-04	2400E-04	4513E+00
133	5	3	2	5296E+01	1851E-08	1632E-07	7844E-06	5365E-04	5446E-04	4513E+00
134	5	3	3	1073E+02	8216E-07	2975E-06	6798E-05	3966E-04	4683E-04	4514E+00
135	5	3	4	5296E+01	1084E-06	4716E-06	1739E-04	3686E-03	3865E-03	4518E+00
136	6	1	1	7693E-08	6693E-07	5876E-06	1203E-04	7965E-04	4233E-04	4518E+00
137	6	1	2	5296E+01	6693E-07	6611E-06	1443E-04	5819E-04	8335E-04	4519E+00
138	6	1	3	1073E+02	2972E-05	1205E-04	1251E-03	5040E-04	1905E-03	4521E+00
139	6	1	4	5296E+01	3922E-05	1910E-04	3199E-03	4684E-03	8114E-03	4529E+00
140	6	2	1	1126E+01	1542E-08	2176E-07	5229E-06	3462E-05	4008E-05	4529E+00
141	6	2	2	5296E+01	1542E-08	2449E-07	6755E-06	7961E-05	8615E-05	4529E+00
142	6	2	3	1339E-12	6847E-07	4462E-06	5438E-05	5885E-05	1184E-04	4529E+00
143	6	2	4	5296E+01	9037E-07	7074E-06	1391E-04	5469E-04	5940E-04	4530E+00
144	6	3	1	1126E+01	1542E-08	1935E-07	4358E-06	1505E-05	1962E-05	4530E+00
145	6	3	2	5296E+01	1542E-08	2176E-07	5229E-06	3462E-05	4008E-05	4530E+00
146	6	3	3	1073E+02	6847E-07	3966E-06	4532E-05	2559E-05	7555E-05	4530E+00
147	6	3	4	5296E+01	9037E-07	6288E-06	1159E-04	2378E-04	3609E-04	4530E+00
148	7	1	1	1126E+01	1339E-07	7346E-07	0.	8695E-04	8903E-04	4531E+00
149	7	1	2	5296E+01	1339E-07	8264E-07	0.	2046E-03	2047E-03	4533E+00
150	7	1	3	1073E+02	5943E-06	1506E-05	0.	1512E-03	1533E-03	4535E+00
151	7	1	4	5296E+01	7844E-06	2387E-05	0.	1405E-02	1409E-02	4549E+00
152	7	2	1	1126E+01	3084E-09	2721E-08	0.	1038E-04	1039E-04	4549E+00
153	7	2	2	5296E+01	3084E-09	3061E-08	0.	2389E-04	2389E-04	4549E+00
154	7	2	3	1073E+02	1369E-07	5577E-07	0.	1765E-04	1772E-04	4549E+00
155	7	2	4	5296E+01	1807E-07	8842E-07	0.	1641E-03	1642E-03	4551E+00
156	7	3	1	1126E+01	3084E-09	2418E-08	0.	4515E-05	4518E-05	4551E+00
157	7	3	2	5296E+01	3084E-09	2721E-08	0.	1038E-04	1039E-04	4551E+00
158	7	3	3	1073E+02	1369E-07	4958E-07	0.	7676E-05	7739E-05	4551E+00
159	7	3	4	5296E+01	1807E-07	7860E-07	0.	7134E-04	7143E-04	4552E+00
160	*****	*****	*****	0.	0.	0.	-R	-R	-R	5399E+00
WT (160) =										
EMISS(160) =										
TRANS(160) =										
IDX = 160										
.1816E+01										
.3275E+03										

Table 4-4b. Sorted array for artificial source transfer-coefficients
(and carried-along weights) for sample Problem 5.

TRANS, WT =	0.	0.	.3637E-51	.5612E-05	.3637E-51	.8001E-04	.3637E-51	.3308E-05
.3637E-51	.1092E-03	.3637E-51	.3308E-05	.3637E-51	.6080E-04	.3637E-51	.3308E-05	
.3637E-51	.5612E-05	.3637E-51	.2400E-04	.3637E-51	.4518E-05	.3637E-51	.4781E-03	
.3637E-51	.5446E-04	.3637E-51	.1228E-03	.3637E-51	.1039E-04	.3637E-51	.1962E-05	
.3637E-51	.8903E-04	.3637E-51	.5826E-04	.3637E-51	.1255E-03	.3637E-51	.1210E-02	
.4365E-51	.5612E-05	.4365E-51	.1132E-03	.4365E-51	.1851E-02	.4365E-51	.1282E-03	
.4365E-51	.1053E-04	.4365E-51	.1282E-03	.4365E-51	.7298E-04	.4365E-51	.1137E-03	
.4365E-51	.7298E-04	.4365E-51	.1144E-02	.4365E-51	.7298E-04	.4365E-51	.5612E-05	
.4365E-51	.1053E-04	.4365E-51	.5612E-05	.4365E-51	.1798E-03	.4365E-51	.1798E-03	
.4365E-51	.1132E-03	.4365E-51	.1851E-02	.4365E-51	.1851E-02	.4365E-51	.3865E-03	
.4365E-51	.8692E-03	.4365E-51	.1798E-03	.4365E-51	.1228E-03	.4365E-51	.1244E-03	
.4365E-51	.2573E-02	.4365E-51	.3140E-03	.4365E-51	.7760E-02	.4365E-51	.2561E-02	
.4365E-51	.8114E-03	.4365E-51	.1642E-03	.4365E-51	.2150E-02	.4365E-51	.3925E-02	
.4365E-51	.5446E-04	.4365E-51	.2623E-03	.4365E-51	.1079E-02	.4365E-51	.1053E-04	
.4365E-51	.1228E-03	.4365E-51	.2164E-02	.4365E-51	.7143E-04	.4365E-51	.4008E-05	
.4365E-51	.1409E-02	.4365E-51	.2632E-01	.4365E-51	.2389E-04	.4365E-51	.2047E-03	
.4365E-51	.1282E-03	.4365E-51	.8615E-05	.4365E-51	.8335E-04	.4365E-51	.6940E-04	
.4365E-51	.3609E-04	.4365E-51	.1039E-04	.4365E-51	.1174E-01	.4365E-51	.2085E-02	
.4365E-51	.3133E-01	.4365E-51	.2152E-01	.4365E-51	.1647E-02	.4365E-51	.3821E-02	
.4365E-51	.2547E-02	.4365E-51	.1255E-03	.4365E-51	.2785E-03	.4365E-51	.1006E-02	
.4851E-51	.6359E-03	.4851E-51	.2314E-04	.4851E-51	.3025E-04	.4851E-51	.4050E-02	
.4851E-51	.2314E-04	.4851E-51	.3025E-04	.4851E-51	.9978E-04	.4851E-51	.2314E-04	
.4851E-51	.4683E-04	.4851E-51	.3925E-03	.4851E-51	.9815E-03	.4851E-51	.9278E-03	
.4851E-51	.2978E-03	.4851E-51	.2602E-03	.4851E-51	.1533E-03	.4851E-51	.7555E-05	
.4851E-51	.1699E-03	.4851E-51	.7739E-05	.4851E-51	.1772E-04	.7280E-51	.1092E-03	
.7280E-51	.1786E-02	.7280E-51	.1798E-03	.7280E-51	.1366E-03	.7280E-51	.7268E-03	
.3597E-38	.1092E-03	.4506E-37	.6080E-04	.4506E-37	.1092E-03	.6135E-37	.1992E-02	
.1200E-23	.2561E-02	.1326E-23	.4053E-01	.7354E-23	.1144E-02	.7354E-23	.2561E-02	
.1339E-12	.1184E-04	.1339E-12	.3025E-04	.3705E-11	.4008E-05	.3705E-11	.5612E-05	
.8333E-10	.2726E-02	.2307E-09	.6359E-03	.3234E-09	.2379E-03	.7393E-09	.1905E-03	
.7393E-09	.6359E-03	.8132E-09	.6873E-02	.8534E-09	.1450E-02	.1491E-08	.5697E-02	
.2590E-08	.8001E-04	.3062E-08	.1366E-03	.5835E-08	.7268E-03	.7693E-08	.8001E-04	
.7693E-08	.4233E-04	.8740E-08	.1328E-02	.8990E-08	.4231E-02	.1083E-07	.1786E-02	
.1384E-07	.9278E-03	.2199E-07	.1167E-01	.3119E-07	.3140E-03	.6192E-07	.9278E-03	
.6192E-07	.2602E-03	.8970E-07	.1647E-02	.1160E-06	.1992E-02	.1482E-06	.1092E-03	
.1553E-06	.3821E-02	.4514E-06	.6080E-04	.4614E-06	.1092E-03	.8300E-06	.1798E-03	
.4550E-05	.3925E-02	.5278E-05	.1798E-03	.5278E-05	.1228E-03	.6474E-04	.2695E-02	
.9948E-04	.1450E-01	.2231E-03	.3738E-01	.1901E-02	.2726E-02	.4801E-02	.4265E-02	
.6281E-02	.2726E-02	.6281E-02	.1328E-02	.6812E-02	.4519E-01	.4617E-01	.5741E-01	
.1158E+00	.2271E-01	.1276E+00	.4231E-02	.1816E+01	.5399E+00	.3798E+01	.1992E-02	
.3798E+01	.4231E-02							

Table 4-4c. Sorted array for emission radiances (and carried-along weights) for sample Problem 5.

EMISS,WT1 =									
0.	0.	.1126E+01	.5612E-05	.1126E+01	.8001E-04	.1126E+01	.3308E-05	.1126E+01	.3308E-05
.1126E+01	.8001E-04	.1126E+01	.3308E-05	.1126E+01	.1210E-02	.1126E+01	.3308E-05	.1126E+01	.3308E-05
.1126E+01	.5612E-05	.1126E+01	.1092E-03	.1126E+01	.1992E-02	.1126E+01	.7268E-03	.1126E+01	.7268E-03
.1126E+01	.1786E-02	.1126E+01	.1092E-03	.1126E+01	.1366E-03	.1126E+01	.1092E-03	.1126E+01	.1092E-03
.1126E+01	.6080E-04	.1126E+01	.1228E-03	.1126E+01	.1328E-02	.1126E+01	.5612E-05	.1126E+01	.5612E-05
.1126E+01	.6080E-04	.1126E+01	.2400E-04	.1126E+01	.5446E-04	.1126E+01	.4781E-03	.1126E+01	.4781E-03
.1126E+01	.4008E-05	.1126E+01	.8001E-04	.1126E+01	.1039E-04	.1126E+01	.8903E-04	.1126E+01	.8903E-04
.1126E+01	.1962E-05	.1126E+01	.5826E-04	.1126E+01	.4233E-04	.1126E+01	.1255E-03	.1126E+01	.1255E-03
.1126E+01	.4518E-05	.5296E+01	.7298E-04	.5296E+01	.1132E-03	.5296E+01	.1282E-03	.5296E+01	.1282E-03
.5296E+01	.5612E-05	.5296E+01	.1053E-04	.5296E+01	.5612E-05	.5296E+01	.1132E-03	.5296E+01	.1132E-03
.5296E+01	.7298E-04	.5296E+01	.1132E-03	.5296E+01	.1851E-02	.5296E+01	.5612E-05	.5296E+01	.5612E-05
.5296E+01	.1053E-04	.5296E+01	.1282E-03	.5296E+01	.1798E-03	.5296E+01	.2547E-02	.5296E+01	.2547E-02
.5296E+01	.2561E-02	.5296E+01	.2152E-01	.5296E+01	.7298E-04	.5296E+01	.2561E-02	.5296E+01	.2561E-02
.5296E+01	.2561E-02	.5296E+01	.3821E-02	.5296E+01	.1798E-03	.5296E+01	.1798E-03	.5296E+01	.1798E-03
.5296E+01	.1228E-03	.5296E+01	.1647E-02	.5296E+01	.1144E-02	.5296E+01	.1174E-01	.5296E+01	.1174E-01
.5296E+01	.3133E-01	.5296E+01	.3925E-02	.5296E+01	.2164E-02	.5296E+01	.4053E-01	.5296E+01	.4053E-01
.5296E+01	.2573E-02	.5296E+01	.3140E-03	.5296E+01	.2632E-01	.5296E+01	.1228E-03	.5296E+01	.1228E-03
.5296E+01	.2623E-03	.5296E+01	.1144E-02	.5296E+01	.2156E-02	.5296E+01	.1282E-03	.5296E+01	.1282E-03
.5296E+01	.1006E-02	.5296E+01	.1851E-02	.5296E+01	.1079E-02	.5296E+01	.1053E-04	.5296E+01	.1053E-04
.5296E+01	.7760E-02	.5296E+01	.5446E-04	.5296E+01	.1244E-03	.5296E+01	.3865E-03	.5296E+01	.3865E-03
.5296E+01	.1851E-02	.5296E+01	.8335E-04	.5296E+01	.6940E-04	.5296E+01	.8114E-03	.5296E+01	.8114E-03
.5296E+01	.4003E-05	.5296E+01	.8615E-05	.5296E+01	.3609E-04	.5296E+01	.2389E-04	.5296E+01	.2389E-04
.5296E+01	.2047E-03	.5296E+01	.1642E-03	.5296E+01	.1409E-02	.5296E+01	.2785E-03	.5296E+01	.2785E-03
.5296E+01	.1039E-04	.5296E+01	.2085E-02	.5296E+01	.7143E-04	.5296E+01	.1255E-03	.5296E+01	.1255E-03
.5296E+01	.8692E-03	.1073E+02	.9278E-03	.1073E+02	.2314E-04	.1073E+02	.2314E-04	.1073E+02	.2314E-04
.1073E+02	.6359E-03	.1073E+02	.3025E-04	.1073E+02	.2602E-03	.1073E+02	.4050E-02	.1073E+02	.4050E-02
.1073E+02	.5697E-02	.1073E+02	.2314E-04	.1073E+02	.6359E-03	.1073E+02	.6359E-03	.1073E+02	.6359E-03
.1073E+02	.1450E-02	.1073E+02	.3925E-03	.1073E+02	.3025E-04	.1073E+02	.9278E-03	.1073E+02	.9278E-03
.1073E+02	.1905E-03	.1073E+02	.2602E-03	.1073E+02	.9978E-04	.1073E+02	.9278E-03	.1073E+02	.9278E-03
.1073E+02	.2379E-03	.1073E+02	.2978E-03	.1073E+02	.3025E-04	.1073E+02	.1533E-03	.1073E+02	.1533E-03
.1073E+02	.6873E-02	.1073E+02	.1699E-03	.1073E+02	.1167E-01	.1073E+02	.1772E-04	.1073E+02	.1772E-04
.1073E+02	.1184E-04	.1073E+02	.9815E-03	.1073E+02	.4683E-04	.1073E+02	.7739E-05	.1073E+02	.7739E-05
.1073E+02	.7555E-05	.6389E+02	.1992E-02	.6389E+02	.3821E-02	.6389E+02	.1798E-03	.6389E+02	.1798E-03
.6389E+02	.1092E-03	.6389E+02	.3738E-01	.6389E+02	.2726E-02	.6389E+02	.1786E-02	.6389E+02	.1786E-02
.6389E+02	.1450E-01	.6389E+02	.4519E-01	.6389E+02	.3925E-02	.6389E+02	.1092E-03	.6389E+02	.1092E-03
.6389E+02	.2726E-02	.6389E+02	.6080E-04	.6389E+02	.2695E-02	.6389E+02	.3140E-03	.6389E+02	.3140E-03
.6389E+02	.1366E-03	.6389E+02	.1798E-03	.6389E+02	.1092E-03	.6389E+02	.1647E-02	.6389E+02	.1647E-02
.6389E+02	.7268E-03	.6389E+02	.1328E-02	.6389E+02	.1228E-03	.6389E+02	.1798E-03	.6389E+02	.1798E-03
.6389E+02	.2726E-02	.1208E+03	.4231E-02	.1473E+03	.4265E-02	.1473E+03	.4231E-02	.1473E+03	.4231E-02
.2227E+03	.5741E-01	.2529E+03	.2271E-01	.2553E+03	.1992E-02	.2553E+03	.4231E-02	.2553E+03	.4231E-02
.3275E+03	.5435E+00								

Table 4-4d. Cumulative, normalized weight arrays for artificial source transfer-coefficients and emission radiances in sample Problem 5.

WT,WT1 =								
0.	0.	.5640E-05	.5620E-05	.8604E-04	.8573E-04	.8936E-04	.8904E-04	
.1991E-03	.1691E-03	.2024E-03	.1725E-03	.2635E-03	.1384E-02	.2669E-03	.1387E-02	
.2725E-03	.1393E-02	.2966E-03	.1502E-02	.3012E-03	.3497E-02	.7816E-03	.4224E-02	
.8364E-03	.6013E-02	.9598E-03	.6122E-02	.9702E-03	.6259E-02	.9722E-03	.6368E-02	
.1062E-02	.6429E-02	.1120E-02	.6552E-02	.1246E-02	.7881E-02	.2462E-02	.7887E-02	
.2468E-02	.7948E-02	.2581E-02	.7972E-02	.4442E-02	.8026E-02	.4571E-02	.8505E-02	
.4581E-02	.8509E-02	.4710E-02	.8589E-02	.4784E-02	.8600E-02	.4897E-02	.8689E-02	
.4971E-02	.8691E-02	.6120E-02	.8749E-02	.6194E-02	.8791E-02	.6199E-02	.8917E-02	
.6210E-02	.8922E-02	.6216E-02	.8995E-02	.6396E-02	.9108E-02	.6577E-02	.9236E-02	
.6691E-02	.9242E-02	.8551E-02	.9253E-02	.1041E-01	.9258E-02	.1080E-01	.9372E-02	
.1167E-01	.9445E-02	.1185E-01	.9558E-02	.1198E-01	.1141E-01	.1210E-01	.1142E-01	
.1469E-01	.1143E-01	.1500E-01	.1156E-01	.2280E-01	.1174E-01	.2538E-01	.1429E-01	
.2619E-01	.1685E-01	.2636E-01	.3839E-01	.2852E-01	.3847E-01	.3247E-01	.4103E-01	
.3252E-01	.4359E-01	.3279E-01	.4742E-01	.3387E-01	.4760E-01	.3388E-01	.4778E-01	
.3400E-01	.4790E-01	.3618E-01	.4955E-01	.3625E-01	.5070E-01	.3626E-01	.6245E-01	
.3767E-01	.9382E-01	.6412E-01	.9776E-01	.6414E-01	.9992E-01	.6435E-01	.1405E+00	
.6448E-01	.1431E+00	.6449E-01	.1434E+00	.6457E-01	.1697E+00	.6464E-01	.1699E+00	
.6467E-01	.1701E+00	.6469E-01	.1713E+00	.7648E-01	.1734E+00	.7858E-01	.1736E+00	
.1101E+00	.1746E+00	.1317E+00	.1764E+00	.1333E+00	.1775E+00	.1372E+00	.1775E+00	
.1397E+00	.1853E+00	.1399E+00	.1853E+00	.1401E+00	.1855E+00	.1412E+00	.1859E+00	
.1418E+00	.1877E+00	.1419E+00	.1878E+00	.1418E+00	.1879E+00	.1459E+00	.1887E+00	
.1459E+00	.1887E+00	.1460E+00	.1887E+00	.1461E+00	.1887E+00	.1461E+00	.1887E+00	
.1461E+00	.1890E+00	.1465E+00	.1891E+00	.1475E+00	.1905E+00	.1485E+00	.1908E+00	
.1488E+00	.1908E+00	.1490E+00	.1929E+00	.1492E+00	.1930E+00	.1492E+00	.1931E+00	
.1493E+00	.1940E+00	.1494E+00	.1949E+00	.1494E+00	.1949E+00	.1495E+00	.1949E+00	
.1513E+00	.1956E+00	.1515E+00	.1956E+00	.1516E+00	.1959E+00	.1523E+00	.1999E+00	
.1524E+00	.2056E+00	.1525E+00	.2057E+00	.1526E+00	.2063E+00	.1546E+00	.2069E+00	
.1572E+00	.2084E+00	.1979E+00	.2088E+00	.1991E+00	.2088E+00	.2016E+00	.2097E+00	
.2017E+00	.2099E+00	.2017E+00	.2102E+00	.2017E+00	.2103E+00	.2017E+00	.2112E+00	
.2044E+00	.2115E+00	.2051E+00	.2117E+00	.2053E+00	.2118E+00	.2055E+00	.2119E+00	
.2061E+00	.2188E+00	.2130E+00	.2190E+00	.2145E+00	.2307E+00	.2202E+00	.2307E+00	
.2203E+00	.2307E+00	.2204E+00	.2317E+00	.2212E+00	.2317E+00	.2213E+00	.2317E+00	
.2213E+00	.2317E+00	.2226E+00	.2337E+00	.2269E+00	.2376E+00	.2287E+00	.2377E+00	
.2296E+00	.2379E+00	.2413E+00	.2753E+00	.2417E+00	.2780E+00	.2426E+00	.2798E+00	
.2428E+00	.2943E+00	.2445E+00	.3396E+00	.2465E+00	.3435E+00	.2466E+00	.3436E+00	
.2505E+00	.3463E+00	.2505E+00	.3464E+00	.2506E+00	.3491E+00	.2508E+00	.3494E+00	
.2548E+00	.3495E+00	.2549E+00	.3497E+00	.2551E+00	.3498E+00	.2578E+00	.3515E+00	
.2723E+00	.3522E+00	.3099E+00	.3535E+00	.3126E+00	.3537E+00	.3169E+00	.3539E+00	
.3197E+00	.3566E+00	.3210E+00	.3608E+00	.3664E+00	.3651E+00	.4241E+00	.3693E+00	
.4469E+00	.4268E+00	.4512E+00	.4495E+00	.9937E+00	.4515E+00	.9957E+00	.4558E+00	
.1000E+01	.1000E+01							
STATISTICAL CLOUDS, P1,P2,P3,P4 =		.10		.25		.50		.90
SOURCE TRANSFER CF T1,T2,T3,T4 =		.437E-51		.154E-06		.280E+00		.152E+01
EMISSION E1,E2,E3,E4 =		.530E+01		.639E+02		.261E+03		.314E+03

Table 4-5a. Initial arrays for solar source transfer-coefficients, emission radiances, and weights in sample Problem 5. Wavelength = 2.5 μm .

IDX	LL	MM	HH	TRANS	EMISS	CC-2	CC-3	CC-4	CC-5	WT	WT(SUM)
1	1			.1897E-02	.2553E+03	.6889E-03	.4799E-03	.1648E-02	.1414E-02	.4231E-02	.4231E-02
2	2			.2714E-01	.1473E+03	.6889E-03	.4799E-03	.1648E-02	.1414E-02	.4231E-02	.8462E-02
3	3			.3171E-01	.1208E+03	.6889E-03	.4799E-03	.1648E-02	.1414E-02	.4231E-02	.1269E-01
4	4			.1048E-01	.2227E+03	.1528E-02	.1056E-02	.7331E-02	.4750E-01	.5741E-01	.7011E-01
5	5			.4338E-02	.2529E+03	.8986E-04	.5236E-04	.0506E-03	.2191E-01	.2271E-01	.9281E-01
6	6			.1887E-02	.2553E+03	.7488E-04	.6991E-04	.4338E-03	.1414E-02	.1992E-02	.9480E-01
7	7			.2714E-01	.1473E+03	.7488E-04	.8726E-05	.0	.4241E-02	.4265E-02	.9907E-01
8	8	1		.5061E-01	.6389E+02	.3250E-02	.2120E-02	.1197E-01	.2795E-01	.4519E-01	.1443E+00
9	9	2		.5061E-01	.6389E+02	.7488E-04	.7854E-04	.5205E-03	.3252E-02	.3925E-02	.1482E+00
10	10	3		.5061E-01	.6389E+02	.7488E-04	.6981E-04	.4338E-03	.1414E-02	.1992E-02	.1502E+00
11	11		1	.8408E-01	.1126E+01	.7488E-04	.6981E-04	.4338E-03	.1414E-02	.1992E-02	.1502E+00
12	12	2		.7621E-01	.5296E+01	.3325E-02	.7854E-04	.5205E-03	.3252E-02	.3925E-02	.1522E+00
13	13	3		.7255E-01	.1073E+02	.1337E-02	.1431E-02	.4511E-02	.2403E-02	.1167E-01	.1678E+00
14	14	4		.7621E-01	.5296E+01	.1337E-02	.2269E-02	.1154E-01	.2234E-01	.4053E-01	.2083E+00
15	15	1	1	.5061E-01	.6389E+02	.1337E-02	.2491E-03	.1448E-02	.8958E-03	.1798E-03	.2110E+00
16	16	1	2	.5061E-01	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2112E+00
17	17	1	3	.5061E-01	.6389E+02	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.2113E+00
18	18	2	1	.5061E-01	.6389E+02	.1337E-03	.2491E-03	.1448E-02	.8958E-03	.1798E-03	.2140E+00
19	19	2	2	.5061E-01	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2142E+00
20	20	2	3	.5061E-01	.6389E+02	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.2143E+00
21	21	3	1	.5061E-01	.6389E+02	.1337E-03	.2491E-03	.1448E-02	.8958E-03	.1798E-03	.2171E+00
22	22	3	2	.5061E-01	.6389E+02	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2172E+00
23	23	3	3	.5061E-01	.6389E+02	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.2173E+00
24	24	4	1	.5061E-01	.6389E+02	.2964E-03	.5480E-03	.2406E-02	.3010E-01	.3738E-01	.2347E+00
25	25	4	2	.5061E-01	.6389E+02	.6830E-05	.2030E-04	.2800E-03	.3514E-02	.3821E-02	.2585E+00
26	26	4	3	.5061E-01	.6389E+02	.6830E-05	.1804E-04	.2333E-03	.1388E-01	.1450E-01	.2748E+00
27	27	5	1	.5061E-01	.6389E+02	.1744E-04	.2717E-04	.5715E-03	.1388E-01	.1450E-01	.2748E+00
28	28	5	2	.5061E-01	.6389E+02	.4018E-06	.1006E-05	.2485E-04	.1621E-02	.1647E-02	.2765E+00
29	29	5	3	.5061E-01	.6389E+02	.4018E-06	.8946E-06	.2071E-04	.7048E-03	.7268E-03	.2772E+00
30	30	6	1	.5061E-01	.6389E+02	.1453E-04	.3623E-04	.3810E-03	.8958E-03	.1328E-02	.2785E+00
31	31	6	2	.5061E-01	.6389E+02	.3348E-06	.1342E-05	.1657E-04	.1046E-03	.1228E-03	.2787E+00
32	32	6	3	.5061E-01	.6389E+02	.2906E-05	.1193E-05	.1381E-04	.4547E-04	.6080E-04	.2814E+00
33	33	7	1	.5061E-01	.6389E+02	.6696E-07	.1677E-06	0.	.3137E-03	.3140E-03	.2817E+00
34	34	7	2	.5061E-01	.6389E+02	.6696E-07	.1491E-06	0.	.3137E-03	.3140E-03	.2819E+00
35	35	7	3	.5061E-01	.6389E+02	.6696E-07	.1491E-06	0.	.3137E-03	.3140E-03	.2819E+00
36	36	1	1	.8408E-01	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.2820E+00
37	37	1	2	.7621E-01	.5296E+01	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2822E+00
38	38	1	3	.7255E-01	.1073E+02	.1368E-03	.1681E-03	.5456E-03	.7730E-04	.9278E-03	.2831E+00
39	39	1	4	.7621E-01	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.2561E-02	.2856E+00
40	40	2	1	.8408E-01	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.2858E+00
41	41	2	2	.7621E-01	.5296E+01	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2859E+00
42	42	2	3	.7255E-01	.1073E+02	.1368E-03	.1681E-03	.5456E-03	.7730E-04	.9278E-03	.2869E+00
43	43	2	4	.7621E-01	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.2561E-02	.2894E+00
44	44	3	1	.8408E-01	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.2895E+00
45	45	3	2	.7621E-01	.5296E+01	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2897E+00
46	46	3	3	.7255E-01	.1073E+02	.1368E-03	.1681E-03	.5456E-03	.7730E-04	.9278E-03	.2906E+00
47	47	3	4	.7621E-01	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.2561E-02	.2932E+00
48	48	4	1	.8408E-01	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.2932E+00
49	49	4	2	.7621E-01	.5296E+01	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.2932E+00
50	50	4	3	.7255E-01	.1073E+02	.1368E-03	.1681E-03	.5456E-03	.7730E-04	.9278E-03	.2950E+00
51	51	4	4	.7621E-01	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.2561E-02	.2988E+00
52	52	5	1	.8408E-01	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.3045E+00
53	53	5	2	.7621E-01	.5296E+01	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.3045E+00
54	54	5	3	.7255E-01	.1073E+02	.1368E-03	.1681E-03	.5456E-03	.7730E-04	.9278E-03	.3045E+00
55	55	5	4	.7621E-01	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.2561E-02	.3045E+00
56	56	6	1	.8408E-01	.1126E+01	.3080E-05	.8201E-05	.5246E-04	.4547E-04	.1092E-03	.3358E+00
57	57	6	2	.7621E-01	.5296E+01	.3080E-05	.9226E-05	.6295E-04	.1046E-03	.1798E-03	.3358E+00
58	58	6	3	.7255E-01	.1073E+02	.1368E-03	.1681E-03	.5456E-03	.7730E-04	.9278E-03	.3516E+00
59	59	6	4	.7621E-01	.5296E+01	.1805E-03	.2665E-03	.1395E-02	.7184E-03	.2561E-02	.3516E+00

Table 4-5a. (Continued)

60	7	1	1	-8408E-01	-1126E+01	-6696E-07	-1491E-06	0.	-1364E-03	-1366E-03	-3531E+00
61	2	2	2	-7621E-01	-5296E+01	-6998E-07	-1677E-06	0.	-3137E-03	-3140E-03	-3534E+00
62	7	3	3	-7255E-01	-1073E+02	-2973E-05	-3057E-05	0.	-2319E-03	-2379E-03	-3537E+00
63	7	4	4	-7621E-01	-5296E+01	-1924E-05	-4846E-05	0.	-2155E-02	-2164E-02	-3558E+00
64	1	1	1	-8408E-01	-1126E+01	-1453E-04	-3623E-04	-3810E-03	-8958E-03	-1288E-02	-3572E+00
65	1	3	3	-7621E-01	-5296E+01	-1453E-04	-4078E-04	-4572E-03	-2060E-02	-2378E-02	-3597E+00
66	1	3	3	-7255E-01	-1073E+02	-6452E-03	-7428E-03	-3963E-02	-1523E-02	-2632E-01	-3666E+00
67	1	4	4	-7621E-01	-5296E+01	-8515E-03	-1178E-02	-1014E-01	-1415E-01	-2632E-01	-3929E+00
68	2	1	1	-8408E-01	-1126E+01	-3348E-06	-1342E-05	-1657E-04	-1046E-03	-1228E-03	-3931E+00
69	2	2	2	-7621E-01	-5296E+01	-3348E-06	-1510E-05	-1988E-04	-2405E-03	-2623E-03	-3933E+00
70	2	3	3	-7255E-01	-1073E+02	-1487E-04	-2751E-04	-1723E-03	-1778E-03	-3925E-03	-3937E+00
71	2	4	4	-7621E-01	-5296E+01	-1962E-04	-4361E-04	-4407E-03	-1652E-02	-2156E-02	-3959E+00
72	3	1	1	-8408E-01	-1126E+01	-3348E-06	-1193E-05	-1381E-04	-4547E-04	-6080E-04	-3960E+00
73	3	3	3	-7621E-01	-5296E+01	-1487E-04	-1342E-05	-1657E-04	-1046E-03	-1228E-03	-3963E+00
74	3	3	3	-7255E-01	-1073E+02	-1487E-04	-2445E-04	-1436E-03	-7730E-04	-2602E-03	-3974E+00
75	3	4	4	-7621E-01	-5296E+01	-1962E-04	-3877E-04	-3672E-03	-7184E-03	-1144E-02	-3975E+00
76	1	1	1	-8408E-01	-1126E+01	-6157E-06	-4040E-05	-5484E-04	-2965E-04	-8001E-04	-3977E+00
77	1	1	2	-7621E-01	-5296E+01	-1578E-06	-4545E-05	-5484E-04	-2965E-04	-8001E-04	-3977E+00
78	1	1	3	-7255E-01	-1073E+02	-2734E-04	-8282E-04	-4753E-03	-5040E-04	-6359E-03	-3983E+00
79	1	1	4	-7621E-01	-5296E+01	-3608E-04	-1313E-03	-1216E-02	-4684E-03	-1851E-02	-4001E+00
80	1	2	1	-8408E-01	-1126E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-5612E-05	-4022E+00
81	1	2	2	-7621E-01	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-1053E-04	-4022E+00
82	1	2	3	-7255E-01	-1073E+02	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-3025E-04	-4022E+00
83	1	2	4	-7621E-01	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-1132E-03	-4033E+00
84	1	3	1	-8408E-01	-1126E+01	-1419E-07	-1330E-06	-1655E-05	-3505E-05	-3303E-05	-4033E+00
85	1	3	2	-7621E-01	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-5612E-05	-4033E+00
86	1	3	3	-7255E-01	-1073E+02	-6299E-06	-2727E-05	-1722E-04	-2559E-05	-2314E-04	-4033E+00
87	1	3	4	-7621E-01	-5296E+01	-8314E-06	-4323E-05	-4053E-04	-2378E-04	-7298E-04	-4044E+00
88	2	1	1	-8408E-01	-1126E+01	-6157E-06	-4040E-05	-5484E-04	-2965E-04	-8001E-04	-4006E+00
89	2	1	2	-7621E-01	-5296E+01	-1578E-06	-4545E-05	-5484E-04	-2965E-04	-8001E-04	-4006E+00
90	2	1	3	-7255E-01	-1073E+02	-2734E-04	-8282E-04	-4753E-03	-5040E-04	-6359E-03	-4013E+00
91	2	1	4	-7621E-01	-5296E+01	-3608E-04	-1313E-03	-1216E-02	-4684E-03	-1851E-02	-4031E+00
92	2	2	1	-8408E-01	-1126E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-5612E-05	-4031E+00
93	2	2	2	-7621E-01	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-1053E-04	-4031E+00
94	2	2	3	-7255E-01	-1073E+02	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-3025E-04	-4032E+00
95	2	2	4	-7621E-01	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-1132E-03	-4033E+00
96	2	3	1	-8408E-01	-1126E+01	-1419E-07	-1330E-06	-1655E-05	-3505E-05	-3303E-05	-4033E+00
97	2	3	2	-7621E-01	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-5612E-05	-4033E+00
98	2	3	3	-7255E-01	-1073E+02	-6299E-06	-2727E-05	-1722E-04	-2559E-05	-2314E-04	-4033E+00
99	2	3	4	-7621E-01	-5296E+01	-8314E-06	-4323E-05	-4053E-04	-2378E-04	-7298E-04	-4034E+00
100	3	1	1	-8408E-01	-1126E+01	-6157E-06	-4040E-05	-5484E-04	-2965E-04	-8001E-04	-4035E+00
101	3	1	2	-7621E-01	-5296E+01	-1578E-06	-4545E-05	-5484E-04	-2965E-04	-8001E-04	-4035E+00
102	3	1	3	-7255E-01	-1073E+02	-2734E-04	-8282E-04	-4753E-03	-5040E-04	-6359E-03	-4036E+00
103	3	1	4	-7621E-01	-5296E+01	-3608E-04	-1313E-03	-1216E-02	-4684E-03	-1851E-02	-4036E+00
104	3	2	1	-8408E-01	-1126E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-5612E-05	-4036E+00
105	3	2	2	-7621E-01	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-1053E-04	-4036E+00
106	3	2	3	-7255E-01	-1073E+02	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-3025E-04	-4036E+00
107	3	2	4	-7621E-01	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-1132E-03	-4036E+00
108	3	3	1	-8408E-01	-1126E+01	-1419E-07	-1330E-06	-1655E-05	-3505E-05	-3303E-05	-4036E+00
109	3	3	2	-7621E-01	-5296E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-5612E-05	-4036E+00
110	3	3	3	-7255E-01	-1073E+02	-6299E-06	-2727E-05	-1722E-04	-2559E-05	-2314E-04	-4036E+00
111	3	3	4	-7621E-01	-5296E+01	-8314E-06	-4323E-05	-4053E-04	-2378E-04	-7298E-04	-4036E+00
112	4	1	1	-8408E-01	-1126E+01	-6157E-06	-4040E-05	-5484E-04	-2965E-04	-8001E-04	-4036E+00
113	4	1	2	-7621E-01	-5296E+01	-1578E-06	-4545E-05	-5484E-04	-2965E-04	-8001E-04	-4036E+00
114	4	1	3	-7255E-01	-1073E+02	-2734E-04	-8282E-04	-4753E-03	-5040E-04	-6359E-03	-4036E+00
115	4	1	4	-7621E-01	-5296E+01	-3608E-04	-1313E-03	-1216E-02	-4684E-03	-1851E-02	-4036E+00
116	4	2	1	-8408E-01	-1126E+01	-1419E-07	-1496E-06	-1987E-05	-3462E-05	-5612E-05	-4036E+00
117	4	2	2	-7621E-01	-5296E+01	-1419E-07	-1683E-06	-2384E-05	-7961E-05	-1053E-04	-4036E+00
118	4	2	3	-7255E-01	-1073E+02	-6299E-06	-3067E-05	-2067E-04	-5885E-05	-3025E-04	-4036E+00
119	4	2	4	-7621E-01	-5296E+01	-8314E-06	-4863E-05	-5285E-04	-5469E-04	-1132E-03	-4036E+00

Table 4-5a. (Continued)

120	4	3	1	8408E-01	1126E+01	3146E-07	2926E-06	7364E-05	5057E-04	5826E-04	4385E+00
121	4	3	2	7621E-01	5296E+01	3146E-07	329E-06	8837E-05	1163E-03	1255E-03	4386E+00
122	4	3	3	7255E-01	1073E+02	1397E-05	599E-05	7659E-04	8597E-04	1699E-03	4388E+00
123	4	3	4	7621E-01	5296E+01	1843E-05	5510E-05	1959E-03	7990E-03	1006E-02	4398E+00
124	5	1	1	8408E-01	1126E+01	8031E-07	4407E-06	1804E-04	4596E-03	4781E-03	4403E+00
125	5	1	2	7621E-01	5296E+01	8031E-07	4958E-06	2165E-04	1057E-02	1079E-02	4414E+00
126	5	1	3	7255E-01	1073E+02	3566E-05	5035E-05	1876E-03	7812E-03	9815E-03	4423E+00
127	5	1	4	7621E-01	5296E+01	4706E-05	1432E-04	4799E-03	7261E-02	7760E-02	4501E+00
128	5	2	1	8408E-01	1126E+01	1851E-08	1632E-07	7844E-06	5365E-04	5446E-04	4502E+00
129	5	2	2	7621E-01	5296E+01	1851E-08	1836E-07	9412E-06	1234E-03	1244E-03	4503E+00
130	5	2	3	7255E-01	1073E+02	8216E-07	3346E-06	8157E-05	9121E-04	9978E-04	4504E+00
131	5	2	4	7621E-01	5296E+01	1084E-06	5305E-06	2086E-04	8477E-03	8692E-03	4512E+00
132	5	3	1	8408E-01	1126E+01	1851E-08	1451E-07	6536E-06	2333E-04	2400E-04	4513E+00
133	5	3	2	7621E-01	5296E+01	1851E-08	1632E-07	7844E-06	5365E-04	5446E-04	4513E+00
134	5	3	3	7255E-01	1073E+02	8216E-07	2975E-06	6798E-05	3966E-04	4683E-04	4514E+00
135	5	3	4	7621E-01	5296E+01	1084E-06	4716E-06	1739E-04	3686E-03	3865E-03	4518E+00
136	6	1	1	8408E-01	1126E+01	6693E-07	5876E-06	1203E-04	2955E-04	4233E-04	4518E+00
137	6	1	2	7621E-01	5296E+01	6693E-07	6611E-06	1443E-04	6819E-04	8335E-04	4519E+00
138	6	1	3	7255E-01	1073E+02	2972E-05	1205E-04	1251E-03	5040E-04	1905E-03	4521E+00
139	6	1	4	7621E-01	5296E+01	3922E-05	1910E-04	3199E-03	4684E-03	8114E-03	4529E+00
140	6	2	1	8408E-01	1126E+01	1542E-08	2176E-07	5229E-06	3462E-05	4008E-05	4529E+00
141	6	2	2	7621E-01	5296E+01	1542E-08	2449E-07	6275E-06	7961E-05	8615E-05	4529E+00
142	6	2	3	7255E-01	1073E+02	6847E-07	4462E-06	5438E-05	5885E-05	1184E-04	4529E+00
143	6	2	4	7621E-01	5296E+01	9037E-07	7074E-06	1391E-04	5469E-04	6940E-04	4530E+00
144	6	3	1	8408E-01	1126E+01	1542E-08	1935E-07	4358E-06	1505E-05	1962E-05	4530E+00
145	6	3	2	7621E-01	5296E+01	1542E-08	2176E-07	5229E-06	3462E-05	4008E-05	4530E+00
146	6	3	3	7255E-01	1073E+02	6847E-07	3966E-06	4532E-05	2559E-05	7555E-05	4530E+00
147	6	3	4	7621E-01	5296E+01	9037E-07	5288E-06	1159E-04	2378E-04	3609E-04	4530E+00
148	7	1	1	8408E-01	1126E+01	1339E-07	7346E-07	0.	8895E-04	8903E-04	4531E+00
149	7	1	2	7621E-01	5296E+01	1339E-07	8264E-07	0.	2046E-03	2047E-03	4533E+00
150	7	1	3	7255E-01	1073E+02	5943E-06	1506E-05	0.	1512E-03	1533E-03	4535E+00
151	7	1	4	7621E-01	5296E+01	7844E-06	2387E-05	0.	1405E-02	1409E-02	4549E+00
152	7	2	1	8408E-01	1126E+01	3084E-09	2721E-08	0.	1038E-04	1039E-04	4549E+00
153	7	2	2	7621E-01	5296E+01	3084E-09	3061E-08	0.	2388E-04	2389E-04	4549E+00
154	7	2	3	7255E-01	1073E+02	1369E-07	5577E-07	0.	1765E-04	1772E-04	4549E+00
155	7	2	4	7621E-01	5296E+01	1807E-07	8842E-07	0.	1641E-03	1642E-03	4551E+00
156	7	3	1	8408E-01	1126E+01	3084E-09	2418E-08	0.	4515E-05	4518E-05	4551E+00
157	7	3	2	7621E-01	5296E+01	3084E-09	2721E-08	0.	1038E-04	1039E-04	4551E+00
158	7	3	3	7255E-01	1073E+02	1369E-07	4958E-07	0.	7676E-05	7739E-05	4551E+00
159	7	3	4	7621E-01	5296E+01	1807E-07	7860E-07	0.	7134E-04	7143E-04	4552E+00
160	*****	*****	*****	0.	0.	-R	-R	-R	-R	5435E+00	9987E+00

Table 4-5b. Sorted array for solar source transfer-coefficients
(and carried-along weights) for sample Problem 5.

TRANS, WT =								
0.	0.	.6451E-03	.4385E+00	.3887E-02	.1992E-02	.3887E-02	.4231E-02	
.4398E-02	.2271E-01	.1048E-01	.5741E-01	.2714E-01	.4265E-02	.2714E-01	.4231E-02	
.3171E-01	.4231E-02	.5061E-01	.4519E-01	.5061E-01	.3925E-02	.5061E-01	.6080E-04	
.5061E-01	.2695E-02	.5061E-01	.3140E-03	.5061E-01	.2726E-02	.5061E-01	.1798E-03	
.5061E-01	.1092E-03	.5061E-01	.2726E-02	.5061E-01	.1798E-03	.5061E-01	.1992E-02	
.5061E-01	.1228E-03	.5061E-01	.1798E-03	.5061E-01	.1092E-03	.5061E-01	.3738E-01	
.5061E-01	.3821E-02	.5061E-01	.1786E-02	.5061E-01	.1450E-01	.5061E-01	.1647E-02	
.5061E-01	.7268E-03	.5061E-01	.1328E-02	.5061E-01	.2726E-02	.5061E-01	.1092E-03	
.5061E-01	.1366E-03	.7255E-01	.9278E-03	.7255E-01	.1167E-01	.7255E-01	.3025E-04	
.7255E-01	.2379E-03	.7255E-01	.9278E-03	.7255E-01	.1450E-02	.7255E-01	.9278E-03	
.7255E-01	.6873E-02	.7255E-01	.3025E-04	.7255E-01	.2602E-03	.7255E-01	.2602E-03	
.7255E-01	.5697E-02	.7255E-01	.2314E-04	.7255E-01	.6359E-03	.7255E-01	.6359E-03	
.7255E-01	.4683E-04	.7255E-01	.3925E-03	.7255E-01	.3025E-04	.7255E-01	.1699E-03	
.7255E-01	.2314E-04	.7255E-01	.4050E-02	.7255E-01	.6359E-03	.7255E-01	.9815E-03	
.7255E-01	.1184E-04	.7255E-01	.2978E-03	.7255E-01	.1772E-04	.7255E-01	.2314E-04	
.7255E-01	.7555E-05	.7255E-01	.7739E-05	.7255E-01	.1905E-03	.7255E-01	.1533E-03	
.7255E-01	.9978E-04	.7621E-01	.1798E-03	.7621E-01	.2561E-02	.7621E-01	.2561E-02	
.7621E-01	.3821E-02	.7621E-01	.1851E-02	.7621E-01	.3133E-01	.7621E-01	.1228E-03	
.7621E-01	.2561E-02	.7621E-01	.1144E-02	.7621E-01	.1798E-03	.7621E-01	.3140E-03	
.7621E-01	.2632E-01	.7621E-01	.1647E-02	.7621E-01	.2623E-03	.7621E-01	.1174E-01	
.7621E-01	.2156E-02	.7621E-01	.1282E-03	.7621E-01	.2164E-02	.7621E-01	.1851E-02	
.7621E-01	.2573E-02	.7621E-01	.1798E-03	.7621E-01	.7298E-04	.7621E-01	.1228E-03	
.7621E-01	.1282E-03	.7621E-01	.1144E-02	.7621E-01	.8692E-03	.7621E-01	.3925E-02	
.7621E-01	.1132E-03	.7621E-01	.4053E-01	.7621E-01	.5612E-05	.7621E-01	.1282E-03	
.7621E-01	.5612E-05	.7621E-01	.1053E-04	.7621E-01	.7298E-04	.7621E-01	.1132E-03	
.7621E-01	.7298E-04	.7621E-01	.1132E-03	.7621E-01	.1851E-02	.7621E-01	.5612E-05	
.7621E-01	.1053E-04	.7621E-01	.1255E-03	.7621E-01	.2785E-03	.7621E-01	.2547E-02	
.7621E-01	.2085E-02	.7621E-01	.2152E-01	.7621E-01	.1409E-02	.7621E-01	.7760E-02	
.7621E-01	.1006E-02	.7621E-01	.1244E-03	.7621E-01	.1079E-02	.7621E-01	.6615E-05	
.7621E-01	.8335E-04	.7621E-01	.5446E-04	.7621E-01	.8114E-03	.7621E-01	.3865E-03	
.7621E-01	.1053E-04	.7621E-01	.3609E-04	.7621E-01	.6940E-04	.7621E-01	.2047E-03	
.7621E-01	.4008E-05	.7621E-01	.2389E-04	.7621E-01	.1039E-04	.7621E-01	.1642E-03	
.7621E-01	.7143E-04	.8408E-01	.1092E-03	.8408E-01	.6080E-04	.8408E-01	.7268E-03	
.8408E-01	.1786E-02	.8408E-01	.1092E-03	.8408E-01	.1366E-03	.8408E-01	.6001E-04	
.8408E-01	.6080E-04	.8408E-01	.1228E-03	.8408E-01	.1328E-02	.8408E-01	.1092E-03	
.8408E-01	.3308E-05	.8408E-01	.5612E-05	.8408E-01	.8001E-04	.8408E-01	.3308E-05	
.8408E-01	.8001E-04	.8408E-01	.1255E-03	.8408E-01	.1210E-02	.8408E-01	.3308E-05	
.8408E-01	.5612E-05	.8408E-01	.5826E-04	.8408E-01	.4233E-04	.8408E-01	.2400E-04	
.8408E-01	.5446E-04	.8408E-01	.4781E-03	.8408E-01	.4008E-05	.8408E-01	.4518E-05	
.8408E-01	.1039E-04	.8408E-01	.8903E-04	.8408E-01	.1962E-05	.8408E-01	.5612E-05	
.8408E-01	.1992E-02							

Table 4-5c. Cumulative, normalized weight arrays for solar source transfer-coefficients and emission radiances in sample Problem 5.

WT,WT1 =								
0.	0.	.4907E+00	.5620E-05	.4929E+00	.8573E-04	.4976E+00	.8904E-04	
.5231E+00	.1691E-03	.5873E+00	.1725E-03	.5921E+00	.1384E-02	.5968E+00	.1387E-02	
.6015E+00	.1393E-02	.6521E+00	.1502E-02	.6565E+00	.3497E-02	.6566E+00	.4224E-02	
.6596E+00	.6013E-02	.6599E+00	.6122E-02	.6630E+00	.6259E-02	.6632E+00	.6368E-02	
.6633E+00	.6429E-02	.6663E+00	.6552E-02	.6666E+00	.7881E-02	.6688E+00	.7887E-02	
.6689E+00	.7948E-02	.6691E+00	.7972E-02	.6692E+00	.8026E-02	.7111E+00	.8505E-02	
.7153E+00	.8509E-02	.7173E+00	.8589E-02	.7336E+00	.8600E-02	.7354E+00	.8689E-02	
.7362E+00	.8691E-02	.7377E+00	.8749E-02	.7408E+00	.8791E-02	.7409E+00	.8917E-02	
.7410E+00	.8922E-02	.7421E+00	.8995E-02	.7551E+00	.9108E-02	.7552E+00	.9236E-02	
.7554E+00	.9242E-02	.7565E+00	.9253E-02	.7581E+00	.9258E-02	.7591E+00	.9372E-02	
.7668E+00	.9445E-02	.7669E+00	.9558E-02	.7671E+00	.1141E-01	.7674E+00	.1142E-01	
.7738E+00	.1143E-01	.7738E+00	.1156E-01	.7745E+00	.1174E-01	.7753E+00	.1429E-01	
.7753E+00	.1685E-01	.7757E+00	.3839E-01	.7758E+00	.3847E-01	.7760E+00	.4103E-01	
.7760E+00	.4359E-01	.7805E+00	.4742E-01	.7812E+00	.4760E-01	.7823E+00	.4778E-01	
.7824E+00	.4790E-01	.7827E+00	.4955E-01	.7827E+00	.5070E-01	.7827E+00	.6245E-01	
.7827E+00	.9382E-01	.7827E+00	.9776E-01	.7830E+00	.9992E-01	.7831E+00	.1405E+00	
.7832E+00	.1431E+00	.7834E+00	.1434E+00	.7863E+00	.1697E+00	.7892E+00	.1699E+00	
.7935E+00	.1701E+00	.7955E+00	.1713E+00	.8306E+00	.1734E+00	.8307E+00	.1736E+00	
.8336E+00	.1746E+00	.8349E+00	.1764E+00	.8351E+00	.1775E+00	.8354E+00	.1775E+00	
.8649E+00	.1853E+00	.8567E+00	.1853E+00	.8670E+00	.1855E+00	.8801E+00	.1859E+00	
.8825E+00	.1877E+00	.8827E+00	.1878E+00	.8851E+00	.1879E+00	.8872E+00	.1887E+00	
.8901E+00	.1887E+00	.8903E+00	.1887E+00	.8903E+00	.1887E+00	.8905E+00	.1887E+00	
.8906E+00	.1890E+00	.8919E+00	.1891E+00	.8929E+00	.1905E+00	.8973E+00	.1908E+00	
.8974E+00	.1908E+00	.9427E+00	.1929E+00	.9428E+00	.1930E+00	.9429E+00	.1931E+00	
.9429E+00	.1940E+00	.9429E+00	.1949E+00	.9430E+00	.1949E+00	.9431E+00	.1949E+00	
.9432E+00	.1956E+00	.9433E+00	.1956E+00	.9454E+00	.1959E+00	.9454E+00	.1999E+00	
.9454E+00	.2056E+00	.9456E+00	.2057E+00	.9459E+00	.2063E+00	.9487E+00	.2069E+00	
.9511E+00	.2084E+00	.9751E+00	.2088E+00	.9767E+00	.2088E+00	.9854E+00	.2097E+00	
.9865E+00	.2099E+00	.9867E+00	.2102E+00	.9879E+00	.2103E+00	.9879E+00	.2112E+00	
.9880E+00	.2115E+00	.9880E+00	.2117E+00	.9889E+00	.2118E+00	.9894E+00	.2119E+00	
.9894E+00	.2188E+00	.9894E+00	.2190E+00	.9895E+00	.2307E+00	.9897E+00	.2307E+00	
.9897E+00	.2307E+00	.9898E+00	.2317E+00	.9898E+00	.2317E+00	.9900E+00	.2317E+00	
.9900E+00	.2317E+00	.9902E+00	.2337E+00	.9902E+00	.2376E+00	.9910E+00	.2377E+00	
.9930E+00	.2379E+00	.9932E+00	.2753E+00	.9933E+00	.2780E+00	.9934E+00	.2798E+00	
.9935E+00	.2943E+00	.9936E+00	.3396E+00	.9951E+00	.3435E+00	.9952E+00	.3436E+00	
.9952E+00	.3463E+00	.9952E+00	.3464E+00	.9953E+00	.3491E+00	.9953E+00	.3494E+00	
.9954E+00	.3496E+00	.9955E+00	.3497E+00	.9969E+00	.3498E+00	.9969E+00	.3515E+00	
.9969E+00	.3522E+00	.9970E+00	.3535E+00	.9970E+00	.3537E+00	.9970E+00	.3539E+00	
.9971E+00	.3566E+00	.9976E+00	.3608E+00	.9976E+00	.3651E+00	.9977E+00	.3693E+00	
.9977E+00	.4268E+00	.9978E+00	.4495E+00	.9978E+00	.4515E+00	.9978E+00	.4558E+00	
.1000E+01	.1000E+01							
STATISTICAL CLOUDS, P1,P2,P3,P4 = .10 .25 .50 .90								
SUN TRANSFER COEF S1,S2,S3,S4 = .131E-03 .329E-03 .393E-02 .762E-01								
EMISSION E1,E2,E3,E4 = .570E+01 .639E+02 .261E+03 .314E+03								

Table 4-6. Definitions of quantities in Tables 4-4a and 4-5a.

Column	Heading	Description
1	IDX	Cloud-configuration index
2,3,4	LL,MM,HH	Cloud indexes for low-, medium-, and high-layer clouds
5	TRANS	Transfer coefficient (for artificial source in Table 4-4a and for solar source in Table 4-5a)
6	EMISS	Emission radiance from highest cloud in set (independent of type of source)
7,8,9,10	CC=2,3,4,5	Weights or relative occurrence frequencies of given cloud set with cloud-coverage category CC (or cloud-coverage fractions of 0.3, 0.5, 0.8, and 1.0)
11	WT	Total weight or relative occurrence frequency of given cloud set (sum of weights for CC=2,3,4,5)
12	WT(SUM)	Cumulative sum of WT for all cloud-configuration sets

(Appendix Equation (30a)) exceeds 100. In this event function TRANSF uses the initialized value of FLUX, $1.E-50$, an arbitrarily small value. The results for $IDX=160$ are provided by subroutine SCLOUD for the Earth's surface. The initial setting of $WT(160)$, the probability of seeing the ground with or without clouds being present, occurs in subroutine CLDWT, and the corresponding $WT(SUM)$ would be exactly 1.0 except for small numerical inconsistencies. $WT(160)$ is reset in subroutine SCLOUD to take account of the two-leg CFLOS required to see the ground lighted by the source (either artificial or the sun).

Before sorting the TRANS and EMISS arrays, we have augmented each of them (as well as the WT and WT1 arrays) with one additional member whose value is set to zero. This procedure allows subroutine LINEAR to interpolate within the array given to it when the weight of the smallest (nonzero) member exceeds the smallest fractile (now 0.10) for which an integral-distribution value is desired.

Tables 4-4b and 4-5b give the TRANS array after it has been sorted (by a call to subroutine SORTLJ from subroutine SCLOUD) in the order of increasing values. The WT array is simply carried along. The TRANS and WT values are presented in pairs in Tables 4-4b and 4-5b.

Table 4-4c gives the EMISS array after it has been sorted in the order of increasing values. The WT1 array is simply carried along. The EMISS and WT1 values are presented in pairs in Table 4-c.

Tables 4-4d and 4-5c give the cumulative, normalized weight arrays WT and WT1; these quantities are also presented in pairs.

At the end of Tables 4-4d and 4-5c the values of the transfer coefficient and emission radiance are given corresponding to the four user-selected fractiles (here taken to be 0.10, 0.25, 0.50, and 0.90) determined from the cumulative, normalized weight arrays WT (for transfer coefficient) and WT1 (for emission radiance).

We repeat, as noted in Section 2.2, that in the 160-member distributions for the solar source transfer-coefficients and emission radiances, there are only 10 different values (nine for clouds, one for the Earth) because (a) there are only nine different cloud-top altitudes (cf. Table 2-1), (b) the bidirectional reflectance of any cloud is assumed to be approximated by that for cloud-type 4 (stratocumulous), and (c) the directional emissivity computed for cloud-type 4 is used for all cloud types. We have collated the essential results for the solar source transfer-coefficient array in Table 4-7a and those for the emission radiance

Table 4-7a. Solar source transfer-coefficient distribution for sample Problem 5.

IDX	TCOEF sr ⁻¹	No. Of Cases	Total Weight	Cumul. Weight	Fractiles	TCOEF sr ⁻¹	CLD TOP km	TAIR	(TAIR) ²
					0.10	0.131 ⁻³			
					0.25	0.329 ⁻³			
160	0.6451 ⁻³	1	0.4907	0.4907			0.0	0.1424	0.02027
1,6	0.3887 ⁻²	2	0.0069	0.4976			1.0	0.2150	0.04622
					0.50	0.393 ⁻²			
5	0.4398 ⁻²	1	0.0255	0.5231			1.15	0.2287	0.05231
4	0.1048 ⁻¹	1	0.0642	0.5873			2.3	0.3531	0.1247
2,7	0.2714 ⁻¹	2	0.0095	0.5968			4.0	0.5681	0.3227
3	0.3171 ⁻¹	1	0.0047	0.6015			4.5	0.6141	0.3771
8,9,10	0.5061 ⁻¹	24	0.1395	0.7410			6.0	0.7758	0.6019
13	0.7255 ⁻¹	32	0.0422	0.7832			9.0	0.9289	0.8628
12,14	0.7621 ⁻¹	64	0.2068	0.9900	0.90	0.762 ⁻¹	10.0	0.9520	0.9063
11	0.8408 ⁻¹	32	0.0100	1.0000			12.0	1.0	1.0
		<u>160</u>	<u>1.0000</u>						

array in Table 4-7b. These latter two tables should facilitate understanding the values of the solar transfer-coefficient and emission radiance for the fractiles 0.10, 0.25, 0.50, and 0.90 printed at the end of Table 4-5c.

The variation in values of the (attenuated) solar source transfer-coefficient (TCOEF) for the nine cloud tops is due only to the variation in the (two-leg) air transmittance between the different cloud-top altitudes and 12-km altitude, as verified by our including in Table 4-7a the cloud-top altitude and the air transmittance from the cloud-top altitude to 12-km altitude. The variation in values of the (attenuated) emission radiance (EMISS) for the nine cloud tops is due to the combined effects of (a) the (one-leg) air transmittances from the different cloud-top altitudes to 12-km altitude and (b) the temperature entering the Planck emission function.

In the distributions presented in Tables 4-7a and 4-7b the importance of the Earth's surface is apparent since it has by far the largest single weight associated with it. This feature occurs not only for the data in KMODEL=1 but for the data given in BLOCK DATA for each of the 10 KMODELS. To illustrate this general feature we have evaluated the probability (P_{gnd}) for a detector, pointed straight down, of seeing the ground either with or without clouds being present:

$$P_{\text{gnd}} = \text{CCOVER}(1,K) + \\ \text{CCOVER}(2,K) \times \text{CFLOSF}(4,\theta) + \\ \text{CCOVER}(3,K) \times \text{CFLOSF}(6,\theta) + \\ \text{CCOVER}(4,K) \times \text{CFLOSF}(9,\theta) + \\ \text{CCOVER}(5,K) \times \text{CFLOSF}(11,\theta)$$

where $K = \text{KMODEL}$ and $\theta = 0$ degrees.

The results are:

<u>KMODEL</u>	<u>P_{gnd}</u>	<u>KMODEL</u>	<u>P_{gnd}</u>
1	0.543	6	0.611
2	0.543	7	0.666
3	0.484	8	0.591
4	0.633	9	0.628
5	0.513	10	0.559

Table 4-7b. Emission radiance distribution function for sample Problem 5.

IDX	EMISS		No. of Cases	Total Weight	Cumul. Weight	Fractiles	EMISS		CLD TOP km	T _c °K	ε X PLANCK		T AIR	ε X PLANCK X T AIR	
	$\frac{W}{2}$ km ² sr μm	$\frac{W}{2}$ km ² sr μm					$\frac{W}{2}$ km ² sr μm	$\frac{W}{2}$ km ² sr μm			$\frac{W}{2}$ km ² sr μm	$\frac{W}{2}$ km ² sr μm		$\frac{W}{2}$ km ² sr μm	$\frac{W}{2}$ km ² sr μm
11	1.1	1.1	32	0.0089	0.8922 ⁻²				12.0	210.00	1.13	1.0	1.0	1.1	1.1
12,14	5.3	5.3	64	0.1851	0.1940	0.10	5.3		10.0	223.00	5.56	0.9520		5.3	5.3
13	10.7	10.7	32	0.0377	0.2317				9.0	229.50	11.55	0.9289		10.7	10.7
8,9,10	63.9	63.9	24	0.1249	0.3566	0.25	63.9		6.0	249.00	82.35	0.7758		63.9	63.9
3	120.8	120.8	1	0.0042	0.3608				4.5	258.75	196.74	0.6141		120.8	120.8
2,7	147.3	147.3	2	0.0085	0.3693				4.0	262.00	259.25	0.5681		147.3	147.3
4	222.7	222.7	1	0.0575	0.4268				2.3	273.05	630.64	0.3531		222.7	222.7
5	252.9	252.9	1	0.0227	0.4495				1.15	280.52	1105.88	0.2287		252.9	252.9
1,6	255.3	255.3	2	0.0063	0.4558				1.0	281.50	1187.30	0.2150		255.3	255.3
						0.50	261								
						0.90	314								
160	327.5	327.5	$\frac{1}{160}$	0.5442 1.0000	1.0000				0.0	288.00	2300.40	0.1424		327.5	327.5

It is instructive to relate some of the Problem-5 results to those for Problems 1 to 3. The cloud configurations for IDX equal to 4, 8, and 13 in Table 4-4a are the same as those for Problems 1, 2, and 3, respectively. Since the source is below all clouds in both cases, we should expect the (transmission) transfer coefficients in Table 4-4a to correspond to those at zero lateral displacement in Problems 1, 2, and 3, except that air attenuation is included in Problem 5 but not in Problems 1, 2, and 3. However, the air-attenuation path is the same (cf. Figure 2-6b) for all cloud configurations in Problem 5. Thus, we expect that the TRANS results given in Table 4-4a for IDX = 4, 8, and 13 will differ by a constant factor from those for zero lateral displacement in Problems 1 to 3. To predict this factor we write:

$$\text{TRANS}(\text{Pm } 5) = \text{TC}'(\text{Pms } 1,2,3) \times \text{TAIR}(2.5,0.,0.01) \times (\text{SDISTO})^2.$$

By using the interpolation-extrapolation scheme for air transmittance as described in Section 3-2.28, we hand-calculate the air transmittance to be

$$\begin{aligned} \text{TAIR} &= T_1 (T_1/T_2)^{-(h-h_1)/(h_2-h_1)} \\ &= (0.2150) (0.2150/0.3247)^{-(0.01-1)/(2-1)} \\ &= 0.1430 \end{aligned}$$

and

$$(\text{SDISTO})^2 = (11.99)^2.$$

Thus we predict

$$\text{TRANS} = 20.55 \text{ TC}'.$$

It is satisfying that our prediction is correct, as seen from the data in Table 4-8.

The reason we did not include IDX=114 and Problem 4 in this comparison is that the integral to be evaluated for TRANS in Table 4-4a was skipped owing to the large argument of the sinh and cosh functions and the concomitant smallness of the value of TRANS. (See the related comment made previously with respect to Table 4-4a.)

Table 4-8. Comparison of transfer coefficients from Problem 5 with modified transfer coefficients from Problems 1 to 3.

IDX	TRANS ^a sr ⁻¹	(TC') ^b sr ⁻¹ km ⁻²	TRANS/TC' km ²
4	0.4617 ⁻¹	0.2247 ⁻²	20.55
8	0.6812 ⁻²	0.3315 ⁻³	20.55
13	0.2199 ⁻⁷	0.1070 ⁻⁸	20.55

^aFrom Table 4-4a.

^bFrom Table 4-2 for RANGE=0.0.

4-3.3 Problem 6: Use of the deterministic cloud submodel for an ellipsoidal cloud

Problem 6 illustrates the selection by subroutine LOS of lines-of-sight and the evaluation by subroutine CLOUD3 of transfer coefficients and emission radiances for these same lines-of-sight.

For this problem we have placed a single ellipsoidal cloud at 10-km altitude. The lengths of the semiaxes are $a=4$ km, $b=2$ km, and $c=1$ km. The cloud's properties are those for the Type-4 cloud (strato-cumulous; see Table 2-1). The artificial source is also placed at 10-km altitude and 10 km to the east of the cloud center. The solar source has a zenith angle of 45 degrees. The detector is at synchronous altitude, directly above the cloud. Wavelength is $2.5 \mu\text{m}$. We have made two runs, one (Problem 6a) with $\text{FOV} = 1 \text{ km}^2$ and the other (Problem 6b) with $\text{FOV} = 20 \text{ km}^2$. The input deck is shown in Figure 4-5.

Figure 4-6a is an outline of the cloud in a horizontal plane through its center. The 64 different x,y coordinates of the facet centers are shown by small dots. The 16 x,y coordinates of the facet centers that are considered in subroutine LOS by incrementing the facet-center indexes by two's are denoted by crosses.

Figure 4-6b pertains to the cloud for the artificial source. We show the 16 above-defined facet centers visible to the detector, marked by crosses. Of these, the three that are also visible to the source are marked as RI(R denotes reflective, I the sequence number (1 to 3)). For $\text{FOV} = 1 \text{ km}^2$, each of these three reflective points


```

***** PROBLEM 6A *****
  HD      THETAD  PHID  FOV      DETECTOR
 35793.   90.00001 -90.0001 1.0
HSORCE(1) THETAS(1) PHIS(1) WKT      SOURCE
 10.     90.000001 -89.90  1000.

  ISUN
    1
  ALAM
 2.50
  MODE
    0
  N CLOUD
    1
K CLOUD                                CLOUD PROPERTIES
  H CLOUD THETCD  PHICD  CLOUDA  CLOUDB  CLOUDC  CLDPSI
 4  10.     90.     -90.     4.0     2.0     1.0     0.

***** PROBLEM 6B *****
  HD      THETAD  PHID  FOV      DETECTOR
 35793.   90.00001 -90.0001 20.
HSORCE(1) THETAS(1) PHIS(1) WKT      SOURCE
 10.     90.000001 -89.90  1000.

  ISUN
    1
  ALAM
 2.50
  MODE
    0
  N CLOUD
    1
K CLOUD                                CLOUD PROPERTIES
  H CLOUD THETCD  PHICD  CLOUDA  CLOUDB  CLOUDC  CLDPSI
 4  10.     90.     -90.     4.0     2.0     1.0     0.

```

Figure 4-5. Input data for Problems 6a and 6b.

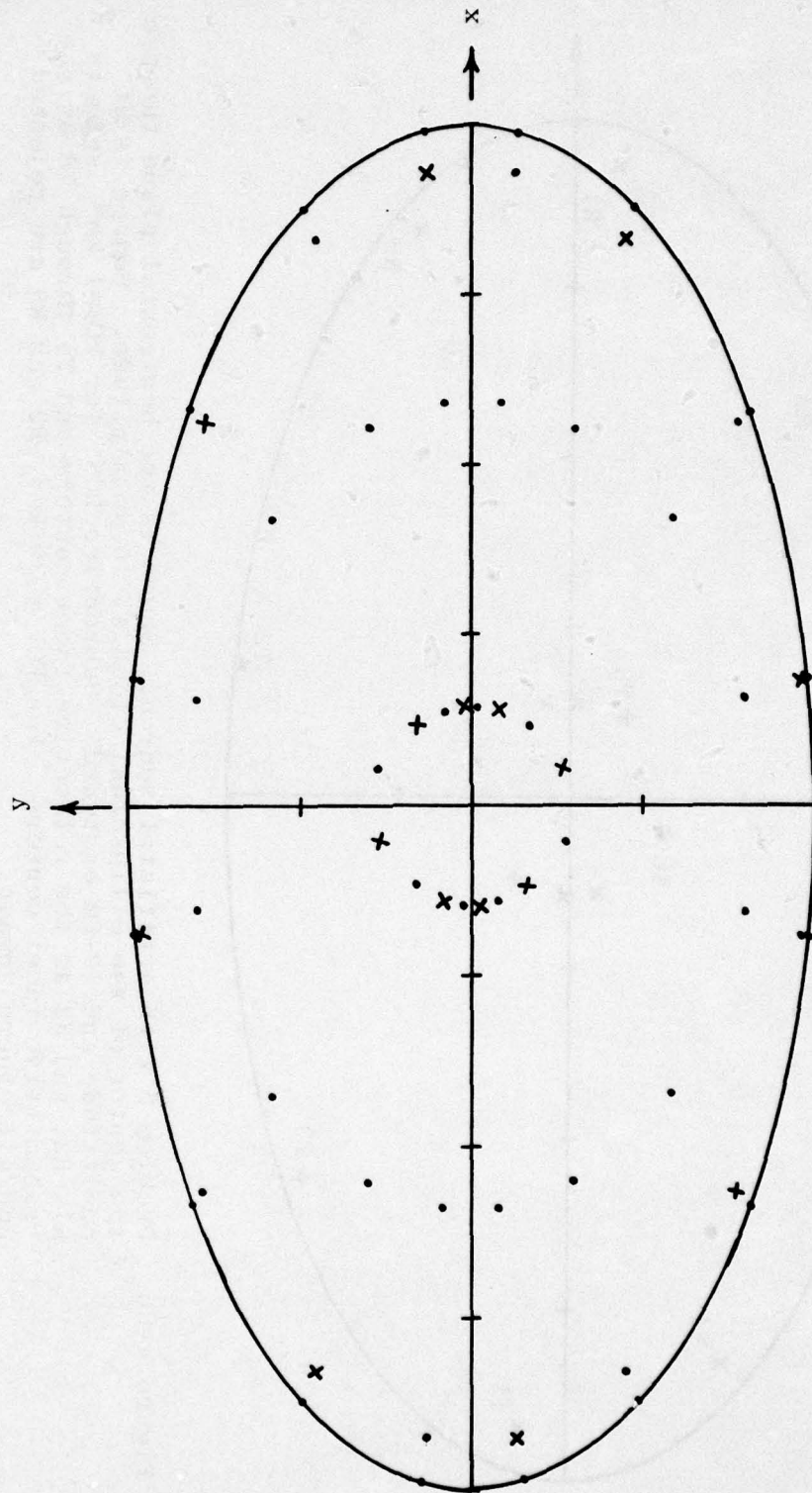


Figure 4-6a. Problem 6 cloud. Shown is the horizontal plane through the center of the ellipsoidal cloud at 10-km altitude. Projected positions of all facet centers are indicated by dots; those examined in subroutines for visibility are marked with crosses.

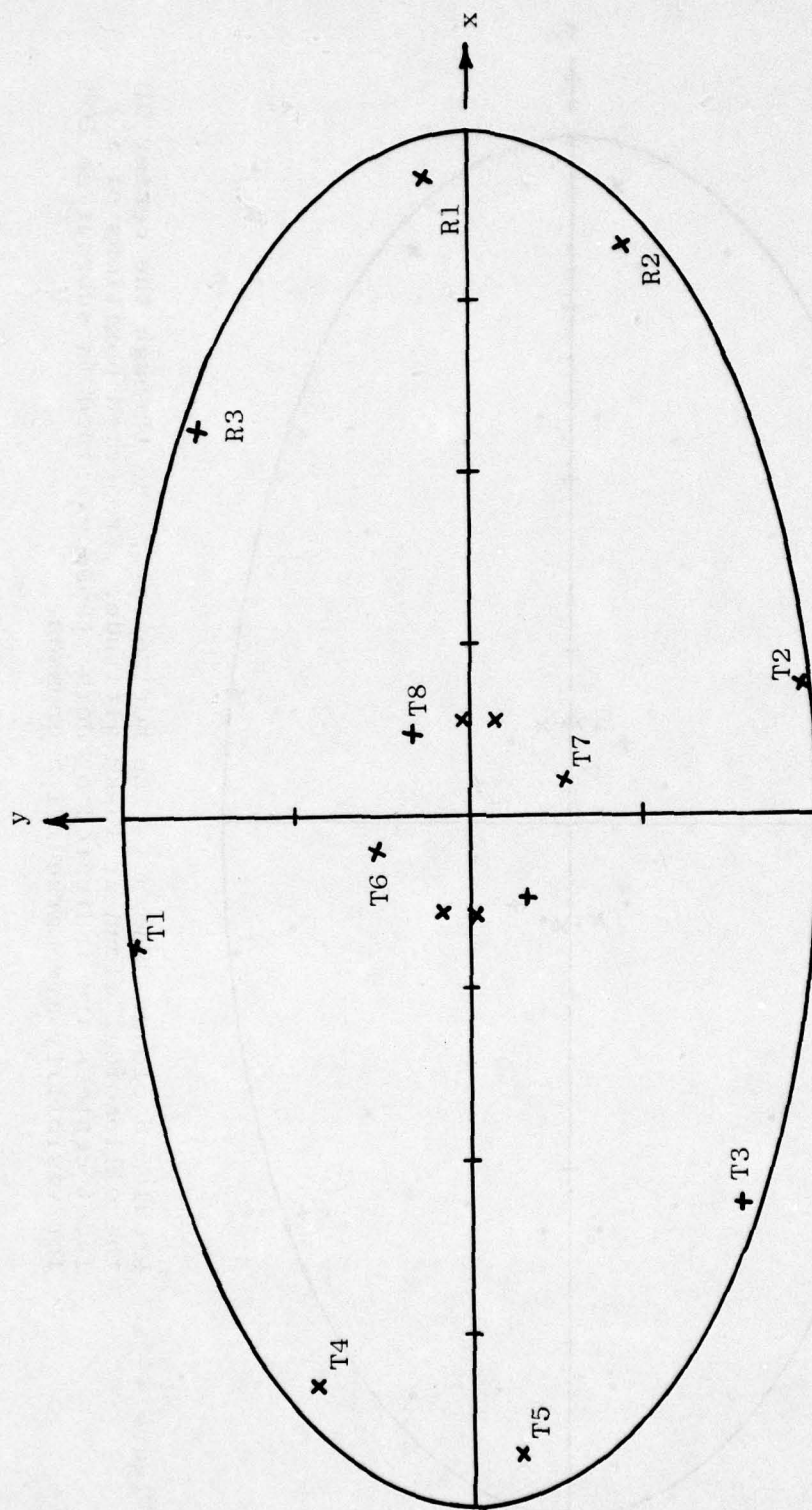


Figure 4-6b. Problem 6 with artificial source. Shown is the horizontal plane through the center of the ellipsoidal cloud at 10-km altitude. Source is at coalatitude and 10-km eastward. Subroutine LOS, for $FOV=1 \text{ km}^2$, selects R1, R2, and R3 as the reflective facet centers and T1 through T8 as the transmissive facet centers. For $FOV = 20 \text{ km}^2$, R2 and R3 are rejected and all others remain.

survives the selection process since none lines within $0.7 \sqrt{\text{FOV}}$ of another. For $\text{FOV} = 20 \text{ km}^2$, R2 and R3 do not survive the selection process. The remaining 13 points (16 minus 3) are transmittive; of these, eight (the maximum number of transmittive points retained by the code) are marked as TI (T denotes transmittive, I the sequence number (1 to 8)). These same eight points obtain for both values of FOV.

Figures 4-6c and 4-6d pertain to the cloud for the solar source and correspond to FOV being 1 km^2 and 20 km^2 , respectively. Again we show the 16 facet centers visible to the detector, marked by crosses. All of these facet centers are visible to the sun; there are no transmittive points. For $\text{FOV} = 1 \text{ km}^2$, 11 of the points (marked as R1 through R11 in Figure 4-6c) survive the selection process; for $\text{FOV} = 20 \text{ km}^2$, four of the points (marked as R1 through R4 in Figure 4-6d) survive the selection process.

The transfer coefficients, emission radiances, and cloud coordinates of the facet centers for both sources and FOV's are given in Table 4-9, to which a guide is provided in Table 10. The coordinates of the first reflective point and the eight transmittive points are, of course, the same in Parts (a) and (b).

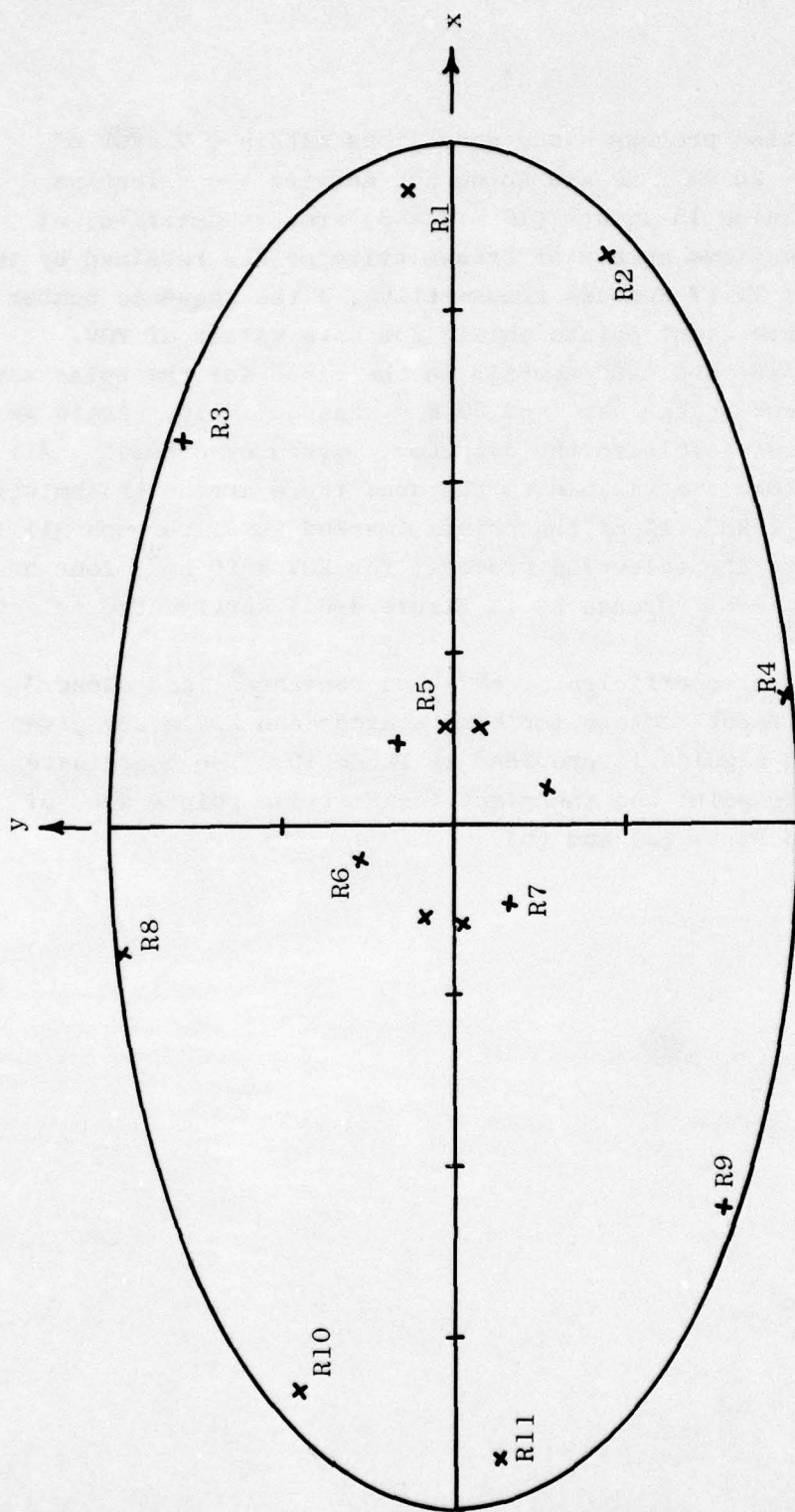


Figure 4-6c. Problem 6a with solar source. Shown is the horizontal plane through the center of the ellipsoidal cloud at 10-km altitude. Source is the sun, eastward at 45-deg zenith angle. Subroutine LOS, for $FOV=1 \text{ km}^2$, selects R1 through R11 as the reflective facet centers. There are no transmissive facet centers.

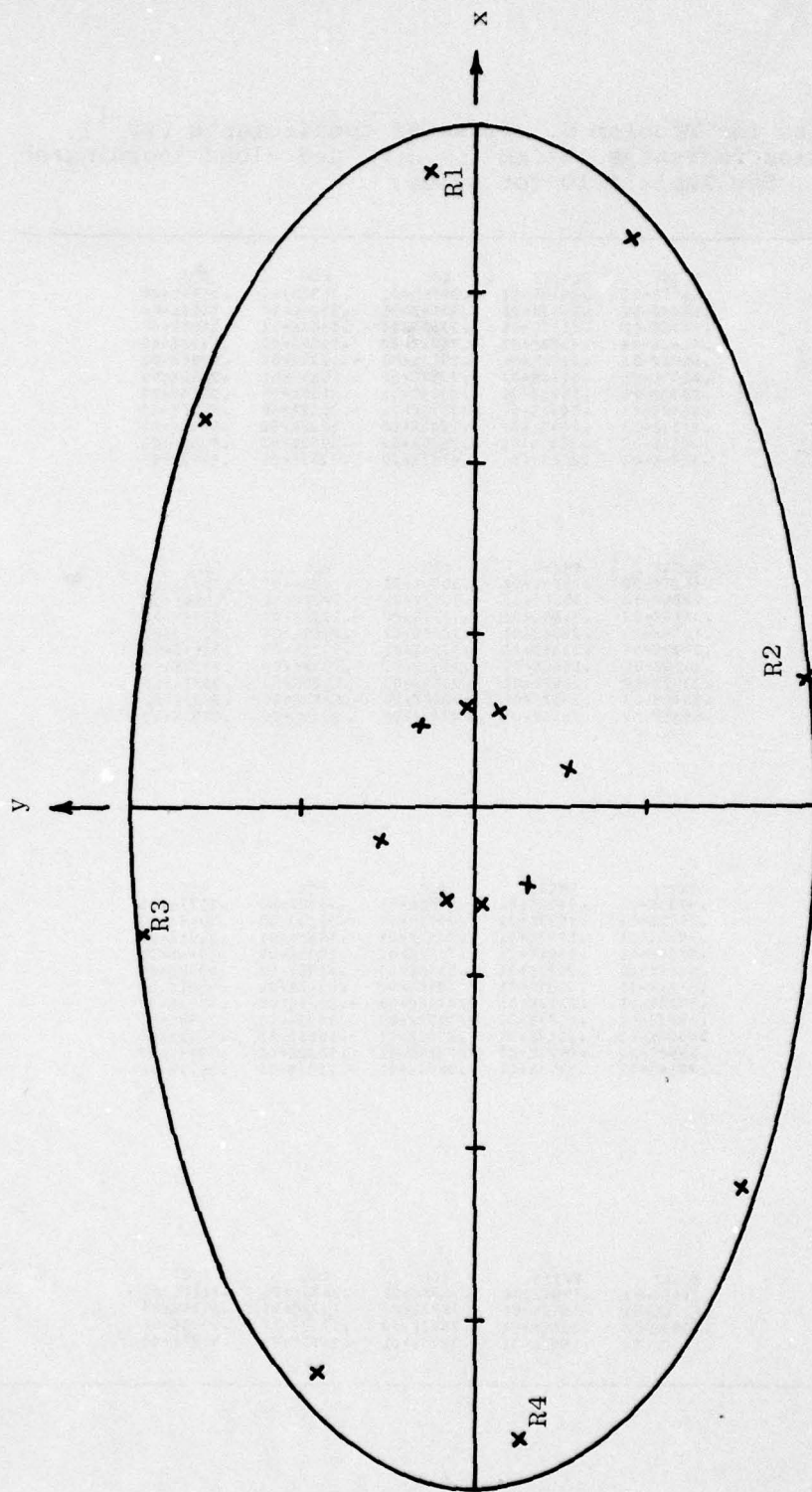


Figure 4-6d. Problem 6b with solar source. Shown is the horizontal plane through the center of the ellipsoidal cloud at 10-km altitude. Source is the sun, eastward at 45-deg zenith angle. Subroutine LOS, for $FOV=20 \text{ km}^2$, selects R1 through R4 as the reflective facet centers. There are no transmissive facet centers.

Table 4-9. Results for Problem 6. Transfer coefficients (sr^{-1}), emission radiances ($\text{W}/(\text{km}^2 \text{ sr } \mu\text{m})$), and cloud coordinates (km). See Table 4-10 for guide.

	TCOEF	EMISS	XCC	YCC	ZCC
(a)	.3483E-01	.2492E+01	.3698E+01	.2633E+00	.3577E+00
	.1844E-01	.1573E+01	.3314E+01	-.9026E+00	.3314E+00
	.5076E-02	.1117E+01	.2260E+01	.1563E+01	.2651E+00
	.4383E-04	.4348E+01	-.7572E+00	.1923E+01	.1994E+00
	.6605E-03	.4352E+01	.7572E+00	-.1923E+01	.1994E+00
	.5299E-06	.1118E+01	-.2260E+01	-.1563E+01	.2651E+00
	.1079E-06	.1573E+01	-.3314E+01	.9026E+00	.3314E+00
	.8940E-07	.2493E+01	-.3698E+01	-.2633E+00	.3577E+00
	.1151E-03	.2635E+01	-.2080E+00	.5282E+00	.9631E+00
	.2615E-03	.2635E+01	.2080E+00	-.5282E+00	.9631E+00
	.3276E-03	.2603E+01	.4747E+00	.3283E+00	.9793E+00

	TCOEF	EMISS	XCC	YCC	ZCC
(b)	.4626E-02	.1501E+01	.3698E+01	.2633E+00	.3577E+00
	.7286E-03	.3561E+01	-.7572E+00	.1923E+01	.1994E+00
	.3771E-02	.3565E+01	.7572E+00	-.1923E+01	.1994E+00
	.1054E-03	.3086E+01	-.2260E+01	-.1563E+01	.2651E+00
	.1722E-04	.2300E+01	-.3314E+01	.9026E+00	.3314E+00
	.1650E-05	.1502E+01	-.3698E+01	-.2633E+00	.3577E+00
	.2307E-02	.2552E+01	-.2080E+00	.5282E+00	.9631E+00
	.3846E-02	.2552E+01	.2080E+00	-.5282E+00	.9631E+00
	.5055E-02	.2515E+01	.4747E+00	.3283E+00	.9793E+00

	TCOEF	EMISS	XCC	YCC	ZCC
(c)	.4833E-01	.2492E+01	.3698E+01	.2633E+00	.3577E+00
	.2992E-01	.1573E+01	.3314E+01	-.9026E+00	.3314E+00
	.1930E-01	.1117E+01	.2260E+01	.1563E+01	.2651E+00
	.5125E-01	.4352E+01	.7572E+00	-.1923E+01	.1994E+00
	.6405E-01	.2581E+01	.5816E+00	.4140E-01	.9892E+00
	.5751E-01	.2635E+01	-.2080E+00	.5282E+00	.9631E+00
	.5927E-01	.2603E+01	-.4747E+00	-.3283E+00	.9793E+00
	.4914E-01	.4348E+01	-.7572E+00	.1923E+01	.1994E+00
	.5535E-02	.1118E+01	-.2260E+01	-.1563E+01	.2651E+00
	.6696E-02	.1573E+01	-.3314E+01	.9026E+00	.3314E+00
	.8916E-02	.2493E+01	-.3698E+01	-.2633E+00	.3577E+00

	TCOEF	EMISS	XCC	YCC	ZCC
(d)	.2768E-01	.1501E+01	.3698E+01	.2633E+00	.3577E+00
	.4876E-01	.3565E+01	.7572E+00	-.1923E+01	.1994E+00
	.4263E-01	.3561E+01	-.7572E+00	.1923E+01	.1994E+00
	.1612E-01	.1502E+01	-.3698E+01	-.2633E+00	.3577E+00

Table 4-10. Guide to Table 4-9 results.

Table 4-9 Part	Source	FOV km ²	Reflective Points	Transmittive Points
(a)	Artificial	1	3	8
(b)	Artificial	20	1	8
(c)	Solar	1	11	0
(d)	Solar	20	4	0

SECTION 5
REFERENCES

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- 6 D. A. Hamlin and M. R. Schoonover, "The ROSCOE Manual, Volume 27 - Natural Background Radiation (Earth Surface-Characterization and -Radiance, Upwelling Radiation, and Solar Radiation)," DNA 3964F-27 [SAI-78-604-LJ-6], January 1979.

APPENDIX A

SOME DIFFUSION PROBLEM SOLUTIONS

A-1 INTRODUCTION

The problem of determining the light flux out of clouds in various configurations of clouds and sources recurs frequently. For convenience the results for a number of such problems are collected here. No claim is made that these are novel or original, many of the solutions being well-known or using standard methods. A unified compilation with a consistent terminology may nevertheless be useful.

A rigorous treatment using the transport equation or Monte Carlo methods to evaluate the effects of scattering and absorption would be, at best, extremely time consuming. Additionally, the specification of the geometry of the clouds only approximates real cloud configurations, making such a careful evaluation of flux overly elaborate. Therefore the approach taken here has been to solve the problem in the approximation of the diffusion equation. The basic assumptions are that there be many scatterings and that precise surface effects be unimportant. An improvement over the most elementary diffusion equation solutions can be achieved by using scattering parameters based on rigorous transport theory or by using the results of Monte Carlo calculations to adjust the results.

A-1.1 Basic Equations

The development follows the lines indicated by Weinberg and Wigner⁽¹⁾ for neutrons. The basic equation to be solved is the diffusion equation:

$$D \operatorname{div} \operatorname{grad} \phi - \Sigma_a \phi + S = \frac{1}{v} \frac{\partial \phi}{\partial t} \quad (1)$$

where: ϕ is the light flux, photons/(cm² sec)

D is the diffusion coefficient

Σ_a is the macroscopic absorption cross-section

S is the light source per unit volume per unit time,
photons/(cm³ sec)

v is the speed of light

The required boundary conditions are given in terms of the flux:

$$J_{\pm} = a\phi + b \left(\mp \frac{\partial \phi}{\partial Z} - \frac{3}{2v} \frac{\partial \phi}{\partial t} \right) \quad (2)$$

J_{\pm} is the flux in the $\pm Z$ direction.

The constants, a and b , are left arbitrary. From the usual definition of flux, $b = D/2$. In "standard" usage, $a = \Sigma_s/4\Sigma$, $D = \Sigma_s/3\Sigma_{tr}$, and $\Sigma_{tr} = \Sigma - \bar{\mu}\Sigma_s$ where Σ , Σ_s , and Σ_{tr} are the macroscopic total, scattering, and transport cross-sections, respectively, and $\bar{\mu}$ is the average cosine of the scattering angle. Here a and b are left undermined to allow later evaluation using better values based on suitable exact calculations. In general the physical boundary conditions require a specified inward flux, sometimes zero. The frequently used "extrapolated end-point" formulation relates ϕ and $\partial\phi/\partial Z$ on the surface. The desired quantities are the emerging fluxes, the actual flux distribution inside the medium being of, at most, peripheral interest.

A-1.2 Diffusion Parameters for an Absorbing medium

In Section A-1.1 the "standard" evaluation was given for the diffusion parameters in terms of the macroscopic cross-sections. That evaluation is strictly applicable only in the limit of small absorption. A more generally applicable evaluation, which we adopt for numerical results in this report, is described in this section.

Case, de Hoffmann, and Placzek⁽²⁾ provide material suitable for a better evaluation based on exact solutions of some problems. The results of Case et al.⁽²⁾ are derived for isotropic scattering. In the present application, some modification has been made to account, at least partially, for anisotropic scattering. A judicious utilization of the transport cross-section (which introduces the anisotropy) must be made.

Case et al.⁽²⁾ use several parameters to which we must refer:

$c =$ average number of emergent particles per collision (cf. Reference 2, p. 43)

$$= \Sigma_s/\Sigma \quad (3)$$

$$= \begin{cases} 0 & \text{for pure absorption} \\ 1 & \text{for pure scattering} \end{cases}$$

$1/\kappa_0(c)$ = diffusion length (dimensionless)
(cf. Reference 2, p. 55)

$\lambda(c)$ = linear extrapolation length (dimensionless)
(cf. Reference 2, p. 137)

The parameter $\kappa_0(c)$, determined by c according to Equation (68) on p. 55 of Reference 2,

$$c = \kappa_0 / \tanh^{-1} \kappa_0, \quad (4)$$

is tabulated and plotted in Reference 2 (pp. 60, 63; Figure 16 on p. 56). The parameter $\lambda(c)$ is also tabulated and plotted in Reference 2 (p. 136; Figure 35 on p. 138). Tabular values of $\kappa_0(c)$ and $\lambda(c)$ are given here in Table A-1. (In the computer code, we use more closely-spaced values of κ_0 .)

Since $\kappa_0(c)$ and $\lambda(c)$ are dimensionless, we are free to associate scale lengths with them in some reasonable way. We do so by choosing a suitable effective macroscopic cross-section (equivalent to choosing an effective mean free path). It is by introducing such a scale length that we adapt the results of Case et al.⁽²⁾ to accommodate non-isotropic scattering through use of the transport cross-section. We first discuss the scale length used with $\kappa_0(c)$ and then that with $\lambda(c)$.

We assume that the dimensioned (1/km) diffusion length, K , and $\kappa_0(c)$ are related by the expression

$$K = \kappa_0(c) \sigma \quad (5)$$

where σ is an effective macroscopic cross-section (or inverse mean free path) whose precise form will be established below. We determine σ by the requirement that the diffusion coefficient, D , whose basic definition (Reference 1, pp. 241, 242) is

$$D = \Sigma_a / K^2, \quad (6)$$

approach its anisotropic-scattering asymptotic value of $(3\Sigma_{tr})^{-1}$ (cf. Reference 1 pp. 196, 197) in the limit that Σ_a approaches zero. To determine σ , we first introduce the usual relation between the total, scattering, and absorption cross-sections,

Table A-1. Values of κ_0 and λ^a .

c	κ_0	λ
0.0	1.000000	1.0000
0.1	1.000000	1.0000
0.2	0.999909	0.9993
0.3	0.997414	0.9889
0.4	0.985624	0.9606
0.5	0.957504	0.9201
0.6	0.907332	0.8750
0.7	0.828635	0.8300
0.8	0.710412	0.7871
0.9	0.525430	0.7472
0.92	0.474002	
0.94	0.413976	
0.96	0.340829	
0.98	0.242983	
0.99	0.172511	
1.00	0.000000	0.7104

^aFrom Tables 8 and 23 of Case et al.⁽²⁾

$$\Sigma_a = \Sigma - \Sigma_s, \quad (7)$$

... and then use Equations (3), (5), (6), and (7) to obtain

$$D = \frac{(1-c)\Sigma}{\kappa_0^2} \quad (8)$$

Next, we use the fact (Reference 2, p. 58) that

$$\kappa_0^2 \rightarrow 3(1-c) \text{ as } c \rightarrow 1. \quad (9)$$

Thus, in order that we can have

$$D \rightarrow \frac{1}{3\Sigma_{tr}} \text{ as } c \rightarrow 1, \quad (10)$$

we must have

$$\frac{\Sigma}{\sigma^2} = \frac{1}{\Sigma_{tr}} \quad (11a)$$

or

$$\boxed{\sigma^2 = \Sigma \Sigma_{tr}} \quad (11b)$$

By collating our results thus far, we have, first of all, the general relation from the usual definition of flux,

$$b = D/2 \quad (12)$$

Then, by combining Equations (8) and (11b), we have

$$D = \frac{1-c}{\kappa_o^2 \Sigma_{tr}} \quad (13)$$

and from Equations (5) and (11b) we have

$$K = \kappa_o \sqrt{\Sigma \Sigma_{tr}} \quad (14)$$

We shall now relate σ , given by Equation (11b), and the parameter $\lambda(c)$. But first, we note that the use of the linear extrapolation length $\lambda(c)$ implies that the relation between ϕ and the normal component of the gradient of ϕ shall be that of the result for a semi-infinite medium, where the value of $\lambda(c)$ is determined by relating the diffusion solution to the exact transport solution.

We now assume that the dimensioned (km) linear extrapolation length, d , and $\lambda(c)$ are related by the expression

$$d = \lambda(c)/\sigma \quad . \quad (15)$$

From the definition of the linear extrapolation length, d (cf. Reference 1, pp. 199, 261), and the relation for the photon current, we must have

$$d = b/a \quad . \quad (16)$$

Thus, from Equations (16), (15), and (5) we have

$$a = \frac{b\sigma}{\lambda(c)} = \frac{bK}{\lambda(c)\kappa_0(c)} \quad . \quad (17)$$

To summarize our parameter evaluation, we have:

1. $c = \Sigma_s/\Sigma$, dimensionless, Equation (3)
2. $\kappa_0(c)$, $\lambda(c)$ from tables
3. $D = \frac{1-c}{\kappa_0^2(c)\Sigma_{tr}}$ km, Equation (13)
4. $K = \kappa_0(c)\sqrt{\Sigma\Sigma_{tr}}$, km^{-1} , Equation (14)
5. $b = D/2$, km, Equation (12)
6. $a = \frac{bK}{\kappa_0(c)\lambda(c)}$, dimensionless, Equation (17)

An examination of the values for $\kappa_0(c)$ and $\lambda(c)$ in Table A-1 shows that

$$\frac{bK}{a} = \kappa_0(c)\lambda(c) \leq 1 \quad . \quad (18)$$

Thus, the factor $[(a/bK) - bK/a]$, which occurs in the diffusion solutions to be developed later, has the very important feature of never being negative.

The diffusion parameters for both the "standard" usage and our adopted usage, as well as their values in the limiting cases $c = 0, 1$, are given in Table A-2. That the limiting values are valid for $c \rightarrow 0$ (pure absorption) can be seen by considering the pure absorption solution for a semi-infinite medium, $\exp(-\Sigma_a Z)$. The positive-direction photon current is just $\exp(-\Sigma_a Z)$, the negative-direction current is 0. For $c \rightarrow 1$ (pure scattering), note that for the parameter a , our limiting value differs somewhat from the usual one.

In the code, the variables a, b , and K are known as DALFA, DBETA, and DKAPPA, respectively.

A-2 SINGLE-LAYER PLANAR SLABS

The first problem to be considered is diffusion in a single layer of finite thickness. The sequence of problems is from the simplest to the more complicated. Time-independent problems are treated before time-dependent ones, one-dimensional problems before two-dimensional ones. This sequence has value both from the standpoint of gradually increasing mathematical complexity and from the fact that the simpler solutions can serve as limiting-case checks on the more complicated solutions.

A-2.1 Steady-State Problems

The first category of problems is steady state, hence time-independent. They are of intrinsic value and also serve as checks on later time-dependent problems.

A-2.1.1 Plane Source, Surface Deposition. A slab of thickness L has unit flux per unit area incident on the lower surface ($Z = 0$), no flux incident on the upper surface. The transmitted and reflected fluxes are sought. This yields the equation for ϕ :

$$\partial^2 \phi(Z) / \partial Z^2 - K^2 \phi(Z) = 0 \quad (19)$$

with $K^2 = \Sigma_a / D$ for the standard usage and $K^2 = K_0^2(c) \Sigma \Sigma_{tr}$ for our adopted usage. The boundary conditions are:

$$J_+(0) = 1 \quad (20a)$$

$$J_-(L) = 0 \quad (20b)$$

Table A-2. Summary of Diffusion Parameters.

Parameter and Units	"Standard" Usage	"Standard" Usage Limiting Cases		Our Adopted Usage	Our Usage Limiting Cases	
		c + 0	c + 1		c + 0	c + 1
Σ , km ⁻¹	$\Sigma_a + \Sigma_s$	Σ_a	Σ_s	$\Sigma_a + \Sigma_s$	Σ_a	Σ_s
Σ_{tr} , km ⁻¹	$\Sigma - \bar{\mu}\Sigma_s$	Σ_a	$\Sigma_s(1-\bar{\mu})$	$\Sigma - \bar{\mu}\Sigma_s$	Σ_a	$\Sigma_s(1-\bar{\mu})$
K, km ⁻¹	$\sqrt{\Sigma_a/D}$	∞	0	$\kappa_o(c)\sqrt{\Sigma_{tr}}$	Σ_a	0
D, km	$\Sigma_s/(3\Sigma_{tr})$	0	$1/(3\Sigma_{tr})$	$(1-c)/(\kappa_o^2(c)\Sigma_{tr})$	$1/\Sigma_a$	$1/(3\Sigma_{tr})$
b, km	D/2	0	$1/(6\Sigma_{tr})$	D/2	$1/(2\Sigma_a)$	$1/(6\Sigma_{tr})$
a, unitless	$\Sigma_s/(4\Sigma)$	0	1/4	$bK/(\kappa_o(c)\lambda(c))$	1/2	$1/(6(0.71)\sqrt{1-\bar{\mu}})$
σ , km ⁻¹				$\kappa_o^2(c)$	1	3(1-c)
				$\lambda(c)$	1	0.7104
				$\sqrt{\Sigma_{tr}}$	Σ_a	$\Sigma_s\sqrt{1-\bar{\mu}} \equiv \Sigma_{tr}/\sqrt{1-\bar{\mu}}$

The reflected flux is $J_-(0)$, the transmitted flux is $J_+(L)$. Solution of this problem by elementary methods yields expressions for these quantities.

$$J_+(L) = (\cosh KL + \frac{1}{2} \left(\frac{a}{Kb} + \frac{bK}{a} \right) \sinh KL)^{-1} \quad (21a)$$

$$J_-(0) = \frac{1}{2} \left(\frac{a}{Kb} - \frac{Kb}{a} \right) \sinh KL J_+(L) \quad (21b)$$

There are several comments to be made about this solution. The condition of small absorption shows up here immediately. For $J_-(0)$ to be a positive quantity (as it should) it is necessary that $K < a/b$. This condition is met for the "standard"-usage parameters if the absorption is small. For our adopted parameters (see Section A-1.2), this condition is always met. Secondly, in the limit of no absorption ($K \rightarrow 0$), the sum of the transmitted and reflected fluxes is unity, as it should be. A small effort, and using $b=D/2$, gives the result that

$$J_+(L) + J_-(0) + \int_0^L \Sigma_a \phi(Z) dZ = 1 \quad .$$

Finally, it can easily be shown that $J_+(L) \leq e^{-KL}$, the defect being due to increased loss in multiple collisions.

A-2.1.2 Plane Source, Surface Deposition (alternate treatment). In Section A-2.1.1 the problem of flow through a slab was treated purely in the diffusion approximation. An alternate approach, based on physical considerations, separates the flux into two parts, that which has had no collisions and the remainder. This leads to an equation for the scattered flux with a source term coming from first collisions. The equation to be solved is

$$D \frac{\partial^2 \phi}{\partial Z^2} - \Sigma_a \phi + \Sigma_s e^{-\Sigma Z} = 0 \quad (22)$$

The source term reflects the exponential decrease in the unscattered flux and the fact that only the scattering (not the absorption) contributes to the source. If J_+ is now considered as applying to only the scattered flux, the appropriate boundary conditions are that there be no flux incident on the slab surfaces:

$$J_+(0) = J_-(L) = 0 \quad . \quad (23)$$

The solution of this system follows the usual lines. A particular solution of the inhomogeneous equation is

$$C e^{-\Sigma Z}, \quad C = \Sigma_s D^{-1} (K^2 - \Sigma^2)^{-1}$$

where K^2 is given as before. To this is added a general solution of the homogeneous equation.

$$\phi(Z) = C e^{-\Sigma Z} + A e^{KL} + B e^{-KL} \quad .$$

The values of A and B are determined from the boundary conditions. The quantities of interest, the transmitted flux, $J_+(L)$, and the reflected flux, $J_-(0)$, can then be evaluated. The quantities now include unscattered flux.)

$$J_+(L) = e^{-\Sigma L} \left\{ 1 + C(a+b\Sigma) + \frac{C(a-b\Sigma)}{2} \left(\frac{a}{bK} - \frac{bK}{a} \right) \frac{\sinh KL}{\text{den}} \right\} \quad (24a)$$

$$- \frac{C(a+b\Sigma)}{\text{den}}$$

$$J_-(0) = C \left\{ a-b\Sigma - \frac{e^{-\Sigma L} (a-b\Sigma) + \frac{a+b\Sigma}{2} \left(\frac{a}{bK} - \frac{bK}{a} \right) \sinh KL}{\text{den}} \right\} \quad (24b)$$

$$\text{den} = \cosh KL + \frac{1}{2} \left(\frac{a}{bK} + \frac{bK}{a} \right) \sinh KL \quad . \quad (24c)$$

An interesting check on this solution can be made by letting the deposition occur in a thin layer ($\Sigma \rightarrow \infty$, Σ_s/Σ finite, with a, b, and K unchanged). The resulting limits,

$$J_+(L) \rightarrow \frac{\Sigma_s/\Sigma}{2(\text{den})}$$

$$J_-(0) \rightarrow \frac{\Sigma_s}{2\Sigma} \left\{ 1 + \frac{1}{2} \left(\frac{a}{bK} - \frac{bK}{a} \right) \sinh KL/(\text{den}) \right\} \quad ,$$

can be interpreted (using Equations (21a) and (21b) as a surface source of strength Σ_s/Σ , half entering the medium and being transmitted and reflected according to the prescription of Section A-2.1, and half being emitted outward immediately.

A-2.1.3 External Point Source, Surface Deposition. A slab of thickness L is illuminated by an isotropically emitting point source at a distance h below the slab. The relevant equations are:

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \phi(r, Z)}{\partial r} \right) + \frac{\partial^2 \phi(r, Z)}{\partial Z^2} - K^2 \phi(r, Z) = 0 \quad (25a)$$

inside the slab, with boundary conditions

$$J_+(r, 0) = \frac{Q}{2\pi} \frac{h}{(r^2 + h^2)^{3/2}} \quad (25b)$$

$$J_-(r, L) = 0 \quad (25c)$$

$$\int_0^\infty J_+(r, 0) 2\pi r dr = Q \quad .$$

Thus Q is the total flux into the slab. This is just half of the total flux emitted by the source.

The solution uses standard methods, although not as elementary as the method of Sections A-2.1.1 and A-2.1.2. As a first step, the problem is reduced to a one-dimensional problem by introducing the Hankel transform.⁽³⁾

$$\bar{\phi}(p, Z) = \int_0^\infty \phi(r, Z) J_0(pr) r dr \quad (26a)$$

$$\phi(r, Z) = \int_0^\infty \bar{\phi}(p, Z) J_0(pr) p dp \quad . \quad (26b)$$

Equation (25a) is multiplied by $rJ_0(pr)$ and integrated. The term involving radial derivatives is integrated by parts twice. Assuming $r^2\phi$ and $(\partial\phi/\partial r)r$ being zero at $r = 0$ and $r^{3/2}\phi$ and $r^{3/2}\partial\phi/\partial r$ being zero at $r = \infty$ then yields the relation

$$\frac{\partial^2 \bar{\phi}(p, Z)}{\partial Z^2} - k^2 \bar{\phi}(p, Z) = 0 \quad (27a)$$

with

$$k^2 = p^2 + K^2 .$$

The corresponding boundary conditions are, using Equations 13.51(5) and 3.7(13) of Reference 4,

$$\bar{J}_+(p, 0) = \frac{Q}{2\pi} e^{-ph} \quad (27b)$$

$$\bar{J}_-(p, L) = 0 \quad (27c)$$

$$\bar{J}_+(p, Z) = a \bar{\phi}(p, Z) + b \frac{\partial \bar{\phi}(p, Z)}{\partial Z} . \quad (27d)$$

The solution of these equations follows the pattern of Sections A-2.1.1 and A-2.1.2.

$$\bar{J}_+(p, Z) = \frac{Q}{2\pi} e^{-ph} \frac{\cosh k(L-Z) + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh k(L-Z)}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} \quad (28a)$$

$$\bar{J}_-(p, Z) = \frac{Q}{2\pi} e^{-ph} \frac{\frac{1}{2} \left(\frac{a}{kb} - \frac{kb}{a} \right) \sinh k(L-Z)}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} . \quad (28b)$$

These relations then give the Hankel transforms of the transmitted and reflected fluxes:

$$\boxed{\bar{J}_+(p, L) = \frac{Q}{2\pi} e^{-ph} \left/ \left[\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL \right] \right.} \quad (29a)$$

$$\bar{J}_-(p, 0) = \frac{Q}{2\pi} e^{-ph} \frac{\frac{1}{2} \left(\frac{a}{kb} - \frac{kb}{a} \right) \sinh kL}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} . \quad (29b)$$

The actual transmitted and reflected fluxes are evaluated as integrals using Equation (26b):

$$J_+(r, L) = \frac{Q}{2\pi} \int_0^\infty \frac{e^{-ph} J_0(pr) p}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} dp \quad (30a)$$

$$J_-(r, 0) = \frac{Q}{2\pi} \int_0^\infty \frac{e^{-ph} J_0(pr) p \frac{1}{2} \left(\frac{a}{kb} - \frac{kb}{a} \right) \sinh kL}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} dp \quad (30b)$$

$$k^2 = p^2 + K^2; \quad K^2 = \Sigma_a / D \quad (30c)$$

A number of quantities can be derived from these accumulated results. The total transmitted and reflected fluxes are easily obtained.

$$\int_0^\infty J_+(r, L) 2\pi r dr = 2\pi \bar{J}_+(0, L) = \frac{Q}{\cosh KL + \frac{1}{2} \left(\frac{a}{Kb} + \frac{Kb}{a} \right) \sinh KL} \quad (31a)$$

$$\int_0^\infty J_-(r, 0) 2\pi r dr = 2\pi \bar{J}_-(0, 0) = \frac{Q \frac{1}{2} \left(\frac{a}{Kb} - \frac{Kb}{a} \right) \sinh KL}{\cosh KL + \frac{1}{2} \left(\frac{a}{Kb} + \frac{Kb}{a} \right) \sinh KL} \quad (31b)$$

These are just the results (adjusted for flux Q incident) of Equations (21a) and (21b). A quantity of some interest is the flux from a strip of width x_0 , with one edge going through $r = 0$. Let J_{s+} be the result for the transmitted flux.

$$J_{S+} = \int_0^{x_0} dx \int_{-\infty}^{\infty} dy J_+ \left(\sqrt{x^2+y^2}, L \right) \quad (32a)$$

$$= \frac{Q}{\pi} \int_0^{\infty} dp \left(\frac{p e^{-ph}}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} \right) \times \quad (32b)$$

$$\int_0^{x_0} dx \int_0^{\infty} dy J_0 \left(p \sqrt{x^2+y^2} \right).$$

By Equations 13.47 (5) and 3.4 (6) of Reference 4, the y-integral is

$$\begin{aligned} \int_0^{\infty} dy J_0(p \sqrt{x^2+y^2}) &= \frac{2^{-\frac{1}{2}} \Gamma(\frac{1}{2})}{p^{\frac{1}{2}} x^{\frac{1}{2}}} J_{-\frac{1}{2}}(px) \\ &= \sqrt{\frac{\pi x}{2p}} \sqrt{\frac{2}{\pi p x}} \cos px \\ &= \cos px/p. \end{aligned}$$

The x-integral can be done immediately.

$$J_{S+} = \frac{Q}{\pi} \int_0^{\infty} \frac{\sin px_0}{p} \frac{e^{-ph}}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} dp \quad (33a)$$

The analogous result for the reflected flux is J_{S-} :

$$J_{S-} = \frac{Q}{\pi} \int_0^\infty \frac{\sin p x_0}{p} \frac{e^{-ph} \frac{1}{2} \left(\frac{a}{kb} - \frac{kb}{a} \right) \sinh kL}{\cosh kL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh kL} dp \quad (33b)$$

The limiting case as $x_0 \rightarrow \infty$ can again be compared with previous results. The quantity $\sin p x_0 / p$ behaves as a Dirac delta-function (see Reference 5, p. 29, Equation (47)).

$$\lim_{x_0 \rightarrow \infty} \frac{\sin p x_0}{p} = \pi \delta(p)$$

$$\lim_{x_0 \rightarrow \infty} J_{S+} = \frac{Q}{2} \frac{1}{\cosh KL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh KL}$$

$$\lim_{x_0 \rightarrow \infty} J_{S-} = \frac{Q}{2} \frac{\frac{1}{2} \left(\frac{a}{kb} - \frac{kb}{a} \right) \sinh KL}{\cosh KL + \frac{1}{2} \left(\frac{a}{kb} + \frac{kb}{a} \right) \sinh KL}$$

These are just half the results in (31a) and (31b) as they should be.

A-2.1.4 Internal Point Source. A slab of thickness L is illuminated by an isotropic point source located a distance h ($< L$) above its lower surface ($Z = 0$). The relevant system of equations to be solved are

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \phi(r, Z)}{\partial r} \right) + \frac{\partial^2 \phi(r, Z)}{\partial Z^2} - K^2 \phi(r, Z) + \delta(\vec{r} - \hat{Z}h)/D = 0 \quad (34a)$$

where \hat{Z} is a unit vector in the Z direction, and

$$J_+(r, 0) = J_-(r, L) = 0 \quad (34b)$$

The delta-function part of ϕ can be removed by introducing the infinite medium solution, $G(\vec{r}, \vec{r}_0)$, where $\vec{r}_0 = \hat{Z} h$.

$$G(\vec{r}, \vec{r}_0) = \frac{1}{4\pi D} \frac{e^{-K|\vec{r}-\vec{r}_0|}}{|\vec{r}-\vec{r}_0|} . \quad (35)$$

It is easy to show, by differentiation, that G satisfies Equation (34a) except where $\vec{r}=\vec{r}_0$. To evaluate the behavior at \vec{r}_0 , the usual path of integration over a small sphere, centered at \vec{r}_0 , is taken. Let T be the sphere volume, Σ its surface, $\rho = |\vec{r}-\vec{r}_0|$, and $d\Omega$ an element of solid angle.

$$\begin{aligned} & \int_T (\text{div grad } G - K^2 G) d\tau \\ &= \int_{\Sigma} \text{grad } G \cdot d\sigma - K^2 \int_T G d\tau \\ &= \int \frac{1}{4\pi D} e^{-K\rho} \left(\frac{-K}{\rho} - \frac{1}{\rho^2} \right) \rho^2 d\Omega - K^2 \int \frac{1}{4\pi D} \frac{e^{-K\rho}}{\rho} \rho^2 d\Omega d\rho \\ &\xrightarrow{\rho \rightarrow 0} \frac{-1}{4\pi D} \int d\Omega . \end{aligned}$$

If \vec{r}_0 is an interior point, $\int d\Omega$ is 4π . Hence $\int_T (\text{div grad } G - K^2 G + \frac{1}{D} \delta(\vec{r}-\vec{r}_0)) d\tau = -\frac{1}{D} + \frac{1}{D} = 0$. Using these results the solution for ϕ consists of two parts, G and ψ , where ψ satisfies the homogeneous part of the equation.

$$\phi(r, Z) = G(r, Z) + \psi(r, Z) \quad (36a)$$

$$G(r, Z) = \frac{1}{4\pi D} \frac{e^{-K \sqrt{r^2 + (Z-h)^2}}}{\sqrt{r^2 + (Z-h)^2}} \quad (36b)$$

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \psi(r, Z)}{\partial r} \right) + \frac{\partial^2 \psi(r, Z)}{\partial Z^2} - K^2 \psi(r, Z) = 0 \quad (36c)$$

$$J_{\pm}(r, Z) = a \psi(r, Z) \mp b \frac{\partial \psi(r, Z)}{\partial Z} + a G(r, Z) \mp b \frac{\partial G(r, Z)}{\partial Z} . \quad (36d)$$

As in the previous section, this is solved using Hankel transforms.

$$\bar{\psi}(p, Z) = \int_0^{\infty} \psi(r, Z) J_0(pr) r dr \quad (37a)$$

$$\frac{\partial^2 \bar{\psi}(p, Z)}{\partial Z^2} - k^2 \bar{\psi}(p, Z) = 0 \quad (37b)$$

$$k^2 = K^2 + p^2 . \quad (37c)$$

The transformed boundary conditions are

$$a \bar{\psi}(p, L) + b \left. \frac{\partial \bar{\psi}(p, Z)}{\partial Z} \right|_{Z=L} = -a \bar{G}(p, L) - b \left. \frac{\partial \bar{G}(p, Z)}{\partial Z} \right|_{Z=L} \quad (38a)$$

$$a \bar{\psi}(p, 0) - b \left. \frac{\partial \bar{\psi}(p, Z)}{\partial Z} \right|_{Z=0} = -a \bar{G}(p, 0) + b \left. \frac{\partial \bar{G}(p, Z)}{\partial Z} \right|_{Z=L} \quad (38b)$$

$$\bar{G}(p, Z) = \int_0^{\infty} \frac{1}{4\pi D} \frac{e^{-K \sqrt{r^2 + (Z-h)^2}}}{\sqrt{r^2 + (Z-h)^2}} J_0(pr) r dr .$$

This integral can be evaluated using Equation 13.47(2) of Reference 4 in a manner analogous to the derivation there of Equation 13.47(4):

$$\bar{G}(p, Z) = \frac{e^{-k|Z-h|}}{4\pi D k} \quad (39a)$$

$$\frac{\partial \bar{G}(p, Z)}{\partial Z} = - \frac{e^{-k|Z-h|}}{4\pi D} \frac{Z-h}{|Z-h|} \quad (39b)$$

The solution desired then leads to the result, using $b = D/2$:

$$\begin{aligned} \bar{J}_+(p, L) = & \left\{ \frac{(bk-a)}{16\pi ab^2 k^2 \left(\cosh kL + \frac{1}{2} \left(\frac{a}{bk} + \frac{bk}{a} \right) \sinh kL \right)} \times \right. \\ & \times [(a-bk)(a \sinh kh + bk \cosh kh) \\ & + (a+bk)e^{-kL}(a \sinh k(L-h) + bk \cosh k(L-h))] \Big\} \\ & + e^{-k(L-h)}(a + bk)/8\pi bk \end{aligned} \quad (40a)$$

$$\begin{aligned} \bar{J}_-(p, 0) = & \left\{ \frac{(bk-a)}{16\pi ab^2 k^2 \left(\cosh kL + \frac{1}{2} \left(\frac{a}{bk} + \frac{bk}{a} \right) \sinh kL \right)} \times \right. \\ & \times [(a+bk)(a \sinh kh + bk \cosh kh) e^{-kL} \\ & + (a-bk)(a \sinh k(L-h) + bk \cosh k(L-h))] \Big\} \\ & + e^{-kh}(a + bk)/8\pi bk \end{aligned} \quad (40b)$$

The evaluation of the actual transmitted fluxes is achieved as in Section A-2.1.3. If desired the second term in each of the expressions can be explicitly integrated. Using Equations 3.71(13) and 13.47(2) of Reference 4,

$$\frac{\int_0^\infty e^{-h} \sqrt{p^2 + K^2} J_0(pr) pdp}{\sqrt{p^2 + K^2}} = \frac{e^{-K} \sqrt{h^2 + r^2}}{\sqrt{h^2 + r^2}} \quad (41a)$$

$$\int_0^\infty e^{-h} \sqrt{p^2 + K^2} J_0(pr) pdp = \frac{he^{-K} \sqrt{h^2 + r^2}}{h^2 + r^2} \left(K + \frac{1}{\sqrt{h^2 + r^2}} \right) . \quad (41b)$$

However, from a computational viewpoint, the convergence of the integral over p should be improved by not separating these terms. A cursory examination indicates convergence for J_+ to be as $e^{-k(L-h)}$ if separation is done, as $e^{-k(L-h)}/k$ if no separation is done.

As was done in Section A-2.1.3, the integrals over a strip can be found.

$$J_{S+} = 2 \int_0^\infty \frac{\sin px_0}{p} \bar{J}_+(p, L) dp \quad (42a)$$

$$J_{S-} = 2 \int_0^\infty \frac{\sin px_0}{p} \bar{J}_-(p, 0) dp . \quad (42b)$$

Similarly, for total fluxes out,

$$\int_0^\infty J_+(r, L) 2\pi r dr = 2\pi \bar{J}_+(0, L) \quad (43a)$$

$$\int_0^\infty J_-(r, 0) 2\pi r dr = 2\pi \bar{J}_-(0, 0) . \quad (43b)$$

A-2.2 Time-Dependent Solutions

The only time-dependent solution that is practical from a computational viewpoint is the pure diffusion problem of a plane slab illuminated by a uniform external source. The method of Laplace transforms is used. The relevant transforms are:

$$\tilde{\phi}(z,s) = \int_0^{\infty} \phi(z,t) e^{-st} dt \quad (44a)$$

$$\tilde{J}_{\pm}(z,s) = \int_0^{\infty} J_{\pm}(z,t) e^{-st} dt \quad (44b)$$

$$F(s) = \int_0^{\infty} f(t) e^{-st} dt \quad (44c)$$

where $f(t)$ is the incident flux. For convolution purposes, the case of $f(t) = \delta(t)$, $F(s) = 1$, is of special interest. The equations and boundary conditions satisfied by the transforms are:

$$\frac{\partial^2 \tilde{\phi}(z,s)}{\partial z^2} = (K^2 + \frac{s}{Dv}) \tilde{\phi}(z,s) \quad (45a)$$

$$\tilde{J}_{\pm}(z,s) = \left(a - \frac{3bs}{2v} \right) \tilde{\phi}(z,s) \mp b \frac{\partial \tilde{\phi}(z,s)}{\partial z} \quad (45b)$$

$$\tilde{J}_{-}(L,s) = 0; \quad \tilde{J}_{+}(0,s) = F(s) \quad (45c)$$

Proceeding in a straightforward way,

$$\tilde{J}_{+}(L,s) = F(s)/G(\lambda) \quad (46a)$$

$$\tilde{J}_{-}(0,s) = F(s) \frac{1}{2} \left(\frac{\alpha}{b\lambda} - \frac{b\lambda}{\alpha} \right) \sinh \lambda L / G(\lambda) \quad (46b)$$

$$G(\lambda) = \cosh \lambda L + \frac{1}{2} \left(\frac{\alpha}{b\lambda} - \frac{b\lambda}{\alpha} \right) \sinh \lambda L \quad (46c)$$

where

$$\lambda^2 = K^2 + s/Dv, \quad \alpha = a - \frac{3}{2} \frac{bs}{v}.$$

The relation to the steady-state solution is apparent, since the integral of the time-dependent solutions over time is just the value of the transform for $s=0$.

The actual time-dependent solution is obtained by the usual inverse Laplace transform,

$$J_{\pm}(z,t) = \frac{1}{2\pi i} \int_{-i\infty+\epsilon}^{i\infty+\epsilon} \tilde{J}_{\pm}(z,s) e^{st} ds \quad (47)$$

This is evaluated by contour integration, giving a sum of the residues at the poles of $\tilde{J}_{\pm}(z,s)$. These are at the zeroes of $G(\lambda)$. The exact evaluation of the zeroes is rather intractable, involving a simultaneous evaluation of the real and imaginary parts of λ . For simplicity, an approximate evaluation was used. This approximation neglected the difference between α and a . In terms of the boundary conditions, this is equivalent to neglecting the $\partial\phi/\partial t$ term, compared to ϕ , in the currents, J_{\pm} . Using this approximation, the values of λ are pure imaginary. For the j^{th} root

$$\lambda_j = i\eta_j \quad (48a)$$

$$\tan \eta_j L = 2ab\eta_j (b^2\eta_j^2 - a^2)^{-1}, \quad \eta_j \neq 0, j=1,2,\dots \quad (48b)$$

$$s_j = Dv(-\eta_j^2 - k^2) \quad (48c)$$

For the special case, $f(t) = \delta(t)$, the inverse Laplace transforms then yield:

* Fluxes, for consistency.

$$J_+(L, t) = \sum_{j=1}^{\infty} \frac{e^{-s_j t} D v \eta_j}{-i G'(i \eta_j)} \quad (49a)$$

$$J_-(0, t) = \sum_{j=1}^{\infty} \frac{e^{-s_j t} \frac{L}{2} \left(\frac{a}{b \eta_j} + \frac{b \eta_j}{a} \right) (\sin \eta_j L) D v \eta_j}{-i G'(i \eta_j)} \quad (49b)$$

$$\begin{aligned} -i G'(i \eta_j) &= L \sin \eta_j L - \frac{1}{2} \left(\frac{a}{b \eta_j} - \frac{b \eta_j}{a} \right) \cos \eta_j L \\ &+ \frac{1}{2} \left(\frac{a}{b \eta_j} + \frac{b \eta_j}{a} \right) \sin \eta_j L \end{aligned} \quad (49c)$$

The error in the roots is of the order of D/L times the value of the root. Thus values of the root near zero, which dominate the late-time behavior, are reasonably well determined. The early-time behavior is less well determined. This does not seem a serious deficiency, since the diffusion model is poor for early times in any case, e.g., giving instantaneous transmission independent of thickness.

A-3 STEADY-STATE DIFFUSION FOR CONVEX BODIES

In order to evaluate the reflection and transmission by more general shapes, a numerical method has been developed which is applicable to general convex shapes. The restriction to convex bodies is to prevent one part of the body serving as a source for another part by an exterior path. The equations to be solved are

$$\nabla^2 \phi(\vec{r}) - K^2 \phi(\vec{r}) = 0 \quad (50a)$$

$$J_{\pm}(\vec{r}) = a \phi(\vec{r}) \mp b \text{grad } \phi(\vec{r}) \cdot \hat{n}(\vec{r}) \quad (50b)$$

where, on the surface, $J_+(\vec{r})$ is the outward flux and $J_-(\vec{r})$ is the inward flux, with $\hat{n}(\vec{r})$ the outward unit vector normal to the surface.

The usual Green's function solution of this type of equation involves finding a function, $G(\vec{r}, \vec{r}')$, which satisfies the Equation (50a) except at $\vec{r} = \vec{r}'$, where it has a delta function type singularity. The usual development proceeds as follows. For a volume, T , with surface Σ ,

$$\begin{aligned} & \int_T [G(\vec{r}, \vec{r}')(\nabla^2 \phi(\vec{r}) - K^2 \phi(\vec{r})) - \phi(\vec{r})(\nabla^2 G(\vec{r}, \vec{r}') - K^2 G(\vec{r}, \vec{r}'))] d\tau \\ &= \int_{\Sigma} [G(\vec{r}, \vec{r}') \text{grad } \phi(\vec{r}) \cdot \hat{n} - \phi(\vec{r}) \text{grad } G(\vec{r}, \vec{r}') \cdot \hat{n}] d\sigma. \end{aligned} \quad (51)$$

Since $\phi(\vec{r})$ satisfies Equation (50a) throughout the volume and $G(\vec{r}, \vec{r}')$ satisfies it, except at $\vec{r} = \vec{r}'$, the volume integral can be shrunk to be over a sphere of arbitrarily small radius about \vec{r}' , volume T_s , surface Σ_s .

$$\begin{aligned} & - \int_T \phi(\vec{r}) (\nabla^2 G(\vec{r}, \vec{r}') - K^2 G(\vec{r}, \vec{r}')) d\tau \\ &= - \int_{T_s} \phi(\vec{r}) (\nabla^2 G(\vec{r}, \vec{r}') - K^2 G(\vec{r}, \vec{r}')) d\tau \\ &= - \int_{T_s} [\text{div}(\phi(\vec{r}) \text{grad } G(\vec{r}, \vec{r}')) - \text{grad } \phi(\vec{r}) \text{grad } G(\vec{r}, \vec{r}')] \\ & \quad - K^2 G(\vec{r}, \vec{r}')] d\tau \\ &= - \int_{\Sigma_s} \phi(\vec{r}) \text{grad } G(\vec{r}, \vec{r}') \cdot \hat{n}(\vec{r}) d\sigma \\ & \quad - \int_{T_s} [\text{grad } \phi(\vec{r}) \cdot \text{grad } G(\vec{r}, \vec{r}') + K^2 G(\vec{r}, \vec{r}')] d\tau. \end{aligned}$$

Since $\nabla^2 G - K^2 G$ has an integrable singularity at $\vec{r} = \vec{r}'$, the second integral vanishes as the sphere radius goes to zero. (Typically G is like $|\vec{r} - \vec{r}'|^{-1}$, $\text{grad } G$ like $|\vec{r} - \vec{r}'|^{-2}$ and $d\tau$ like $|\vec{r} - \vec{r}'|^2 d|\vec{r} - \vec{r}'|$.) In the surface integral, since $\phi(\vec{r})$ is continuous, it may be adequately approximated by $\phi(\vec{r}')$ and removed from the integral. Equation (51) can then be written as

$$\begin{aligned}
 & -\phi(\vec{r}') \lim_{\Sigma_S} \int_{\Sigma_S} \text{grad } G(\vec{r}, \vec{r}') \cdot \hat{n}(\vec{r}) \, d\sigma \\
 & = \int_{\Sigma} [G(\vec{r}, \vec{r}') \text{grad} \phi(\vec{r}) \cdot \hat{n}(\vec{r}) - \phi(\vec{r}) \text{grad} G(\vec{r}, \vec{r}') \cdot \hat{n}(\vec{r})] \, d\sigma \quad (52)
 \end{aligned}$$

The limit-integral multiplying $\phi(\vec{r}')$ is here left explicit since its value depends critically on whether the point \vec{r}' is inside the surface or on the surface. In the former case, the sphere radius will be small enough, in the limiting process, that the sphere surrounds the point, \vec{r}' . If \vec{r}' is on the surface this will not happen.

In the usual textbook formulation, $G(\vec{r}, \vec{r}')$ is chosen to match suitable boundary conditions, e.g., if $\hat{n} \cdot \text{grad} \phi$ is given on the surface, $\hat{n} \cdot \text{grad } G$ is zero on the surface; if ϕ is given, G is set to zero. In the method proposed here, following Banaugh,⁽⁶⁾ the function G is taken to be the infinite medium function. The boundary conditions specify a linear relation between ϕ and $\hat{n} \cdot \text{grad} \phi$ on the boundary. Then, if \vec{r}' is taken to be on the surface, Equation (52) is an integral equation for the unknown values of ϕ or $\hat{n} \cdot \text{grad} \phi$, as desired, on the surface.

For the problem under consideration, where $\vec{\rho} = \vec{r} - \vec{r}'$ and $d\omega$ is element of solid angle, choose

$$G(\vec{r}, \vec{r}') = e^{-K|\vec{r} - \vec{r}'|} |\vec{r} - \vec{r}'|^{-1} \quad (53)$$

$$\begin{aligned}
 \lim_{\Sigma_S} \int_{\Sigma_S} \text{grad } G(\vec{r}, \vec{r}') \cdot \hat{n}(\vec{r}) \, d\sigma &= \lim \int_{\Sigma_S} \frac{\partial}{\partial \rho} (e^{-K\rho} \rho^{-1}) \rho^2 \, d\omega \\
 &= \lim \int_{\Sigma_S} e^{-K\rho} (-K\rho^{-1} - \rho^{-2}) \rho^2 \, d\omega \\
 &= - \int_{\Sigma_S} d\omega \quad .
 \end{aligned}$$

Equation (52) then becomes

$$\Omega \phi(\vec{r}') = \int_{\Sigma} [G(\vec{r}, \vec{r}') \text{grad} \phi(\vec{r}) \cdot \hat{n}(\vec{r}) - \phi(\vec{r}) \text{grad} G(\vec{r}, \vec{r}') \cdot \hat{n}(\vec{r})] d\sigma \quad (54)$$

where Ω is the solid angle subtended by the surface at the point \vec{r}' , e.g., 4π if \vec{r}' is inside the surface, 2π if \vec{r}' is on the surface at a point not a "corner".

For the problem at hand, only surface values are of interest and it will be assumed the surface is "smooth." The quantity of actual interest is $J_+(\vec{r})$ with $J_-(\vec{r})$ given. On the surface

$$\phi(\vec{r}) = \frac{1}{2a} (J_+(\vec{r}) + J_-(\vec{r}))$$

$$\text{grad} \phi(\vec{r}) \cdot \hat{n} = \frac{1}{2b} (J_-(\vec{r}) - J_+(\vec{r}))$$

$$\begin{aligned} \frac{\pi}{a} (J_+(\vec{r}') + J_-(\vec{r}')) = & - \int_{\Sigma} \left[\frac{1}{2a} (J_+(\vec{r}) + J_-(\vec{r})) \text{grad} G(\vec{r}, \vec{r}') \cdot \hat{n} \right. \\ & \left. - \frac{1}{2b} (J_-(\vec{r}) - J_+(\vec{r})) G(\vec{r}, \vec{r}') \right] d\sigma \end{aligned}$$

$$\begin{aligned} J_+(\vec{r}') = & - J_-(\vec{r}') - \int_{\Sigma} J_-(\vec{r}) \left[\frac{1}{2\pi} \text{grad} G(\vec{r}, \vec{r}') \cdot \hat{n} \right. \\ & \left. - \frac{a}{2\pi b} G(\vec{r}, \vec{r}') \right] d\sigma \end{aligned}$$

$$\begin{aligned} & - \int_{\Sigma} J_+(\vec{r}) \left[\frac{1}{2\pi} \text{grad} G(\vec{r}, \vec{r}') \cdot \hat{n} \right. \\ & \left. + \frac{a}{2\pi b} G(\vec{r}, \vec{r}') \right] d\sigma . \end{aligned} \quad (55)$$

The first two terms are, in principle, known, although the actual evaluation of the integral may present some problems. Thus Equation (55) is an integral equation for the values of the emergent flux, J_+ , on the surface.

Computationally, the procedure for solving the equation consists of replacing the integral by a set of algebraic equations. A grid of points, \vec{r}_j , is established, each having an associated region, Σ_j , and a local vector, $\vec{\rho}_j$.

$$\begin{aligned}
 J_+(\vec{r}_j) = & -J_-(\vec{r}_j) - \frac{1}{2\pi} \Sigma_{k \neq j} \int_{\Sigma_k} J_-(\vec{r}_k + \vec{\rho}_k) \left[\text{grad}_{\rho_k} G(\vec{r}_k + \vec{\rho}_k, \vec{r}_j) \cdot \hat{n} \right. \\
 & \left. - \frac{a}{b} G(\vec{r}_k + \vec{\rho}_k, \vec{r}_j) \right] d\sigma_k \\
 & - \frac{1}{2\pi} \Sigma_{k \neq j} \int_{\Sigma_k} J_+(\vec{r}_k + \vec{\rho}_k) \left[\text{grad}_{\rho_k} G(\vec{r}_k + \vec{\rho}_k, \vec{r}_j) \cdot \hat{n} \right. \\
 & \left. + \frac{a}{b} G(\vec{r}_k + \vec{\rho}_k, \vec{r}_j) \right] d\sigma_k \\
 & - \frac{1}{2\pi} \int_{\Sigma_j} J_-(\vec{r}_j + \vec{\rho}_j) \left[\text{grad}_{\rho_j} G(\vec{r}_j + \vec{\rho}_j, \vec{r}_j) \cdot \hat{n} - \frac{a}{b} G(\vec{r}_j + \vec{\rho}_j, \vec{r}_j) \right] d\sigma_j \\
 & - \frac{1}{2\pi} \int_{\Sigma_j} J_+(\vec{r}_j + \vec{\rho}_j) \left[\text{grad}_{\rho_j} G(\vec{r}_j + \vec{\rho}_j, \vec{r}_j) \cdot \hat{n} + \frac{a}{b} G(\vec{r}_j + \vec{\rho}_j, \vec{r}_j) \right] d\sigma_j .
 \end{aligned}
 \tag{56}$$

(grad_{ρ_j} means a gradient with respect to ρ_j coordinates).

The first term is known. In the sums, $k \neq j$, the integrals may be replaced by suitable averages times the area, Σ_k . Only the last two terms require special care because of the singularity of the function G and its gradient. A demonstration that these integrals are finite and an evaluation, neglecting variation in the J 's over the area, is straightforward.

$$\begin{aligned}
\int_{\Sigma_j} G(\vec{r}_j + \vec{\rho}_j, \vec{r}_j) d\sigma &= \int_{\Sigma_j} (e^{-K\rho_j} \rho_j^{-1}) \rho_j d\rho_j d\theta \\
&= \int_{\Sigma_j} e^{-K\rho_j} d\rho_j d\theta \\
&\approx 2\pi \tilde{\rho}_j \\
&\approx 2\pi \sqrt{\frac{\Sigma_j}{\pi}} \quad (\text{where } \pi \rho_j^2 = \Sigma_j) \\
&\approx 2 \sqrt{\pi \Sigma_j} \quad (57)
\end{aligned}$$

$$\begin{aligned}
\int_{\Sigma_j} \text{grad} \rho_j G(\vec{r}_j + \vec{\rho}_j, \vec{r}_j) \cdot \hat{n} d\sigma &= \int_{\Sigma_j} \frac{\partial}{\partial \rho} \left(\frac{e^{-K\rho}}{\rho} \right) \frac{\vec{\rho} \cdot \hat{n}}{\rho} \rho d\rho d\theta \\
&= \int_{\Sigma_j} e^{-K\rho} \left(\frac{-K}{\rho} - \frac{1}{\rho^2} \right) \frac{\vec{\rho} \cdot \hat{n}}{\rho} \rho d\rho d\theta \\
&= \int_{\Sigma_j} e^{-K\rho} \left(-K - \frac{1}{\rho} \right) \frac{\vec{\rho} \cdot \hat{n}}{\rho} d\rho d\theta \\
\frac{\vec{\rho} \cdot \hat{n}}{\rho} &\approx \frac{\rho}{2R}
\end{aligned}$$

where R is the local radius of curvature.

$$\int_{\Sigma_j} \text{grad} \rho_j G(\vec{r}_j + \vec{\rho}_j, \vec{r}_j) \cdot \hat{n} d\sigma \approx - \int_{\Sigma_j} e^{-K\rho} (K\rho + 1) R^{-1} d\rho d\theta \approx -\frac{1}{R} \sqrt{\pi \Sigma_j} \quad (58)$$

Using these evaluations of the integrals then yields a set of simultaneous linear algebraic equations for the $J_+(\vec{r}_j)$.

An alternate approximate scheme can be developed which does not involve the solution of simultaneous equations, thus avoiding time consuming procedures (in the case of many points). It can best be expressed by reverting to Equation (55). Let $S(\vec{r}')$ denote the known first two terms on the right side and $G_+(\vec{r}, \vec{r}')$ the multiplier of J_+ in the integral.

$$J_+(\vec{r}') = S(\vec{r}') - \int_{\Sigma} J_+(\vec{r}) G_+(\vec{r}, \vec{r}') d\sigma$$

$$J_+(\vec{r}') \left(1 + \int_{\Sigma} G_+(\vec{r}, \vec{r}') d\sigma \right) = S(\vec{r}') - \int [J_+(\vec{r}) - J_+(\vec{r}')] G_+(\vec{r}, \vec{r}') d\sigma . \quad (59)$$

This form shows some immediate advantage since the integral on the right is less singular at $\vec{r} - \vec{r}'$ due to the zero of $J_+(\vec{r}) - J_+(\vec{r}')$. The approximate procedure solves this in two successive approximations.

$$J_{1,+}(\vec{r}') = S(\vec{r}') / \left[1 + \int_{\Sigma} G_+(\vec{r}, \vec{r}') d\sigma \right] \quad (60a)$$

$$J_{2,+}(\vec{r}') = J_{1,+}(\vec{r}') - \frac{\int_{\Sigma} [J_{1,+}(\vec{r}) - J_{1,+}(\vec{r}')] G_+(\vec{r}, \vec{r}') d\sigma}{1 + \int_{\Sigma} G_+(\vec{r}, \vec{r}') d\sigma} . \quad (60b)$$

The actual numerical implementation of this involves the same replacement of the integrals by sums, but each step is now explicit.

A-4 DIFFUSION THROUGH MULTIPLE SLABS

The problem of transmission by multiple contiguous plane slabs, in the pure diffusion case, can be derived from the single slab case. The case of plane source and point source follow similar development. The procedure consists in using the emerging flux from the top (bottom) of a layer as the entering flux on the bottom (top) of the next higher (lower) layer and deriving a set of relations between the surfaces.

A-4.1 Planar Diffusion Through Multiple Slabs

Assume N contiguous layers with bottoms at $d_1 < d_2 < \dots < d_N$, thickness $L_1, L_2 \dots L_N$. In each layer,

$$\nabla^2 \phi_i(z) - K_i^2 \phi_i(z) = 0 \quad (61a)$$

$$J_{i,\pm}(z) = a_i \phi_i \mp b_i \frac{\partial \phi_i}{\partial z} \quad (61b)$$

The boundary conditions are

$$J_{1,+}(d_1) = f, \quad J_{N,-}(d_N + L_N) = 0 \quad (62a)$$

$$J_{i+1,+}(d_{i+1}) = J_{i,-}(d_i + L_i) \quad i=1,2,\dots,N-1 \quad (62b)$$

The desired quantities are $J_{N,+}(d_N + L_N)$ and $J_{1,-}(d_1)$. In the i th layer

$$\phi_i(z) = A_i e^{K_i z} + B_i e^{-K_i z}$$

$$J_{i,\pm}(z) = A_i e^{K_i z} (a_i \mp b_i K_i) + B_i e^{-K_i z} (a_i \pm b_i K_i)$$

In matrix notation,

$$[J_i(d_i)] = [P_i][\bar{A}_i] \quad (63a)$$

$$[J_i(d_i + L_i)] = [P_i][Q_i][\bar{A}_i] \quad (63b)$$

where

$$[J_i(x)] = \begin{bmatrix} J_{i,+}(x) \\ J_{i,-}(x) \end{bmatrix} \quad (63c)$$

$$[P_i] = \begin{bmatrix} a_i - b_i K_i & a_i + b_i K_i \\ a_i + b_i K_i & a_i - b_i K_i \end{bmatrix} \quad (63d)$$

$$[Q_i] = \begin{bmatrix} e^{K_i L_i} & 0 \\ 0 & e^{-K_i L_i} \end{bmatrix} \quad (63e)$$

$$[\bar{A}_i] = \begin{bmatrix} A_i & e^{K_i d_i} \\ B_i & e^{-K_i d_i} \end{bmatrix} \quad (63f)$$

The problem has been formulated in terms of a different set of matrices:

$$[T_i] = [R_i] [\bar{A}_i] \quad (64a)$$

where

$$[R_i] = \begin{bmatrix} a_i + b_i K_i & a_i - b_i K_i \\ (a_i - b_i K_i) e^{K_i L_i} & (a_i + b_i K_i) e^{-K_i L_i} \end{bmatrix} \quad (64b)$$

$$[T_i] = \begin{bmatrix} J_{i,-}(d_i) \\ J_{i,+}(d_i + L_i) \end{bmatrix} \quad .$$

A recursion relation is easily developed.

$$[T_i] = [R_i] [\bar{A}_i] = [R_i] [P_i]^{-1} [J_i(d_i)] \quad .$$

By the boundary conditions

$$[J_i(d_i)] = [J_{i-1}(d_{i-1} + L_{i-1})] \quad ,$$

$$\begin{aligned} [T_i] &= [R_i][P_i]^{-1} [P_{i-1}] [Q_{i-1}] [R_{i-1}]^{-1} [T_{i-1}] \\ &= [M_i] [T_{i-1}] \end{aligned}$$

$$\begin{aligned} [T_N] &= [M_N] [M_{N-1}] \dots [M_2] [T_1] \\ &= [M] [T_1] \end{aligned}$$

$$[T_N] = [R_N] [Q_N]^{-1} [P_N]^{-1} [J_N(d_N + L_N)]$$

$$\begin{bmatrix} J_{N,-}(d_N) \\ J_{N,+}(d_N + L_N) \end{bmatrix} = [R_N] [Q_N]^{-1} [P_N]^{-1} \begin{bmatrix} J_{N,+}(d_N + L_N) \\ 0 \end{bmatrix}$$

$$[T_1] = [R_1] [P_1]^{-1} [J_1(d_1)]$$

$$\begin{bmatrix} J_{1,-}(d_1) \\ J_{1,+}(d_1 + L_1) \end{bmatrix} = [R_1] [P_1]^{-1} \begin{bmatrix} f \\ J_{1,-}(d_1) \end{bmatrix} .$$

Defining

$$\hat{D}_i = \cosh K_i L_i - \frac{1}{2} \left(\frac{a_i}{b_i K_i} + \frac{b_i K_i}{a_i} \right) \sinh K_i L_i$$

$$\lambda_i = \frac{1}{2} \left(\frac{a_i}{b_i K_i} - \frac{b_i K_i}{a_i} \right) \sinh K_i L_i$$

$$[\hat{M}_i] = [M_i] / \hat{D}_{i-1} = \begin{bmatrix} 1 & -\lambda_{i-1} \\ \lambda_{i-1} & \hat{D}_i \hat{D}_{i-1}^{-\lambda_i \lambda_{i-1}} \end{bmatrix}$$

$$[\hat{\mathcal{M}}] = [M_N] [M_{N-1}] \dots [M_2] ,$$

straightforward matrix operations lead to

$$J_{N,+}(d_N+L_N) = \left(\prod_{i=1}^N \hat{D}_i \right) f / \left\{ [1, -\lambda_N] [\hat{\mathcal{M}}] \begin{bmatrix} 1 \\ \lambda_1 \end{bmatrix} \right\} . \quad (65a)$$

A similar expression can be derived for $J_{1,-}(d_1)$,

$$J_{1,-}(d_1) = \frac{f \hat{D}_1 [1, -\lambda_N] [\hat{\mathcal{M}}] \begin{bmatrix} 0 \\ 1 \end{bmatrix}}{[1, -\lambda_N] [\hat{\mathcal{M}}] \begin{bmatrix} 1 \\ \lambda_1 \end{bmatrix}} . \quad (65b)$$

Only Equation (65a) has been introduced into a computer program.

It should be noted that the requirement of contiguous layers is overly restrictive in this one-dimensional case. Actually the requirement is for non-overlapping layers,

$$d_1 \leq d_1 + L_1 \leq d_2 \leq d_2 + L_2 \dots \leq d_N \leq d_N + L_N .$$

A-4.2 Point Source Diffusion Through Multiple Slabs

The slab geometry is the same as in Section A-4.1. It is essential, here, that the slabs be contiguous because of cylindrical divergence. The source is a point source at $d_0 (\leq d_1)$. In the i^{th} region, the equations to be satisfied are

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \phi_i}{\partial r} \right) + \frac{\partial^2 \phi_i}{\partial z^2} - K_i^2 \phi_i = 0 \quad (66a)$$

$$J_{i,+}(r,z) = a_i \phi_i + b_i \frac{\partial \phi_i}{\partial z} \quad (66b)$$

The boundary conditions are that J_+ and J_- are continuous at the boundaries and

$$J_{1,+}(r_1, d_1) = \frac{Q}{2\pi} \frac{d_1 - d_0}{[r^2 + (d_1 - d_0)^2]^{3/2}}$$

$$J_{N,-}(r_1, d_N + L_N) = 0$$

As in Section A-2.1.3, Hankel transforms are used. Then in the i^{th} slab

$$\frac{\partial^2 \bar{\phi}_i(p,z)}{\partial z^2} - k_i^2 \bar{\phi}_i(p,z) = 0 \quad (67a)$$

$$k_i^2 = p^2 + K_i^2 \quad (67b)$$

$$\bar{J}_{i,+}(p,z) = a_i \bar{\phi}_i(p,z) + b_i \frac{\partial \bar{\phi}_i(p,z)}{\partial z} \quad (67c)$$

$\bar{J}_{i,+}(p,z)$ and $\bar{J}_{i,-}(p,z)$ are continuous at the interfaces and

$$\bar{J}_{1,+}(p,d_1) = \frac{Q}{2\pi} e^{-p(d_1-d_0)} = \bar{F}(p) \quad (68d)$$

$$\bar{J}_{N,-}(p,d_N+L_N) = 0 \quad (68e)$$

$$\bar{J}_{L+1,\pm}(p,d_{i+1}) = \bar{J}_{i,\pm}(p,d_i+L_i), \quad i=1,2 \dots N-1 \quad (68f)$$

The functions of interest are $\bar{J}_{N,+}(p,d_N+L_N)$ and $\bar{J}_{1,-}(p,d_1)$. These equations are formally the same as Equations (61) and (62) in Section A-4.1, with K_i replaced by k_i and p appearing throughout as a parameter.

$$\bar{J}_{N,+}(p,d_N+L_N) = \bar{F}(p) \prod_{i=1}^N \hat{D}_i / \left\{ [1, -\lambda_N] [\hat{\mathcal{M}}] \begin{bmatrix} 1 \\ \lambda_1 \end{bmatrix} \right\} \quad (69)$$

with

$$\bar{F}(p) = \frac{Q}{2\pi} e^{-p(d_1-d_0)}$$

$$\hat{D}_i = \cosh k_i L_i - \frac{1}{2} \left(\frac{a_i}{b_i k_i} + \frac{b_i k_i}{a_i} \right) \sinh k_i L_i$$

$$\lambda_i = \frac{1}{2} \left(\frac{a_i}{b_i k_i} - \frac{b_i k_i}{a_i} \right) \sinh k_i L_i$$

$$k_i^2 = K_i^2 + p^2$$

$$[\hat{\mathcal{M}}] = [\hat{M}_N] [\hat{M}_{N-1}] \dots [\hat{M}_2]$$

$$[\hat{M}_i] = \begin{bmatrix} 1 & -\lambda_{i-1} \\ \lambda_i & \hat{D}_i \hat{D}_{i-1} - \lambda_i \lambda_{i-1} \end{bmatrix}.$$

The actual value of the emergent flux must be determined by an inversion of the Hankel transform as in Section A-2.1.3.

$$J_{N,+}(r, d_N + L_N) = \int_0^{\infty} \bar{J}_{N,+}(p, d_N + L_N) J_0(pr) p dp \quad (70)$$

A-4.3 Diffusion Through Overlapping or Non-Contiguous Slabs

The restriction to contiguous layers of Section A-4.2 and to non-overlapping layers of Sections A-4.1 and A-4.2 can be removed in a crude approximation. The recipe proposed consists in fixing the tops of all 14 cloud types and the bottoms of the seven low-altitude cloud types, adjusting the bottoms of the remaining layers (i.e., the mid- and high-altitude cloud types) to give contiguous layers and adjusting the density of each layer to give the original optical thickness.

This procedure is admittedly crude but seems the simplest one that even approximately simulates the actual problem.

A-5 REFERENCES

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APPENDIX B
ROSCOE-IR
NATURAL CLOUD PROGRAM LISTING


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60  CLJ  IDEFIL  PARAMS  S  B2  ROSCUER 55
    CLJ  PT  PARAMS  S  ROSCUER 56
    CLJ  ERAD  PARAMS  S  C  ROSCUER 57
    CLJ  DGTOR  PARAMS  S  D1  ROSCUER 58
    CLJ  RTONG  PARAMS  S  D2  ROSCUER 59
    CLJ  P1,P2  SUB. SCLOUD  S  ROSCUER 60
    CLJ  P3,P4  SUB. SCLOUD  S  ROSCUER 61
    CLJ  SOLLAT  SOLARP  SUB. SCLOUD  S  E  ROSCUER 62
    CLJ  SILLON  SOLARP  SUB. SCLOUD  S  E  ROSCUER 63
    CLJ  NSORCE  SOURCE  SUB. CLOUD1  S  ROSCUER 64
    CLJ  HSOURCE(1) SOURCE  SUB. CLOUD1  R  ROSCUER 65
    CLJ  THETAS(1) SOURCE  SUB. CLOUD1  R  ROSCUER 66
    CLJ  PHS(1) SOURCE  SUB. CLOUD1  R  ROSCUER 67
    CLJ  WKT  --  SUB. SCLOUD  R  F  ROSCUER 68
    CLJ  ISUN  --  SUB. SCLOUD  R  ROSCUER 69
    CLJ  KCLDK  X1111  SUB. CLOUD3  S  ROSCUER 70
    CLJ  CLDLAM  X1111  SUB. CLOUD3  S  ROSCUER 71
    CLJ  UL,VL,WL  --  SUB. SCLOUD  S  ROSCUER 72
    CLJ  A SET BY DATA STATEMENT  ROSCUER 73
    CLJ  B1 INPUT FILE FOR NATURAL CLOUD MODEL  ROSCUER 74
    CLJ  B2 OUTPUT FILE FOR NATURAL CLOUD MODEL  ROSCUER 75
    CLJ  C EARTH RADIUS, KM  ROSCUER 76
    CLJ  D1 DEGREES-TO-RADIANS  ROSCUER 77
    CLJ  D2 RADIANS-TO-DEGREES  ROSCUER 78
    CLJ  E SET BY DATA STATEMENT FOR SIMPLE TEST RUNS WHEN  ROSCUER 79
    CLJ  DUMMY USED FOR SUBROUTINES ATMOSU, SOLORB, ETC.  ROSCUER 80
    CLJ  FOR THE REAL SUBROUTINE ATMOSU, ETC., A NUMBER  ROSCUER 81
    CLJ  OF QUANTITIES MUST BE SET, FOR WHICH SEE PROGRAM  ROSCUER 82
    CLJ  DRIVER FOR SUBROUTINES ATMOSU, ETC.  ROSCUER 83
    CLJ  F YIELD OF ARTIFICIAL SOURCE IN KT, USED TO GET  ROSCUER 84
    CLJ  SOURCE RADIUS, BASED ON FORMULA AND ALTITUDE  ROSCUER 85
    CLJ  SCALING FROM GLASSTONE (ENH).  ROSCUER 86
    CLJ  7 CONTINUE  ROSCUER 87
    C  READ DETECTOR AND SOURCE DATA  ROSCUER 88
    C  10 FORMAT(4E10.3)  ROSCUER 89
    CLJ  READ(IN,10)HD,THEIAD,PHID,PDV  ROSCUER 90
    CLJ  IF( HD.LT.0.0 ) GO TO 99  ROSCUER 91
    CLJ  WRITE(OUT,20) HD,THEIAD,PHID,PDV  ROSCUER 92
    CLJ  20 FORMAT(* DETECTOR LOCATION *4E12.4)  ROSCUER 93
    CLJ  NSORCE = 1  ROSCUER 94
    CLJ  READ(IN,10) HSOURCE(1),THETAS(1),PHIS(1),WKT  ROSCUER 95
    CLJ  CALL ATMOSU(2,HSORCE(1))  ROSCUER 96
    CLJ  HSOURCE(1) = 6.70E-02 * WKT**0.40 * (1.2250E-03/RHD)**0.33333  ROSCUER 97
    CLJ  WRITE(OUT,12) HSOURCE(1),THETAS(1),PHIS(1),WKT,HSORCE(1)  ROSCUER 98
    CLJ  12 FORMAT(*0 SOURCE LOCATION, YIELD(KT), AND RADIUS(KM) =*,  ROSCUER 99
    CLJ  1 5E12.4)  ROSCUER 100
    CLJ  PRAD(IN,14) ISUN  ROSCUER 101
    CLJ  14 FORMAT (CL0)  ROSCUER 102
    CLJ  ROSCUER 103
    CLJ  ROSCUER 104
    CLJ  ROSCUER 105
    CLJ  ROSCUER 106
    CLJ  ROSCUER 107
    CLJ  ROSCUER 108
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    CLJ  ROSCUER 110
    CLJ  ROSCUER 111

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115      WRITE(IOUT,16) ISUN
16      FORMAT (* ISUN = *,I2)
      READ(I4,10) ALAM
      WRITE(IOUT,17) ALAM
17      FORMAT (* ALAM = *,E12.4)
      CALL CLOUDO(MODE)
      IF( MODE .NE. 0) GO TO 40

C
C      COMMENT TO CHECK OUT DETERMINISTIC MODE
C
125      CALL POL TO CT(RE*HD,THETAD,PHID,XD,YD,ZD)
      IPASS = 1
22      CONTINUE
      CALL CLOUD1

C
130      DO 30 K=1,NCLOUD
      KCLDR = 99
      CLDLAM = -99.
      CALL LOS( K )
      DO 30 I=1,64
      IF( HLOS(I,1).EQ.0.0 ) GO TO 33
      UL = ULOS(I,1)
      VL = VLOS(I,1)
      WL = WLOS(I,1)
      CALL CLOUD2(UL,VL,WL)
      CALL CLOUD3(UL,VL,WL,X,ALAM,TCOEF,TEMISS,SINCLD)
      IF( SINCLD ) GO TO 7
      WRITE(6,25) KCLDR(K),TCOEF,ALAM,TEMISS
25      FORMAT (////)
25      FORMAT( * THE TRANSFER COEFFICIENT TO CLOUD NO.*IS* IS *E12.4* FOR
      X A *E6.2 * MICRON WAVELENGTH* /
      X * THE THERMAL EMISSION (RADIANCE) IS *E12.4 )
30      CONTINUE
33      CONTINUE
      IF( (ISUN.EQ.0) .OR. (IPASS.EQ.2) ) GO TO 31
      HSORCE(1) = RSUN*RE
      THETAS(1) = 90. - SOLLAT*RTD
      PHIS(1) = SOLLON*RTD
      IPASS = 2
      GO TO 22
40      CONTINUE

C
C      COMMENT TO CHECK OUT STATISTICAL MODE
C
160      KEEPSUN = ISUN
      ISUN = 0
      MSM = 1 $ DDM(1) = 0.10
      C      GET A LOS
      CALL POL TO CT(RE*HD,THETAD,PHID,XD,YD,ZD)
      CALL POL TO CT(KE*HSORCE(1),THETAS(1),PHIS(1),XS,YS,ZS)
      RR = SQRT((KD-XS)**2 + (VL-YS)**2 + (ZS-ZD)**2 )
      UL = (XS-XD)/RR $ VL = (YS-YD)/RR $ WL = (ZS-ZD)/RR
      WL = SIGN ( AMIN1(ABS(WL*1.01),1.00),WL )
      VL = SIGN ( SQRT(1. - WL**2 - UL**2),VL )
170

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175 C THIS PRESCRIPTION WORKS ONLY FOR A PARTICULAR SET OF INPUTS
C I.E., FOR SOURCE AND DETECTOR AT THETA=90. AND PHI=-90.
C
C INTEGRATE OVER RADIAL DISTRIBUTION ON TOP
C OF CLOUD TO GET TOTAL TRANSMISSION
C
C RSUM = 0.0
C DX = 0.25
C DO 301 I=1,50
C X = DXX*(FLOAT(I)-0.999)
C RR = SQRT( (XD-X)**2 + (ABS(VN)-RE)**2 + ZD**2)
C UL = (X - XD) / RR
C XL = 0.00000001
C VL = SQRT( 1. - UL**2 )
C WRITE(6,777) X
C 777 FORMAT(10X,'ROIST = * E12.4)
C P1 = 0.10 $ P2 = 0.25
C P3 = 0.50 $ P4 = 0.90
C CALL SCLJUD(ALAM,UL,VL,ISUN)
C
C TC10 IS THE TRANSFER COEFFICIENT AT 10 PERCENT, ETC.
C RSUM = RSUM + P1*X*14
C
C WRITE(6,26) P1,P2,P3,P4
C WRITE(6,27) T1,T2,T3,T4
C WRITE(6,29) E1,E2,E3,E4
C 26 FORMAT (* STATISTICAL CLOUDS, P1,P2,P3,P4 = *4F10.2)
C 27 FORMAT (* SOURCE TRANSFER CF T1,T2,T3,T4 = *4E10.3)
C 28 FORMAT (* SUN TRANSFER COEF S1,S2,S3,S4 = *4E10.3)
C 29 FORMAT (* EMISSION E1,E2,E3,E4 = *4E10.3)
C 301 CONTINUE
C RSUM = RSUM*DX
C WRITE(6,111) RSUM,ALAM
C 111 FORMAT (* TOTAL TRANSMISSION FOR LAMDA IS *,E13.5,F10.3)
C
C IF( KEEPSUM.EQ.0 ) GO TO 31
C CALL SCLJUD(ALAM,UL,VL,ISUN)
C WRITE(6,26) P1,P2,P3,P4
C WRITE(6,28) S1,S2,S3,S4
C WRITE(6,29) E1,E2,E3,E4
C 31 CONTINUE
C GO TO 7
C 99 CONTINUE
C CALL EXIT
C END

```

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169 ROSCUER
170 ROSCUER
171 ROSCUER
172 ROSCUER
173 ROSCUER
174 ROSCUER
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211 ROSCUER
212 ROSCUER
213 ROSCUER

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2 ATMOSU
 2 ATMOSX
 4 ATMOSU
 5 ATMOSU
 6 ATMOSU
 7 ATMOSU
 8 ATMOSU
 9 ATMOSU
 10 ATMOSU
 11 ATMOSU

SUBROUTINE ATMOSU(JJ,ZH)
 COMMON/ATMOSUP/ DUM1(4),RHO,TT,DUM2(32)
 THIS IS A DUMMY ROUTINE REQUIRED IF THE CLOUD PACKAGE
 IS EXERCISED AS A STAND-ALONE PROGRAM.
 FF = 288.0-6.50*ZH
 RHO = 1.2250E-03 * EXP(-ZH/9.)
 RETURN
 END

CC
 CC
 CC
 CC

1
 5
 10

[illegible]

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115      DATA XNUMVAR/.815,.809,.871,.958,.967,.952,.922,.733,.750,.842,
116      .850,.846,.858,.938,.955,.962,.937,.830,.784,.793,
117      .830,.805,.840,.955,.968,.957,.931,.796,.712,.817,
118      .783,.846,.894,.956,.963,.945,.898,.705,.797,.852,
119      .817,.839,.875,.951,.965,.951,.913,.756,.776,.826,
120      .815,.809,.871,.958,.967,.952,.922,.733,.750,.842,
121      .799,.825,.895,.959,.965,.948,.916,.646,.788,.858,
122      .783,.838,.901,.958,.964,.947,.934,.641,.799,.859,
123      .831,.779,.851,.958,.968,.954,.929,.757,.712,.838,
124      .855,.861,.878,.918,.963,.964,.941,.850,.834,.779,
125      .975,.979,.980,.984,.988,.977,.945,.963,.968,.973,
126      .975,.979,.980,.984,.988,.977,.945,.963,.968,.973,
127      .975,.979,.980,.984,.988,.977,.945,.963,.968,.973/
128      DATA FOR CLOUD STATISTICS
129      CDATA
130      CDATA
131      CDATA
132      CDATA
133      CDATA
134      CDATA
135      CDATA
136      CDATA
137      CDATA
138      CDATA
139      CDATA
140      CDATA
141      CDATA
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162      CDATA
163      CDATA
164      CDATA
165      CDATA
166      CDATA
167      CDATA
168      CDATA
169      CDATA
170      CDATA
171      CDATA

      THE DRY CLIMATE IS TAKEN FROM THE NASA DATA BASE
      FOR REGION 11 AND IS FOR THE NORTHERN U.S. AND WESTERN EUROPE

      THE MOIST CLIMATE IS TAKEN AS REGION 4 AND IS
      FOR THE SOUTH PACIFIC

      1  DRY  ANNUAL  AVERAGE
      2  DRY  WINTER  AVERAGE  NIGHT
      3  DRY  WINTER  AVERAGE  DAY
      4  DRY  SUMMER  AVERAGE  NIGHT
      5  DRY  SUMMER  AVERAGE  DAY
      6  MOIST ANNUAL  AVERAGE
      7  MOIST WINTER  AVERAGE  NIGHT
      8  MOIST WINTER  AVERAGE  DAY
      9  MOIST SUMMER  AVERAGE  NIGHT
      10 MOIST SUMMER  AVERAGE  DAY
      11 ARRAY FOR USER SUPPLIED DATA

      DATA (CDOVER(I,1),I=1,5) /
      X .235,.150,.070,.201,.343 /
      DATA (CFREQ(I,1),I=1,68) /
      X .046,.046,.046,.102,.006,.005,.005,.005,.005,.005,.005,.005,.005,.005,.005,.005,
      X .293,.768,.212,.019,.055,.055,.055,.055,.055,.055,.055,.055,.055,.055,.055,.055,
      X .008,.008,.009,.164,.260,.542,.377,.091,.038,.038,.038,.038,.038,.038,.038,.038,.038,
      X .010,.000,.276,.012,.010,.010,.012,.104,.266,.415,.435,.150,.010,
      X .010,.010,.336,.155,.010,.030,.197,.023,.010,.010,.023,.017,.158,
      X .448,.423,.128/

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B-11

230	X .094,-.094,-.094,-.128,-.027,-.003,-.001,-.104,-.003,-.003,-.003,-.003,-.282, X .161,-.737,-.249,-.014,-.078,-.078,-.151,-.034,-.004,-.001,-.176,-.005, X .004,-.004,-.005,-.197,-.137,-.436,-.474,-.091,-.051,-.051,-.187,-.041, X .007,-.001,-.225,-.008,-.007,-.007,-.008,-.135,-.220,-.289,-.506,-.206,-.020, X .020,-.020,-.285,-.197,-.007,-.020,-.156,-.031,-.007,-.031,-.025,-.171, X .347,-.456,-.197/ DATA (CCOVER(I,9),I=1,5) / X .197,-.232,-.118,-.256,-.197 / DATA (CFREQ(I,1,9),I=1,68) / X .055,-.055,-.055,-.110,-.022,-.017,-.001,-.074,-.003,-.017,-.017,-.003,-.332, X .240,-.721,-.269,-.010,-.050,-.050,-.145,-.029,-.025,-.001,-.142,-.005, X .025,-.025,-.005,-.248,-.200,-.355,-.533,-.112,-.043,-.043,-.112,-.023, X .039,-.002,-.182,-.008,-.039,-.039,-.008,-.202,-.218,-.213,-.522,-.245,-.031, X .031,-.031,-.154,-.065,-.041,-.011,-.196,-.025,-.041,-.041,-.025,-.089,-.221, X .190,-.456,-.354/ DATA (CCOVER(I,10),I=1,5) / X .057,-.212,-.167,-.360,-.234 / DATA (CFREQ(I,1,10),I=1,68) / X .136,-.136,-.136,-.038,-.016,-.025,-.001,-.067,-.000,-.025,-.025,-.000,-.297, X .098,-.546,-.424,-.030,-.100,-.100,-.100,-.031,-.019,-.048,-.001,-.087,-.001, X .048,-.048,-.001,-.311,-.106,-.227,-.654,-.119,-.065,-.065,-.065,-.052,-.025, X .058,-.000,-.149,-.004,-.058,-.058,-.004,-.229,-.169,-.105,-.569,-.326,-.046, X .046,-.046,-.114,-.073,-.044,-.010,-.181,-.018,-.044,-.044,-.018,-.084,-.232, X .120,-.472,-.408/ DATA (CCOVER(I,11),I=1,5) / 5*0. / DATA (CFREQ(I,1,11),I=1,68) / 68*0. / END	229 230 231 232 233 234 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250 251 252 253 254 255
235		
240		
245		
250		
255		


```

1      FUNCTION CFLOSF(ICC,ANGLE)
2      DIMENSION CFLOST(11,10),ANGT(10)
3
4      COMMENT THE 1TH COL IS THE CLOUD COVERAGE CAT IN 10THS
5      THE 2TH IS ELEVATION ANGLE IN DEGREES
6
7      FUNCTION CFLOSF COMPUTES THE PROBABILITY OF A CLOUD-FREE
8      LINE-UP-SIGHT (CFLOS) AS A FUNCTION OF THE CLOUD-COVERAGE AND
9      ZENITH ANGLE OF THE LOS FROM THE GROUND.
10
11      INPUT PARAMETERS
12      ARGUMENT LIST
13      ICC-1 = CLOUD COVERAGE IN TENTHS, 0(1)10
14      ANGLE = ZENITH ANGLE OF LOS FROM EARTH'S SURFACE, DEGREES
15
16      OUTPUT PARAMETER
17      FUNCTION
18      CFLOSF = PROBABILITY OF CFLOS FOR GIVEN INPUT PARAMETERS
19
20      DEFINITION OF DATA
21      ANGT(1A) = ZENITH ANGLE OF ((1A-1)*10)-DEGREES
22      CFLOST(ICC,1A) = PROBABILITY OF CFLOS FOR CLOUD-COVERAGE
23      OF (ICC-1)-TENTHS AND ZENITH ANGLE OF
24      ((1A-1)*10)-DEGREES
25      IA = 1,10 ROW
26      ICC = 1,11 COLUMN
27
28      THE TABULAR DATA (EXCEPT FOR THE BOTTOM ROW) ARE FROM LUND AND
29      SHANKLIN (LS-73, TABLE 3), A CASE FOR WHICH ALL CLOUD TYPES ARE
30      INCLUDED IN THE DATA SAMPLE. WE OBTAINED THE BOTTOM-ROW VALUES
31      AT 90-DEGREE ZENITH ANGLE BY EXTRAPOLATION.
32
33      DATA ANGT /0.,10.,20.,30.,40.,50.,60.,70.,80.,90. /
34      DATA CFLOST/
35      X / .99, .97, .92, .87, .81, .77, .70, .62, .48, .31, .08
36      X / .99, .97, .92, .87, .81, .77, .69, .61, .47, .31, .08
37      X / .99, .97, .91, .86, .80, .76, .68, .61, .47, .30, .08
38      X / .99, .96, .90, .85, .80, .75, .66, .60, .46, .29, .08
39      X / .99, .96, .90, .85, .78, .73, .64, .58, .45, .29, .08
40      X / .99, .95, .88, .83, .76, .71, .62, .55, .42, .27, .07
41      X / .98, .93, .86, .80, .73, .66, .57, .50, .38, .24, .06
42      X / .98, .90, .83, .75, .67, .59, .50, .42, .33, .21, .05
43      X / .97, .86, .76, .65, .55, .47, .39, .32, .24, .16, .03
44      X / .94, .79, .66, .52, .40, .32, .27, .21, .14, .08, .00
45
46      IF( ANGLE.LT.0.0) .OR. (ANGLE.GT.90.0) WRITE(6,10) ANGLE
47      101 FORMAT (32H0 *** WARNING FROM CFLOSF *** ,5X,8H ANGLE =,F8.3,
48      $ 56H AND IS NOT WITHIN THE TABULAR VALUES OF ZENITH ANGLE.)
49
50      DO 10 I = 2,10
51      IA = I - 1
52      IF(ANGLE .LT. ANGT(1I)) GO TO 20
53      10 CONTINUE
54      IA = 9
55      20 CONTINUE
56      CFLOSF = CFLOST(ICC,IA) + (CFLOST(ICC,IA+1) - CFLOST(ICC,IA))
57      X * ( ANGLE - ANGT(IA)) / (ANGT(IA+1) - ANGT(IA))
58      RETURN
59      END
60

```


115	X	9.6639E-02	1.1830E-01	1.3360E-01	1.3091E-01	1.2179E-01	CLD8DR	115
	X	1.0559E-01	1.2558E-01	1.3851E-01	1.3389E-01	1.2538E-01	CLD8DR	116
	X	9.6630E-02	1.2188E-01	1.4431E-01	1.5333E-01	1.6513E-01	CLD8DR	117
	X	1.0342E-01	1.4198E-01	1.8309E-01	2.1201E-01	2.4983E-01	CLD8DR	118
	X	1.0525E-01	1.5226E-01	2.1115E-01	2.7332E-01	3.8946E-01	CLD8DR	119
120	X	9.7656E-02	1.5791E-01	2.4487E-01	3.5475E-01	5.6659E-01	CLD8DR	120
	C	DATA KPN,XLAM,WZER0/ 420, 2.00, 1.73600E-01/					CLD8DR	121
	C	DATA(RFL2(1,1,4),I=1,45)					CLD8DR	122
	X	8.8371E-02	1.1898E-01	1.6013E-01	2.1793E-01	3.8377E-01	CLD8DR	123
	X	7.6074E-02	1.1333E-01	1.5625E-01	1.8800E-01	2.1734E-01	CLD8DR	124
125	X	8.5090E-02	1.1552E-01	1.4847E-01	1.7389E-01	2.1357E-01	CLD8DR	125
	X	7.3286E-02	9.3107E-02	1.1341E-01	1.2897E-01	1.6150E-01	CLD8DR	126
	X	7.4517E-02	1.0633E-01	1.4107E-01	1.6475E-01	1.8816E-01	CLD8DR	127
	X	7.8939E-02	1.2188E-01	1.7802E-01	2.3682E-01	3.2885E-01	CLD8DR	128
	X	8.9686E-02	1.5592E-01	2.5798E-01	3.9300E-01	5.6094E-01	CLD8DR	129
130	X	9.3558E-02	1.9538E-01	3.8712E-01	7.0346E-01	1.3578E+00	CLD8DR	130
	X	1.0526E-01	2.3634E-01	5.1294E-01	1.0559E+00	2.4709E+00	CLD8DR	131
	C	DATA KPN,XLAM,WZER0/ 425, 2.50, 1.00000E+00/					CLD8DR	132
	C	DATA(RFL2(1,1,1),I=1,45)					CLD8DR	133
	X	5.3727E-02	6.1630E-02	6.4746E-02	5.8192E-02	4.8267E-02	CLD8DR	134
135	X	7.0241E-02	7.9019E-02	8.0958E-02	7.0207E-02	5.4988E-02	CLD8DR	135
	X	7.4191E-02	9.9237E-02	1.1306E-01	9.5938E-02	5.6776E-02	CLD8DR	136
	X	1.0199E-01	1.0267E-01	1.1479E-01	1.5888E-01	4.2624E-01	CLD8DR	137
	X	8.6435E-02	7.1816E-02	7.1367E-02	1.0100E-01	3.6964E-01	CLD8DR	138
140	X	6.6220E-02	6.7968E-02	6.5901E-02	5.7996E-02	5.3084E-02	CLD8DR	139
	X	7.9669E-02	8.3811E-02	8.1954E-02	7.0528E-02	5.9312E-02	CLD8DR	140
	X	8.0562E-02	9.8494E-02	1.0504E-01	8.7339E-02	5.5538E-02	CLD8DR	141
	X	8.4083E-02	8.4396E-02	7.7552E-02	6.0925E-02	4.4109E-02	CLD8DR	142
	C	DATA KPN,XLAM,WZER0/ 425, 2.50, 8.66000E-01/					CLD8DR	143
	C	DATA(RFL2(1,1,2),I=1,45)					CLD8DR	144
145	X	8.2263E-02	8.7706E-02	8.6131E-02	7.3159E-02	5.8628E-02	CLD8DR	145
	X	8.8715E-02	9.2875E-02	9.0141E-02	7.6615E-02	6.3000E-02	CLD8DR	146
	X	7.8992E-02	8.3588E-02	8.4315E-02	7.8537E-02	7.8790E-02	CLD8DR	147
	X	7.9467E-02	8.7295E-02	8.8160E-02	7.6728E-02	6.2545E-02	CLD8DR	148
150	X	7.9952E-02	9.2947E-02	9.7663E-02	8.5611E-02	6.5820E-02	CLD8DR	149
	X	8.6310E-02	9.7049E-02	1.0191E-01	9.5043E-02	8.8214E-02	CLD8DR	150
	X	8.6138E-02	1.0412E-01	1.1298E-01	1.0095E-01	7.7064E-02	CLD8DR	151
	X	1.0002E-01	1.0994E-01	1.1135E-01	9.8033E-02	8.2113E-02	CLD8DR	152
155	X	1.3301E-01	1.2562E-01	1.1543E-01	1.0182E-01	1.0465E-01	CLD8DR	153
	C	DATA KPN,XLAM,WZER0/ 425, 2.50, 5.00000E-01/					CLD8DR	154
	C	DATA(RFL2(1,1,3),I=1,45)					CLD8DR	155
	X	7.7234E-02	9.7073E-02	1.0976E-01	1.0281E-01	8.2614E-02	CLD8DR	156
	X	1.0862E-01	1.1630E-01	1.1863E-01	1.0770E-01	9.7784E-02	CLD8DR	157
	X	9.9455E-02	1.0835E-01	1.1120E-01	1.0304E-01	9.8264E-02	CLD8DR	158
160	X	8.7189E-02	1.0490E-01	1.1519E-01	1.0750E-01	9.1368E-02	CLD8DR	159
	X	1.0139E-01	1.2075E-01	1.3098E-01	1.2027E-01	9.9773E-02	CLD8DR	160
	X	9.5764E-02	1.1661E-01	1.3587E-01	1.4730E-01	1.7458E-01	CLD8DR	161
	X	9.5993E-02	1.3746E-01	1.8236E-01	2.1158E-01	2.3687E-01	CLD8DR	162
	X	1.0420E-01	1.5515E-01	2.2161E-01	2.9586E-01	4.3593E-01	CLD8DR	163
165	X	9.7049E-02	1.6485E-01	2.6470E-01	3.8630E-01	5.8798E-01	CLD8DR	164
	C	DATA KPN,XLAM,WZER0/ 425, 2.50, 1.76000E-01/					CLD8DR	165
	C	DATA(RFL2(1,1,4),I=1,45)					CLD8DR	166
	X	6.6116E-02	8.1417E-02	9.7471E-02	1.1189E-01	1.4927E-01	CLD8DR	167
	X	6.5009E-02	8.2617E-02	9.8767E-02	1.0631E-01	1.1712E-01	CLD8DR	168
	X	6.7225E-02	8.3578E-02	9.9654E-02	1.1100E-01	1.3633E-01	CLD8DR	169
170	X	7.4215E-02	9.1721E-02	1.0756E-01	1.1547E-01	1.3118E-01	CLD8DR	170
	X	8.2809E-02	1.0224E-01	1.2330E-01	1.3935E-01	1.8206E-01	CLD8DR	171

172	X	8.1586E-02	1.1835E-01	1.6309E-01	2.0617E-01	2.7698E-01	CLDRDR
173	X	8.7019E-02	1.4830E-01	2.4356E-01	3.7714E-01	6.5601E-01	CLDRDR
174	X	9.0367E-02	1.9329E-01	3.9618E-01	7.5734E-01	1.5910E+00	CLDRDR
175	X	9.6798E-02	2.3813E-01	5.7311E-01	1.3384E+00	3.7215E+00	CLDRDR
176	X	DATA KPN,XLAM,WZER0/ 425, 2.55, 1.00000E+00					CLDRDR
177	X	DATA(RFL3(I,1),I=1,45)					CLDRDR
178	X	5.3080E-02	5.6633E-02	5.5481E-02	4.6728E-02	3.6680E-02	CLDRDR
179	X	5.1942E-02	5.5347E-02	5.3626E-02	4.3847E-02	3.2184E-02	CLDRDR
180	X	4.2704E-02	4.5964E-02	4.6054E-02	4.0721E-02	3.5398E-02	CLDRDR
181	X	4.1380E-02	4.7951E-02	5.1247E-02	4.7488E-02	4.1724E-02	CLDRDR
182	X	4.9009E-02	5.9867E-02	6.5271E-02	5.7953E-02	4.2994E-02	CLDRDR
183	X	4.6718E-02	5.8984E-02	6.4441E-02	5.4046E-02	3.3602E-02	CLDRDR
184	X	5.1907E-02	5.7727E-02	5.8520E-02	5.0300E-02	3.9182E-02	CLDRDR
185	X	5.3280E-02	5.3948E-02	5.1621E-02	4.4863E-02	4.0610E-02	CLDRDR
186	X	6.6145E-02	6.5463E-02	5.9458E-02	4.6381E-02	3.3653E-02	CLDRDR
187	X	DATA KPN,XLAM,WZER0/ 425, 2.55, 8.66000E-01					CLDRDR
188	X	DATA(RFL3(I,1),I=1,45)					CLDRDR
189	X	5.3116E-02	6.0725E-02	6.2799E-02	5.4263E-02	4.1250E-02	CLDRDR
190	X	6.2341E-02	6.8552E-02	6.8937E-02	5.9144E-02	4.6567E-02	CLDRDR
191	X	6.2054E-02	6.9266E-02	7.0409E-02	6.0571E-02	4.7049E-02	CLDRDR
192	X	5.5733E-02	6.6122E-02	7.0300E-02	6.1344E-02	4.5423E-02	CLDRDR
193	X	7.4886E-02	8.1302E-02	8.1426E-02	7.0738E-02	5.8321E-02	CLDRDR
194	X	7.5930E-02	8.6479E-02	8.8884E-02	7.5988E-02	5.6630E-02	CLDRDR
195	X	7.1444E-02	8.3095E-02	8.8617E-02	8.1038E-02	6.8708E-02	CLDRDR
196	X	7.9813E-02	8.7759E-02	9.1947E-02	8.8896E-02	9.2430E-02	CLDRDR
197	X	6.9786E-02	8.7299E-02	9.9263E-02	9.5180E-02	8.1806E-02	CLDRDR
198	X	DATA KPN,XLAM,WZER0/ 425, 2.55, 5.00000E-01					CLDRDR
199	X	DATA(RFL3(I,1),I=1,45)					CLDRDR
200	X	5.9895E-02	7.1368E-02	7.8590E-02	7.5331E-02	6.9010E-02	CLDRDR
201	X	6.7293E-02	7.4836E-02	7.8167E-02	7.3294E-02	6.9907E-02	CLDRDR
202	X	6.5089E-02	7.7425E-02	8.5385E-02	8.2462E-02	7.7048E-02	CLDRDR
203	X	6.7841E-02	8.1656E-02	9.0735E-02	8.757E-02	8.0476E-02	CLDRDR
204	X	7.9548E-02	9.9686E-02	1.1445E-01	1.1251E-01	1.0724E-01	CLDRDR
205	X	7.6502E-02	1.0476E-01	1.2959E-01	1.3360E-01	1.2054E-01	CLDRDR
206	X	8.1443E-02	1.2205E-01	1.6570E-01	1.8850E-01	1.8977E-01	CLDRDR
207	X	8.3993E-02	1.4186E-01	2.2091E-01	2.9812E-01	3.8109E-01	CLDRDR
208	X	8.7714E-02	1.5825E-01	2.6484E-01	3.8855E-01	5.5270E-01	CLDRDR
209	X	DATA KPN,XLAM,WZER0/ 425, 2.55, 1.73600E-01					CLDRDR
210	X	DATA(RFL3(I,1),I=1,45)					CLDRDR
211	X	5.0543E-02	5.7898E-02	6.4396E-02	6.8505E-02	8.4270E-02	CLDRDR
212	X	5.6872E-02	6.6530E-02	7.4678E-02	7.8390E-02	9.0911E-02	CLDRDR
213	X	5.5087E-02	6.7625E-02	7.8474E-02	8.2760E-02	9.1016E-02	CLDRDR
214	X	5.5371E-02	7.2550E-02	8.8824E-02	9.6674E-02	1.0493E-01	CLDRDR
215	X	5.7212E-02	8.6306E-02	1.1826E-01	1.3643E-01	1.4075E-01	CLDRDR
216	X	6.6218E-02	9.9905E-02	1.4261E-01	1.8530E-01	2.5191E-01	CLDRDR
217	X	7.8893E-02	1.3997E-01	2.3525E-01	3.6084E-01	5.8200E-01	CLDRDR
218	X	9.1536E-02	1.9111E-01	3.8695E-01	7.4777E-01	1.6637E+00	CLDRDR
219	X	8.3974E-02	2.2028E-01	5.7006E-01	1.4547E+00	4.5656E+00	CLDRDR
220	X	DATA KPN,XLAM,WZER0/ 426, 2.65, 1.00000E+00					CLDRDR
221	X	DATA(RFL4(I,1),I=1,45)					CLDRDR
222	X	6.3315E-02	4.0561E-02	2.6889E-02	1.9253E-02	2.0385E-02	CLDRDR
223	X	1.5073E-02	1.8480E-02	2.0599E-02	1.9386E-02	1.6392E-02	CLDRDR
224	X	2.5753E-02	2.5708E-02	2.3832E-02	1.9924E-02	1.6919E-02	CLDRDR
225	X	1.2604E-02	1.8186E-02	2.3653E-02	2.3090E-02	1.8173E-02	CLDRDR
226	X	1.5646E-02	1.8703E-02	2.0181E-02	1.8123E-02	1.4203E-02	CLDRDR
227	X	1.5333E-02	1.8986E-02	2.0746E-02	1.8080E-02	1.2618E-02	CLDRDR
228	X	1.2337E-02	1.6194E-02	1.9009E-02	1.8233E-02	1.4723E-02	CLDRDR

230	C	X	1-5218E-02	1-8083E-02	1-9773E-02	1-8667E-02	1-6569E-02	CLDRDR	229
		X	1-6503E-02	1-8949E-02	1-9788E-02	1-7442E-02	1-3805E-02	CLDRDR	230
		X	DATA RPN,XLAM,WZER0/ 426, 2.65, 8.66000E-01/					CLDRDR	231
		X	DATA(RPL4(I,1,2),I=1,45)					CLDRDR	232
		X	1-9786E-02	1-9867E-02	2-1841E-02	2-7512E-02	5-7734E-02	CLDRDR	233
		X	2-0659E-02	2-1434E-02	2-1508E-02	2-0491E-02	2-2240E-02	CLDRDR	234
235		X	2-9040E-02	2-7928E-02	2-5564E-02	2-1548E-02	1-9449E-02	CLDRDR	235
		X	2-3239E-02	2-8071E-02	3-0224E-02	2-6428E-02	1-9196E-02	CLDRDR	236
		X	4-4608E-02	4-2016E-02	3-8877E-02	2-8621E-02	2-1917E-02	CLDRDR	237
		X	6-3218E-02	5-2735E-02	4-3015E-02	3-4017E-02	3-1970E-02	CLDRDR	238
		X	3-9126E-02	4-9393E-02	5-5157E-02	4-9315E-02	3-5587E-02	CLDRDR	239
240		X	5-4105E-02	5-3592E-02	5-1163E-02	4-6063E-02	4-6607E-02	CLDRDR	240
		X	2-7891E-02	4-1406E-02	5-5037E-02	5-9943E-02	5-5217E-02	CLDRDR	241
		X	DATA RPN,XLAM,WZER0/ 426, 2.65, 5.00000E-01/					CLDRDR	242
		X	DATA(RPL4(I,1,3),I=1,45)					CLDRDR	243
		X	2-0567E-02	2-1964E-02	2-2215E-02	2-0493E-02	1-9857E-02	CLDRDR	244
		X	2-3787E-02	2-5669E-02	2-5258E-02	2-0247E-02	1-3567E-02	CLDRDR	245
245		X	2-4385E-02	2-8598E-02	3-0810E-02	2-8655E-02	2-4735E-02	CLDRDR	246
		X	2-8298E-02	3-4536E-02	3-9053E-02	3-8628E-02	3-6879E-02	CLDRDR	247
		X	3-5004E-02	4-6211E-02	5-5837E-02	5-7652E-02	5-4803E-02	CLDRDR	248
		X	3-7861E-02	5-9642E-02	8-2341E-02	8-9417E-02	7-5610E-02	CLDRDR	249
250		X	3-9138E-02	7-3356E-02	1-1932E-01	1-4985E-01	1-4111E-01	CLDRDR	250
		X	4-3935E-02	9-2955E-02	1-7236E-01	2-5140E-01	2-8556E-01	CLDRDR	251
		X	4-9392E-02	1-0765E-01	2-1186E-01	3-4716E-01	4-9702E-01	CLDRDR	252
		X	DATA RPN,XLAM,WZER0/ 426, 2.65, 1.73600E-01/					CLDRDR	253
		X	DATA(RPL4(I,1,4),I=1,45)					CLDRDR	254
255		X	1-5844E-02	1-8345E-02	1-9749E-02	1-8721E-02	1-7363E-02	CLDRDR	255
		X	1-9145E-02	2-1033E-02	2-1560E-02	1-9591E-02	1-7653E-02	CLDRDR	256
		X	2-2144E-02	2-3309E-02	2-4826E-02	2-7362E-02	4-0892E-02	CLDRDR	257
		X	2-4163E-02	2-9487E-02	3-4828E-02	3-9111E-02	5-0175E-02	CLDRDR	258
		X	2-6133E-02	4-1230E-02	5-7635E-02	6-4740E-02	5-9121E-02	CLDRDR	259
260		X	3-0903E-02	5-6207E-02	9-2149E-02	1-2538E-01	1-4805E-01	CLDRDR	260
		X	3-6622E-02	8-1639E-02	1-6582E-01	2-8536E-01	4-4432E-01	CLDRDR	261
		X	4-1085E-02	1-1829E-01	3-1424E-01	7-2430E-01	1-5853E+00	CLDRDR	262
		X	4-5844E-02	1-5420E-01	5-0390E-01	1-5769E+00	5-7206E+00	CLDRDR	263
265		X	DATA RPN,XLAM,WZER0/ 427, 2.75, 1.00000E+00/					CLDRDR	264
		X	DATA(RPL5(I,1,1),I=1,45)					CLDRDR	265
		X	5-4773E-04	8-6908E-04	1-2643E-03	1-5769E-03	1-8229E-03	CLDRDR	266
		X	6-2783E-04	9-1048E-04	1-2716E-03	1-6691E-03	2-4475E-03	CLDRDR	267
		X	5-7365E-04	9-2491E-04	1-3430E-03	1-6156E-03	1-6811E-03	CLDRDR	268
		X	5-5865E-04	8-6923E-04	1-2520E-03	1-5747E-03	1-9052E-03	CLDRDR	269
270		X	5-2488E-04	8-8420E-04	1-3611E-03	1-7849E-03	2-1415E-03	CLDRDR	270
		X	4-5873E-04	7-4351E-04	1-1143E-03	1-4551E-03	1-8198E-03	CLDRDR	271
		X	6-2050E-04	9-9749E-04	1-4640E-03	1-8273E-03	2-0795E-03	CLDRDR	272
		X	6-6493E-04	9-4753E-04	1-2999E-03	1-6780E-03	2-4237E-03	CLDRDR	273
		X	4-3178E-04	7-7318E-04	1-2855E-03	1-8771E-03	2-6672E-03	CLDRDR	274
275		X	DATA RPN,XLAM,WZER0/ 427, 2.75, 8.66000E-01/					CLDRDR	275
		X	DATA(RPL5(I,1,2),I=1,45)					CLDRDR	276
		X	7-5118E-04	8-1746E-04	8-4178E-04	7-8933E-04	7-7489E-04	CLDRDR	277
		X	4-9333E-04	7-2599E-04	8-1920E-04	5-6336E-04	1-8009E-04	CLDRDR	278
		X	5-6445E-04	8-2179E-04	1-0876E-03	1-2141E-03	1-2153E-03	CLDRDR	279
280		X	7-1208E-04	9-9927E-04	1-3357E-03	1-6462E-03	2-1788E-03	CLDRDR	280
		X	7-1629E-04	1-2076E-03	1-8132E-03	2-2084E-03	2-2788E-03	CLDRDR	281
		X	1-0120E-03	1-5881E-03	2-2526E-03	2-6661E-03	2-7682E-03	CLDRDR	282
		X	9-4973E-04	1-7477E-03	2-9083E-03	4-0415E-03	4-9357E-03	CLDRDR	283
		X	1-0398E-03	2-0536E-03	3-5957E-03	5-0620E-03	5-8012E-03	CLDRDR	284
285		X	1-0902E-03	2-2364E-03	4-1711E-03	6-5639E-03	9-2685E-03	CLDRDR	285

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345	X / 1.4432E-03 , 1.4302E-03 , 1.5076E-03 , 1.8093E-03 , 3.5716E-03 , CLDRDR	343
	X / 1.3499E-03 , 1.8646E-03 , 2.5667E-03 , 3.5513E-03 , 6.2817E-03 , CLDRDR	344
	X / 1.5644E-03 , 1.6991E-03 , 2.8934E-03 , 3.2423E-03 , 3.7992E-03 , CLDRDR	345
	X / 3.3582E-04 , 7.6495E-04 , 1.6042E-03 , 2.9073E-03 , 4.9624E-03 , CLDRDR	346
	X / 1.1218E-03 , 1.4217E-03 , 1.8146E-03 , 2.3751E-03 , 4.1389E-03 , CLDRDR	347
	X / 1.0855E-03 , 2.4392E-03 , 4.9467E-03 , 8.0977E-03 , 1.0875E-02 , CLDRDR	348
350	X / 2.7523E-03 , 5.3205E-03 , 1.0212E-02 , 1.9566E-02 , 4.7256E-02 , CLDRDR	349
	X / 3.1640E-03 , 8.9367E-03 , 2.4474E-02 , 6.3939E-02 , 1.9213E-01 , CLDRDR	350
	X / 3.3338E-03 , 1.2574E-02 , 4.7551E-02 , 1.8285E-01 , 9.2023E-01 , CLDRDR	351
	C DATA KPN,XLAM,WZER0/ 432, 3.20, 1.00000E+00/	352
	C DATA(RPL7(1,1),I=1,45)	353
355	X / 2.2381E-03 , 2.5124E-03 , 2.8035E-03 , 3.1294E-03 , 4.4726E-03 , CLDRDR	354
	X / 2.4909E-03 , 2.6017E-03 , 2.7447E-03 , 2.9844E-03 , 4.3760E-03 , CLDRDR	355
	X / 2.2896E-03 , 2.5921E-03 , 2.9325E-03 , 3.3526E-03 , 4.9532E-03 , CLDRDR	356
	X / 2.2124E-03 , 2.3881E-03 , 2.6135E-03 , 2.9711E-03 , 4.6150E-03 , CLDRDR	357
	X / 2.1736E-03 , 2.3962E-03 , 2.6508E-03 , 2.9872E-03 , 4.4209E-03 , CLDRDR	358
360	X / 2.2319E-03 , 2.3962E-03 , 2.6208E-03 , 3.0954E-03 , 4.7981E-03 , CLDRDR	359
	X / 2.7621E-03 , 2.7398E-03 , 2.8569E-03 , 3.3162E-03 , 6.0492E-03 , CLDRDR	360
	X / 2.3798E-03 , 2.6678E-03 , 3.0376E-03 , 3.6052E-03 , 5.8875E-03 , CLDRDR	361
	X / 2.3686E-03 , 2.5606E-03 , 2.8162E-03 , 3.2388E-03 , 5.1581E-03 , CLDRDR	362
	C DATA KPN,XLAM,WZER0/ 432, 3.20, 8.66000E-01/	363
	C DATA(RPL7(1,2),I=1,45)	364
365	X / 2.5813E-03 , 3.0038E-03 , 3.1291E-03 , 2.6698E-03 , 1.9251E-03 , CLDRDR	365
	X / 2.6401E-03 , 2.7600E-03 , 2.8902E-03 , 3.0721E-03 , 4.2584E-03 , CLDRDR	366
	X / 3.0477E-03 , 2.8996E-03 , 2.8158E-03 , 2.8774E-03 , 4.1238E-03 , CLDRDR	367
	X / 2.3955E-03 , 2.8588E-03 , 3.2771E-03 , 3.5198E-03 , 4.1929E-03 , CLDRDR	368
370	X / 2.0123E-03 , 2.9603E-03 , 3.9775E-03 , 4.5483E-03 , 4.7496E-03 , CLDRDR	369
	X / 2.3615E-03 , 3.3798E-03 , 4.5471E-03 , 5.5008E-03 , 6.7912E-03 , CLDRDR	370
	X / 2.2137E-03 , 3.2347E-03 , 4.4515E-03 , 5.5288E-03 , 7.0603E-03 , CLDRDR	371
	X / 2.3439E-03 , 3.4192E-03 , 4.8860E-03 , 6.7919E-03 , 1.1297E-02 , CLDRDR	372
	X / 2.2418E-03 , 3.5387E-03 , 5.2920E-03 , 7.2229E-03 , 1.0369E-02 , CLDRDR	373
	C DATA KPN,XLAM,WZER0/ 432, 3.20, 5.00000E-01/	374
	C DATA(RPL7(1,3),I=1,45)	375
375	X / 2.4118E-03 , 3.7976E-03 , 5.0827E-03 , 5.0473E-03 , 3.4680E-03 , CLDRDR	376
	X / 2.5424E-03 , 3.5279E-03 , 4.3203E-03 , 4.2175E-03 , 3.2935E-03 , CLDRDR	377
	X / 2.6502E-03 , 3.1842E-03 , 3.6294E-03 , 3.8127E-03 , 4.2968E-03 , CLDRDR	378
	X / 3.0587E-03 , 3.5391E-03 , 4.0700E-03 , 4.6808E-03 , 6.8123E-03 , CLDRDR	379
380	X / 2.9507E-03 , 4.3131E-03 , 5.9667E-03 , 7.5186E-03 , 9.9249E-03 , CLDRDR	380
	X / 3.1184E-03 , 4.9601E-03 , 7.2599E-03 , 9.1735E-03 , 1.0895E-02 , CLDRDR	381
	X / 3.8802E-03 , 6.3366E-03 , 1.0015E-02 , 1.5050E-02 , 2.5831E-02 , CLDRDR	382
	X / 4.8843E-03 , 7.3526E-03 , 1.1325E-02 , 1.8439E-02 , 4.2498E-02 , CLDRDR	383
	X / 4.7470E-03 , 8.9773E-03 , 1.5891E-02 , 2.6479E-02 , 4.8292E-02 , CLDRDR	384
	C DATA KPN,XLAM,WZER0/ 432, 3.20, 1.73600E-01/	385
	C DATA(RPL7(1,4),I=1,45)	386
385	X / 2.6928E-03 , 4.0262E-03 , 5.8235E-03 , 8.0003E-03 , 1.2530E-02 , CLDRDR	387
	X / 3.3211E-03 , 4.2607E-03 , 5.0165E-03 , 5.734E-03 , 4.7737E-03 , CLDRDR	388
	X / 3.3930E-03 , 4.0589E-03 , 4.6547E-03 , 4.9877E-03 , 5.8714E-03 , CLDRDR	389
390	X / 3.9449E-03 , 4.7291E-03 , 5.7623E-03 , 7.3286E-03 , 1.2860E-02 , CLDRDR	390
	X / 4.3951E-03 , 6.7266E-03 , 9.7828E-03 , 1.3060E-02 , 1.8554E-02 , CLDRDR	391
	X / 5.4314E-03 , 8.7131E-03 , 1.3673E-02 , 2.0817E-02 , 3.7117E-02 , CLDRDR	392
	X / 6.8674E-03 , 1.2367E-02 , 2.1316E-02 , 3.4192E-02 , 6.0009E-02 , CLDRDR	393
	X / 8.5311E-03 , 1.7241E-02 , 3.4637E-02 , 6.9626E-02 , 1.7728E-01 , CLDRDR	394
395	X / 8.7021E-03 , 2.0823E-02 , 5.4661E-02 , 1.7301E-01 , 1.0120E+00 , CLDRDR	395
	C DATA KPN,XLAM,WZER0/ 435, 3.50, 1.00000E+00/	396
	C DATA(RPL8(1,1),I=1,45)	397
	X / 3.9995E-02 , 3.8324E-02 , 3.5939E-02 , 3.2725E-02 , 3.5524E-02 , CLDRDR	398
	X / 4.2419E-02 , 4.6002E-02 , 4.5976E-02 , 3.9763E-02 , 3.2545E-02 , CLDRDR	399

400		X	4.5036E-02	4.6258E-02	4.4954E-02	3.9769E-02	3.6812E-02	CLDRDR	400
		X	5.0371E-02	4.4566E-02	3.9107E-02	3.4185E-02	3.7512E-02	CLDRDR	401
		X	5.1055E-02	4.6899E-02	4.1902E-02	3.5924E-02	3.5849E-02	CLDRDR	402
		X	4.3450E-02	4.4222E-02	4.337E-02	3.9980E-02	4.1299E-02	CLDRDR	403
405		X	4.2486E-02	4.3113E-02	4.1873E-02	3.7850E-02	3.7434E-02	CLDRDR	404
		X	4.3339E-02	4.0787E-02	3.7949E-02	3.4960E-02	3.9936E-02	CLDRDR	405
		X	4.5118E-02	4.3892E-02	4.1443E-02	3.7401E-02	3.8976E-02	CLDRDR	406
	C	DATA KPN,XLAM,WZER0/ 435, 3.50, 8.66000E-01/						CLDRDR	407
		DATA(RFL8(I,1,2),I=1,45)						CLDRDR	408
		X / 5.2061E-02	5.8214E-02	5.9052E-02	5.0329E-02	3.8162E-02		CLDRDR	409
410		X	6.2870E-02	6.1438E-02	5.6146E-02	4.5681E-02	3.7177E-02	CLDRDR	410
		X	5.5855E-02	5.3309E-02	4.8929E-02	4.2177E-02	4.0516E-02	CLDRDR	411
		X	4.7769E-02	4.8704E-02	4.7508E-02	4.3096E-02	4.2705E-02	CLDRDR	412
		X	4.8673E-02	5.0254E-02	4.9573E-02	4.5353E-02	4.5076E-02	CLDRDR	413
415		X	3.9856E-02	4.6006E-02	5.0363E-02	5.0417E-02	5.3297E-02	CLDRDR	414
		X	4.0213E-02	4.6819E-02	5.2531E-02	5.5576E-02	6.6054E-02	CLDRDR	415
		X	4.4734E-02	5.0139E-02	5.5470E-02	6.0566E-02	8.1476E-02	CLDRDR	416
		X	3.9976E-02	5.1867E-02	6.3711E-02	7.1337E-02	8.3797E-02	CLDRDR	417
	C	DATA KPN,XLAM,WZER0/ 435, 3.50, 5.00000E-01/						CLDRDR	418
		DATA(RFL8(I,1,3),I=1,45)						CLDRDR	419
420		X / 5.2385E-02	7.1243E-02	9.1024E-02	1.0445E-01	1.2205E-01		CLDRDR	420
		X	5.3326E-02	7.3399E-02	9.1026E-02	9.3612E-02	8.3417E-02	CLDRDR	421
		X	4.4951E-02	5.8311E-02	6.9011E-02	6.9362E-02	6.3389E-02	CLDRDR	422
		X	4.5231E-02	5.3367E-02	6.0240E-02	6.3233E-02	7.2502E-02	CLDRDR	423
425		X	4.5041E-02	5.8263E-02	6.7008E-02	7.3723E-02	8.7425E-02	CLDRDR	424
		X	4.6345E-02	6.1387E-02	7.188E-02	8.8923E-02	1.0859E-01	CLDRDR	425
		X	4.8949E-02	7.4661E-02	1.0795E-01	1.4261E-01	1.9859E-01	CLDRDR	426
		X	5.5234E-02	8.7770E-02	1.3405E-01	1.9208E-01	3.0603E-01	CLDRDR	427
		X	5.3656E-02	9.1525E-02	1.4972E-01	2.2876E-01	3.8529E-01	CLDRDR	428
430		C	DATA KPN,XLAM,WZER0/ 435, 3.50, 1.73600E-01/					CLDRDR	429
		DATA(RFL8(I,1,4),I=1,45)						CLDRDR	430
		X / 3.8284E-02	7.0000E-02	1.1371E-01	1.4914E-01	1.6055E-01		CLDRDR	431
		X	4.3095E-02	6.7699E-02	9.1284E-02	1.2477E-01	1.9609E-01	CLDRDR	432
		X	4.2916E-02	5.4721E-02	6.8268E-02	8.2664E-02	1.1923E-01	CLDRDR	433
435		X	4.1874E-02	5.5292E-02	7.1332E-02	8.1704E-02	9.6526E-02	CLDRDR	434
		X	4.7868E-02	6.5886E-02	8.7022E-02	1.0750E-01	1.4676E-01	CLDRDR	435
		X	5.1965E-02	7.8822E-02	1.1108E-01	1.5579E-01	2.5991E-01	CLDRDR	436
		X	5.6165E-02	9.8673E-02	1.6601E-01	2.6020E-01	4.4713E-01	CLDRDR	437
		X	6.3932E-02	1.3537E-01	2.6853E-01	4.7584E-01	8.4918E-01	CLDRDR	438
440		X	7.3568E-02	1.6248E-01	3.4828E-01	7.1358E-01	1.6881E+00	CLDRDR	439
	C	DATA KPN,XLAM,WZER0/ 440, 4.00, 1.00000E+00/						CLDRDR	440
		DATA(RFL9(I,1,1),I=1,45)						CLDRDR	441
		X / 7.056E-02	6.6629E-02	6.9572E-02	5.9369E-02	4.2621E-02		CLDRDR	442
		X	5.6099E-02	6.4320E-02	6.710E-02	5.9875E-02	4.8514E-02	CLDRDR	443
445		X	6.6702E-02	6.5828E-02	6.3197E-02	5.8241E-02	6.2522E-02	CLDRDR	444
		X	6.9785E-02	7.0618E-02	6.6541E-02	5.5368E-02	4.5332E-02	CLDRDR	445
		X	6.3429E-02	6.8923E-02	6.8352E-02	5.7612E-02	4.4219E-02	CLDRDR	446
		X	5.9453E-02	6.3887E-02	6.4337E-02	5.7915E-02	5.2577E-02	CLDRDR	447
		X	6.3321E-02	6.4344E-02	6.2581E-02	5.6645E-02	5.6098E-02	CLDRDR	448
450		X	7.265E-02	6.8261E-02	6.3393E-02	5.6645E-02	6.1000E-02	CLDRDR	449
		X	7.5859E-02	8.9348E-02	9.0412E-02	7.6420E-02	5.6797E-02	CLDRDR	450
	C	DATA KPN,XLAM,WZER0/ 440, 4.00, 8.66000E-01/						CLDRDR	451
		DATA(RFL9(I,1,2),I=1,45)						CLDRDR	452
		X / 6.9259E-02	7.5671E-02	7.7308E-02	7.0302E-02	6.3925E-02		CLDRDR	453
455		X	7.1106E-02	8.3547E-02	8.7641E-02	7.4920E-02	5.3569E-02	CLDRDR	454
		X	8.1744E-02	8.2238E-02	7.8765E-02	6.9493E-02	6.5715E-02	CLDRDR	455
		X	7.4577E-02	7.7389E-02	7.5623E-02	6.6669E-02	6.0389E-02	CLDRDR	456

460 X 7.6929E-02 , 8.1116E-02 , 8.0645E-02 , 7.2508E-02 , 6.7312E-02 , CLD8DR 457
 X 7.5559E-02 , 7.9429E-02 , 7.9236E-02 , 7.2368E-02 , 6.9963E-02 , CLD8DR 458
 X 7.1461E-02 , 8.1150E-02 , 9.0703E-02 , 8.8513E-02 , 8.7244E-02 , CLD8DR 459
 X 6.8598E-02 , 8.5133E-02 , 9.7502E-02 , 9.6936E-02 , 9.1597E-02 , CLD8DR 460
 X 7.3721E-02 , 8.9882E-02 , 1.0252E-01 , 1.9418E-01 , 1.0605E-01/ CLD8DR 461
 DATA KPM, KLAM, WZER0/ 440, 4.00, 5.00000E-01/ CLD8DR 462
 DATA(RFL9(I,1,3),I=1,45) CLD8DR 463
 X / 8.0588E-02 , 9.1765E-02 , 1.0024E-01 , 1.0231E-01 , 1.1516E-01, CLD8DR 464
 X 7.8142E-02 , 9.4849E-02 , 1.0484E-01 , 9.8078E-02 , 8.2858E-02, CLD8DR 465
 X 7.7449E-02 , 8.8103E-02 , 9.2628E-02 , 8.4778E-02 , 7.4174E-02, CLD8DR 466
 X 7.4176E-02 , 8.6320E-02 , 9.4180E-02 , 9.1932E-02 , 9.0656E-02, CLD8DR 467
 X 8.5939E-02 , 1.0204E-01 , 1.1336E-01 , 1.1227E-01 , 1.1150E-01, CLD8DR 468
 X 8.7706E-02 , 1.0866E-01 , 1.2783E-01 , 1.3783E-01 , 1.5769E-01, CLD8DR 469
 X 8.9221E-02 , 1.1780E-01 , 1.6014E-01 , 1.9014E-01 , 2.1724E-01, CLD8DR 470
 X 9.9521E-02 , 1.4557E-01 , 2.0498E-01 , 2.7162E-01 , 4.0271E-01, CLD8DR 471
 X 9.2745E-02 , 1.5082E-01 , 2.3497E-01 , 3.4132E-01 , 5.4450E-01/ CLD8DR 472
 DATA KPM, KLAM, WZER0/ 440, 4.00, 1.73600E-01/ CLD8DR 473
 DATA(RFL9(I,1,4),I=1,45) CLD8DR 474
 X / 7.1144E-02 , 9.1484E-02 , 1.1183E-01 , 1.2556E-01 , 1.5023E-01, CLD8DR 475
 X 6.5636E-02 , 8.7610E-02 , 1.1128E-01 , 1.3009E-01 , 1.6269E-01, CLD8DR 476
 X 6.3826E-02 , 7.9407E-02 , 9.4066E-02 , 1.0268E-01 , 1.2020E-01, CLD8DR 477
 X 6.0787E-02 , 7.8909E-02 , 9.6056E-02 , 1.0465E-01 , 1.1526E-01, CLD8DR 478
 X 6.7155E-02 , 9.3466E-02 , 1.2242E-01 , 1.4449E-01 , 1.7479E-01, CLD8DR 479
 X 7.4152E-02 , 1.0687E-01 , 1.4944E-01 , 1.9961E-01 , 3.0746E-01, CLD8DR 480
 X 8.9782E-02 , 1.4624E-01 , 2.3114E-01 , 3.4908E-01 , 6.0833E-01, CLD8DR 481
 X 8.9324E-02 , 1.8376E-01 , 3.6226E-01 , 6.6617E-01 , 1.3467E+00, CLD8DR 482
 X 9.6656E-02 , 2.2381E-01 , 5.1271E-01 , 1.1643E+00 , 3.2859E+00/ CLD8DR 483
 DATA KPM, KLAM, WZER0/ 450, 5.00, 1.00000E+00/ CLD8DR 484
 DATA(RFL10(I,1,1),I=1,45) CLD8DR 485
 X / 3.0860E-02 , 3.3706E-02 , 3.4964E-02 , 3.3258E-02 , 3.3592E-02, CLD8DR 486
 X 2.9041E-02 , 3.2556E-02 , 3.4322E-02 , 3.2562E-02 , 3.1579E-02, CLD8DR 487
 X 3.2634E-02 , 3.8256E-02 , 4.0401E-02 , 3.5373E-02 , 2.6824E-02, CLD8DR 488
 X 2.9870E-02 , 3.5884E-02 , 3.8755E-02 , 3.4560E-02 , 2.6475E-02, CLD8DR 489
 X 3.6096E-02 , 3.9507E-02 , 4.0115E-02 , 3.5719E-02 , 3.0851E-02, CLD8DR 490
 X 3.3268E-02 , 3.4079E-02 , 3.3990E-02 , 3.2596E-02 , 3.6534E-02, CLD8DR 491
 X 3.1698E-02 , 3.9824E-02 , 4.4590E-02 , 4.0548E-02 , 3.0629E-02, CLD8DR 492
 X 3.1945E-02 , 3.6592E-02 , 3.8825E-02 , 3.6015E-02 , 3.2214E-02, CLD8DR 493
 X 3.7706E-02 , 3.8799E-02 , 3.8327E-02 , 3.5440E-02 , 3.6277E-02/ CLD8DR 494
 DATA KPM, KLAM, WZER0/ 450, 5.00, 8.66000E-01/ CLD8DR 495
 DATA(RFL10(I,1,2),I=1,45) CLD8DR 496
 X / 2.4429E-02 , 3.1795E-02 , 4.1313E-02 , 4.0358E-02 , 3.1696E-02, CLD8DR 497
 X 3.4698E-02 , 3.9582E-02 , 4.1167E-02 , 3.6316E-02 , 2.9656E-02, CLD8DR 498
 X 3.4683E-02 , 4.1094E-02 , 4.3614E-02 , 3.7961E-02 , 2.7992E-02, CLD8DR 499
 X 3.6829E-02 , 4.2934E-02 , 4.5361E-02 , 4.0192E-02 , 3.1567E-02, CLD8DR 500
 X 3.9340E-02 , 4.5389E-02 , 4.9049E-02 , 4.7334E-02 , 4.5974E-02, CLD8DR 501
 X 3.8716E-02 , 4.4921E-02 , 4.8950E-02 , 4.7880E-02 , 4.7629E-02, CLD8DR 502
 X 3.6380E-02 , 4.9511E-02 , 5.9900E-02 , 5.8573E-02 , 4.7119E-02, CLD8DR 503
 X 4.1265E-02 , 5.1878E-02 , 6.1588E-02 , 6.6314E-02 , 7.4155E-02, CLD8DR 504
 X 3.7312E-02 , 5.1642E-02 , 6.5663E-02 , 7.1850E-02 , 7.3425E-02/ CLD8DR 505
 DATA KPM, KLAM, WZER0/ 450, 5.00, 5.00000E-01/ CLD8DR 506
 DATA(RFL10(I,1,3),I=1,45) CLD8DR 507
 X / 4.0185E-02 , 4.5309E-02 , 4.9320E-02 , 5.0795E-02 , 5.9181E-02, CLD8DR 508
 X 4.2358E-02 , 5.0768E-02 , 5.6769E-02 , 5.6264E-02 , 5.5279E-02, CLD8DR 509
 X 4.4703E-02 , 4.9749E-02 , 5.2001E-02 , 4.8800E-02 , 4.6592E-02, CLD8DR 510
 X 4.1983E-02 , 5.0831E-02 , 5.7154E-02 , 5.4458E-02 , 5.4310E-02, CLD8DR 511
 X 4.5331E-02 , 6.1865E-02 , 7.5921E-02 , 7.8972E-02 , 6.7106E-02, CLD8DR 512
 X 4.5281E-02 , 6.6351E-02 , 8.7983E-02 , 9.7564E-02 , 9.5352E-02, CLD8DR 513


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515      X 5.4955E-02 , 8.3788E-02 , 1.1842E-01 , 1.4651E-01 , 1.7526E-01, CLD9DR
516      X 5.6161E-02 , 9.6111E-02 , 1.5396E-01 , 2.1998E-01 , 3.1559E-01, CLD8DR
517      X 5.6652E-02 , 1.0848E-01 , 1.9164E-01 , 2.9381E-01 , 4.2778E-01, CLD8DR
518      C DATA KPN,XLAM,MZFR0/ 450, 5.00, 1.73600E-01/ CLD9DR
519      X / 3.0171E-02 , 4.0968E-02 , 5.2498E-02 , 6.0945E-02 , 7.3305E-02, CLD8DR
520      X 3.0411E-02 , 4.0016E-02 , 5.0964E-02 , 6.1708E-02 , 8.5349E-02, CLD8DR
521      X 3.1124E-02 , 4.1387E-02 , 5.2687E-02 , 6.2451E-02 , 8.1067E-02, CLD8DR
522      X 3.4009E-02 , 4.6370E-02 , 5.8683E-02 , 6.5175E-02 , 7.0335E-02, CLD8DR
523      X 4.1566E-02 , 5.8808E-02 , 7.8585E-02 , 9.5280E-02 , 1.2007E-01, CLD8DR
524      X 4.3250E-02 , 7.0946E-02 , 1.0915E-01 , 1.5036E-01 , 2.0957E-01, CLD8DR
525      X 5.8935E-02 , 1.0602E-01 , 1.8261E-01 , 2.9294E-01 , 5.1499E-01, CLD8DR
526      X 5.8149E-02 , 1.3646E-01 , 3.0546E-01 , 6.3216E-01 , 1.4125E+00, CLD8DR
527      X 6.0197E-02 , 1.6701E-01 , 4.5542E-01 , 1.2160E+00 , 3.9358E+00/ CLD8DR
528      DO 20 I = 1,4 CLD8DR
529      ITHIN = I CLD8DR
530      IF(CTHIN -CT. TCTHIN(I)) GO TO 30 CLD8DR
531      20 CONTINUE CLD8DR
532      30 DO 40 I = 1,5 CLD8DR
533      ITHOUT = I CLD8DR
534      IF(CTHOUT -CT. TCTHOUT(I)) GO TO 50 CLD8DR
535      40 CONTINUE CLD8DR
536      50 DO 60 I = 1,9 CLD8DR
537      IPHOUT = I CLD8DR
538      IF(CPHOUT -LT. TCPHOUT(I)) GO TO 70 CLD8DR
539      60 CONTINUE CLD8DR
540      70 CONTINUE CLD8DR
541      DO 80 I = 2,10 CLD8DR
542      ILAM = I - 1 CLD8DR
543      IF(ALAM -LT. ALAMT(I)) GO TO 90 CLD8DR
544      80 CONTINUE CLD8DR
545      90 CONTINUE CLD8DR
546      XLAM = (ALAM - ALAMT(ILAM)) / (ALAMT(ILAM+1) - ALAMT(ILAM)) CLD8DR
547      GO TO(110,120,130,140,150,160,170,180,190) ILAM CLD8DR
548      110 CLD8DR = RFL1(ITHOUT,IPHOUT,ITHIN) CLD8DR
549      1 + (RFL2(ITHOUT,IPHOUT,ITHIN) - RFL1(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
550      RETURN CLD8DR
551      120 CLD8DR = RFL2(ITHOUT,IPHOUT,ITHIN) CLD8DR
552      1 + (RFL3(ITHOUT,IPHOUT,ITHIN) - RFL2(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
553      RETURN CLD8DR
554      130 CLD8DR = RFL3(ITHOUT,IPHOUT,ITHIN) CLD8DR
555      1 + (RFL4(ITHOUT,IPHOUT,ITHIN) - RFL3(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
556      RETURN CLD8DR
557      140 CLD8DR = RFL4(ITHOUT,IPHOUT,ITHIN) CLD8DR
558      1 + (RFL5(ITHOUT,IPHOUT,ITHIN) - RFL4(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
559      RETURN CLD8DR
560      150 CLD8DR = RFL5(ITHOUT,IPHOUT,ITHIN) CLD8DR
561      1 + (RFL6(ITHOUT,IPHOUT,ITHIN) - RFL5(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
562      RETURN CLD8DR
563      160 CLD8DR = RFL6(ITHOUT,IPHOUT,ITHIN) CLD8DR
564      1 + (RFL7(ITHOUT,IPHOUT,ITHIN) - RFL6(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
565      RETURN CLD8DR
566      170 CLD8DR = RFL7(ITHOUT,IPHOUT,ITHIN) CLD8DR
567      1 + (RFL8(ITHOUT,IPHOUT,ITHIN) - RFL7(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
568      RETURN CLD8DR
569      180 CLD8DR = RFL8(ITHOUT,IPHOUT,ITHIN) CLD8DR
570      1 + (RFL9(ITHOUT,IPHOUT,ITHIN) - RFL8(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
571      RETURN CLD8DR
572      190 CLD8DR = RFL9(ITHOUT,IPHOUT,ITHIN) CLD8DR
573      1 + (RFL10(ITHOUT,IPHOUT,ITHIN) - RFL9(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD8DR
574      RETURN CLD8DR
575      END CLD8DR

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AD-A083 339

SCIENCE APPLICATIONS INC LA JOLLA CA

F/G 18/3

THE ROSCOE MANUAL. VOLUME 24. NATURAL CLOUDS (PHYSICAL AND OPTI--ETC(U)

JUL 79 R R JOHNSTON, D E STEVENSON, W A ARON

DNA001-76-C-0194

UNCLASSIFIED

SAI-78-604-LJ-5-VOL-24

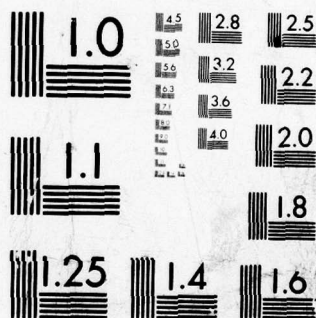
DNA-3964F-24

NL

3 OF 3

AD-A083 339





MICROCOPY RESOLUTION TEST CHART
NATIONAL BUREAU OF STANDARDS-1963-A

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58     CLOGEOM

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13 FORMAT(7A5)

VOCABULARY

XI (10,20) X COORD OF THE I(I=1,10) TH SOURCE IN JTH CLOUD
 ETA (10,20) Y COORD OF THE I(I=1,10) TH SOURCE IN JTH CLOUD
 ZETA(10,20) ZCOORD OF THE I(I=1,10) TH SOURCE IN JTH CLOUD
 RHOS(10,20) DISTANCE FROM THE SOURCE TO THE CLOUD CENTER
 XID(20) RECTANGULAR COORD OF DETECTOR W.R.T. JTH CLOUD
 ETAD(20) RECTANGULAR COORD OF DETECTOR W.R.T. JTH CLOUD
 RHOD(20) DISTANCE OF THE DETECTOR FROM THE JTH CLOUD
 CPHI(4,4,20) DEFINED THE AREA ELEMENTS (1ST QUAD ONLY)
 CTH (4,4,20) AREAS OVER THE WHOLE CLOUD
 CPHIBAR(16,20) AREAS OVER THE WHOLE CLOUD
 CTHBAR (8,20) AREAS OVER THE WHOLE CLOUD
 CRBAR(4,4,20) TO MID PT OF EACH AREA ELEMENT
 CAREA(4,4,20) FIRST OCTANT AREA - ALL OTHERS ARE SYMMETRIC

INPUT PARAMETERS

CLJ CLOUD COMMON
 CLJ
 CLJ
 CLJ
 CLJ
 CLJ
 CLJ

NCLCLOUD = NUMBER OF DETERMINISTIC CLOUDS FOR WHICH THE
 ALTITUDE OF CENTER, SEMI-AXES, AND ORIENTATION
 ARE READ BY SUBROUTINE CLOUD0
 FOR K = 1,NCLCLOUD,


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515      X 5.4956E-02 , 8.3788E-02 , 1.1842E-01 , 1.4651E-01 , 1.7526E-01, CLD9DR
      X 5.6161E-02 , 9.6111E-02 , 1.5396E-01 , 2.1998E-01 , 3.1559E-01, CLD9DR
      X 5.6652E-02 , 1.0848E-01 , 1.9164E-01 , 2.9381E-01 , 4.2778E-01, CLD9DR
      DATA KPH,XLAM,WZFRQ/ 450, 5.00, 1.73600E-01/ CLD9DR
      DATA(RPL10(I),4),I=1,45) CLD9DR
520      X / 3.0171E-02 , 4.0988E-02 , 5.2498E-02 , 6.0945E-02 , 7.3305E-02, CLD9DR
      X 3.0411E-02 , 4.0016E-02 , 5.0964E-02 , 6.1708E-02 , 8.5349E-02, CLD9DR
      X 3.1124E-02 , 4.1387E-02 , 5.2687E-02 , 6.2451E-02 , 8.1067E-02, CLD9DR
      X 3.4009E-02 , 4.6370E-02 , 5.8683E-02 , 6.5175E-02 , 7.0335E-02, CLD9DR
      X 4.1566E-02 , 5.8808E-02 , 7.8585E-02 , 9.5280E-02 , 1.2007E-01, CLD9DR
      X 4.3252E-02 , 7.0946E-02 , 1.0915E-01 , 1.5036E-01 , 2.0957E-01, CLD9DR
      X 5.8935E-02 , 1.0602E-01 , 1.8281E-01 , 2.9294E-01 , 5.1499E-01, CLD9DR
      X 5.8149E-02 , 1.3646E-01 , 3.0546E-01 , 6.3216E-01 , 1.4125E+00, CLD9DR
      X 6.0197E-02 , 1.6701E-01 , 4.5542E-01 , 1.2160E+00 , 3.9358E+00, CLD9DR
      DO 20 I = 1,4 CLD9DR
      ITHIN = I CLD9DR
      IF(CTHIN -GT- TCTHIN(I)) GO TO 30 CLD9DR
530      20 CONTINUE CLD9DR
      30 DO 40 I = 1,5 CLD9DR
      ITHOUT = I CLD9DR
      IF(CTHOUT -GT- TCTHOUT(I)) GO TO 50 CLD9DR
535      40 CONTINUE CLD9DR
      50 DO 60 I = 1,9 CLD9DR
      IPHOUT = I CLD9DR
      IF(CPHOUT -LT- TCPHOUT(I)) GO TO 70 CLD9DR
540      60 CONTINUE CLD9DR
      70 CONTINUE CLD9DR
      DO 80 I = 2,10 CLD9DR
      ILAM = I - 1 CLD9DR
      IF(ILAM -LT- ALAMT(I)) GO TO 90 CLD9DR
545      80 CONTINUE CLD9DR
      90 CONTINUE CLD9DR
      KLAM = (ALAM - ALAMT(ILAM)) / (ALAMT(ILAM+1) - ALAMT(ILAM)) CLD9DR
      GO TO(110,130,140,150,160,170,180,190) ILAM CLD9DR
550      110 CLD9DR = RFL1(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL2(ITHOUT,IPHOUT,ITHIN) - RFL1(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      120 CLD9DR = RFL2(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL3(ITHOUT,IPHOUT,ITHIN) - RFL2(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      130 CLD9DR = RFL3(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL4(ITHOUT,IPHOUT,ITHIN) - RFL3(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      140 CLD9DR = RFL4(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL5(ITHOUT,IPHOUT,ITHIN) - RFL4(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      150 CLD9DR = RFL5(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL6(ITHOUT,IPHOUT,ITHIN) - RFL5(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      160 CLD9DR = RFL6(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL7(ITHOUT,IPHOUT,ITHIN) - RFL6(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      170 CLD9DR = RFL7(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL8(ITHOUT,IPHOUT,ITHIN) - RFL7(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      180 CLD9DR = RFL8(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL9(ITHOUT,IPHOUT,ITHIN) - RFL8(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      190 CLD9DR = RFL9(ITHOUT,IPHOUT,ITHIN) CLD9DR
      1 + (RFL10(ITHOUT,IPHOUT,ITHIN) - RFL9(ITHOUT,IPHOUT,ITHIN)) *XLAM CLD9DR
      RETURN CLD9DR
      END CLD9DR
575

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60 CLJ CLOUDA(K) = LONGEST SEMI-AXIS OF CLOUD-K. ASSUMED TO BE IN CLODEOM
CLJ HORIZONTAL PLANE AND WILL BE IN EAST-WEST CLODEOM
CLJ DIRECTION IF ORIENTATION ANGLE CLOPSI=0.0, KM CLODEOM
CLJ CLOUDB(K) = SEMI-MINOR AXIS IN HORIZONTAL PLANE OF ELLIPSOIDAL CLODEOM
CLJ CLOUD-K, KM CLODEOM
CLJ CLOUDC(K) = SEMI-MINOR AXIS IN VERTICAL DIRECTION OF CLODEOM
CLJ ELLIPSOIDAL CLOUD-K, KM CLODEOM
65 CLJ PARAMS COMMON CLODEOM
CLJ RTD = CONVERSION FACTOR FROM RADIAN TO DEGREES CLODEOM
CLJ DTR = CONVERSION FACTOR FROM DEGREES TO RADIAN CLODEOM
CLJ OUTPUT PARAMETERS CLODEOM
CLJ CORDO COMMON CLODEOM
CLJ CTR(I,K) = POLAR ANGLE IN CLOUD-CENTERED COORDINATES OF A CLODEOM
CLJ BOUNDARY OF THE I-TH POLAR SET OF SURFACE FACETS CLODEOM
CLJ FOR THE PRINCIPAL OCTANT OF THE ELLIPSOIDAL CLODEOM
CLJ CLOUD-K, RADIAN I=1,5 K=1,20 CLODEOM
70 CLJ CPH(J,K) = AZIMUTHAL ANGLE IN CLOUD-CENTERED COORDINATES OF A CLODEOM
CLJ BOUNDARY OF THE J-TH AZIMUTHAL SET OF SURFACE CLODEOM
CLJ FACETS FOR THE PRINCIPAL OCTANT OF THE ELLIPSOIDAL CLODEOM
CLJ CLOUD-K, RADIAN J=1,5 K=1,20 CLODEOM
75 CLJ CTHBAR(I,K) = POLAR ANGLE IN CLOUD-CENTERED COORDINATES OF THE CLODEOM
CLJ CENTER OF THE I-TH POLAR SET OF SURFACE FACETS FOR CLODEOM
CLJ ELLIPSOIDAL CLOUD-K, DEGREE I=1,8 K=1,20 CLODEOM
80 CLJ CPHBAR(J,K) = AZIMUTHAL ANGLE IN CLOUD-CENTERED COORDINATES OF CLODEOM
CLJ THE CENTER OF THE J-TH AZIMUTHAL SET OF SURFACE CLODEOM
CLJ FACETS FOR ELLIPSOIDAL CLOUD-K, DEGREE J=1,6 K=1,20 CLODEOM
85 CLJ CRBAR(I,J,K) = CLOUD-CENTERED RADIAL DISTANCE TO THE CENTER OF CLODEOM
CLJ SURFACE FACET I,J IN PRINCIPAL OCTANT, KM CLODEOM
CLJ I=1,4 J=1,4 K=1,20 CLODEOM
CLJ (RESULTS FOR OTHER OCTANTS ARE OBTAINED BY SYMTY.) CLODEOM
90 CLJ CAREA(I,J,K) = AREA OF SURFACE FACET I,J IN PRINCIPAL OCTANT OF CLODEOM
CLJ ELLIPSOIDAL CLOUD-K, KM**2 I=1,4 J=1,4 K=1,20 CLODEOM
CLJ ASQ(K) = SQUARE OF LENGTH A, THE SEMI-MAJOR AXIS IN CLODEOM
CLJ HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2 CLODEOM
CLJ BSQ(K) = SQUARE OF LENGTH B, THE SEMI-MINOR AXIS IN CLODEOM
CLJ HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2 CLODEOM
95 CLJ CSQ(K) = SQUARE OF LENGTH C, THE SEMI-MINOR AXIS IN CLODEOM
CLJ VERTICAL DIRECTION OF ELLIPSOIDAL CLOUD, KM**2 CLODEOM
CLJ C CLODEOM
100 CLJ COMMON/CLOUD/ MCLOUD, CLODEOM
CLJ 1 HCLD(20),THETCD(20),PHICD(20),CLOUDA(20),CLOUDB(20), CLODEOM
CLJ 2 CLOUDC(20),CLOPSI(20),KCLD(20) CLODEOM
105 CLJ COMMON/CORDO/ XI(1,20),ETA(1,20),ZETA(1,20), CLODEOM
CLJ 1 XID(20),STAD(20),ZETAD(20),CPH(5,20),CTH(5,20) CLODEOM
CLJ 2, ASQ(20),BSQ(20),CSQ(20) CLODEOM
CLJ 2, CPHBAR(16,20),CTHBAR(8,20),CRBAR(4,4,20),CAREA(4,4,20) CLODEOM
CLJ COMMON /PARAMS/ IN,LOUT,PL,PF, DTR,RTD CLODEOM
CLJ MAPPING OF AREAS AND REANS CLODEOM
CLJ FIRST QUAD SYMMETRIC AREA-- ALSO GOOD FOR THE THETA INDEX CLODEOM
CLJ FUNCTION IPRIME, CALLED WITH A NUMBER IN THE FIRST COLUMN, CLODEOM
CLJ SHOULD RETURN THE PAIRED NUMBER IN THE SECOND COLUMN. CLODEOM
110 CLJ 1 - 1 CLODEOM
CLJ 2 - 2 CLODEOM
CLJ 3 - 3 CLODEOM
CLJ 4 - 4 CLODEOM


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175      A21 = SIN(DTR*CPHIBAR(L,K))**2
          A12 = 1.0-A21
          DO 15 J = 1,4
            A31 = COS(DTR*CTHBAR(J,K))**2
            A11 = 1.0-A31
            CPHBAR(J,K) = 1. / SQRT(A11*A12 / ASQ(K)
              X + A11*A21/BSQ(K) + A31/CSQ(K) )
          15 CONTINUE
180      C
          C
          EVALUATE AREA
          SURFAC = 0.
          THETAM = CTH(L,K)
          DO 390 I=1,4
            DTHETA = (CTH(I+1,K)-THETAM)/XINT
            PHIM = CPH(L,K)
            DO 380 J=1,4
              CAREA(I,J,K) = 0.
            DPHI = (CPH(J+1,K)-PHIM)/XINT
            DA = DTHETA * DPHI / 9.0
            DO 360 II=1,MINT
              G(II)=0.0
              KII=II-1
              TII=THETAM+XII*DTHETA
              DO 350 JJ=1,MINTM2,2
                TJJ=JJ-1
                PJJ1=PHIM+YJJ*DPHI
                PJJ2=PJJ1+DPHI
                PJJ3=PJJ2+DPHI
                S(II)=G(II)+DSURF(TII,PJJ1,K)+4.*DSURF(TII,PJJ2,K)+
                  1 DSURF(TII,PJJ3,K)
              350 CONTINUE
              360 CONTINUE
            DO 370 IK=1,MINTM2,2
              CAREA(I,J,K) = CAREA(I,J,K) + DA*(G(II) + 4.*G(II+1) + G(II+2))
            370 CONTINUE
            SURFAC = SURFAC + CAREA(I,J,K)
            PHIM = CPH(J+1,K)
          380 CONTINUE
          THETAM = CTH(I+1,K)
          390 CONTINUE
          1000 RETURN
          END
200
205
210

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CLDGEOM 168
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1  SUBROUTINE CLOUDT(ALA,ANG)
2  COMMON /CONFIG/CTYPL(8),CTYPM(4),CTYPH(5),CFLAG,CL,C2
3  COMMON /CLDFREQ/ KMODEL,CCOVER(5,11),CFREQ(17,4,11)
4  COMMON/CLDWT/IDX,WT(161),TRANS(161),EMISS(161)
5  DIMENSION ALX(20),P(20),N(5)
6  EQUIVALENCE(ALX,P)
7  DIMENSION TYPEL(8),TYPEM(4),TYPEH(5)
8  DIMENSION ICC(5)
9  INTEGER H1,H2,HH,CC,CL,C2
10  INTEGER CFLAG
11
12  SUBROUTINE CLOUDT, FOR GIVEN SOURCE AND DETECTOR LOCATIONS,
13  COMPUTES THREE ARRAYS (TRANS, EMISS, AND WT), EACH WITH IDX
14  MEMBERS (NORMALLY 150). THE TRANS AND EMISS ARRAYS ARE,
15  RESPECTIVELY, (1) THE DISTRIBUTION OF IRRADIANCE-TO-RADIANCE
16  TRANSFER COEFFICIENTS (1/SR) AT THE 12-KM ALTITUDE TRANSFER POINT
17  AND (2) THE DISTRIBUTION OF (ATTENUATED) SPECTRAL RADIANCES
18  (WATTS/(KM**2 SR MICRON)) AT 12-KM ALTITUDE AND DIRECTED TOWARD
19  THE DETECTOR. THE WT ARRAY IS THE SET OF WEIGHTS ASSOCIATED WITH
20  THE SET OF STATISTICAL CLOUD CONFIGURATIONS, INFLUENCED BY
21  CLOUD-COVERAGE FRACTIONS AND CLOUD-FREE LINE-OF-SIGHTS FROM THE
22  DETECTOR.
23
24  INPUT VARIABLES
25  ARGUMENT LIST
26  ALA = WAVELENGTH, MICRONS
27  ANG = ZENITH ANGLE OF THE DETECTOR MEASURED AT THE INTER-
28  SECTION POINT OF THE DETECTOR LOS WITH THE EARTH'S
29  SURFACE, DEGREES
30
31  CLDFREQ COMMON
32  DEFINITIONS OF THE FOLLOWING THREE QUANTITIES ARE IN
33  THE BLOCK DATA ROUTINE. KMODEL, CCOVER(ICC,KMODEL),
34  AND CFREQ(KCLOUD,ICC,KMODEL)
35
36  OUTPUT VARIABLES
37  CLOUDT COMMON
38  IDX = AS AN OUTPUT QUANTITY, IDX IS ONE PLUS THE TOTAL
39  NUMBER OF CLOUD CONFIGURATIONS, WHICH IS 1+159=160
40  FOR KMODEL=1,10. FOR KMODEL=11, THE USER SUPPLIES
41  STATISTICAL CLOUD DATA AND IDX MAY BE DIFFERENT.
42  HOWEVER, DIMENSION STATEMENTS CURRENTLY RESTRICT
43  IDX FROM BEING LARGER THAN 160.
44
45  WT(1) = FOR ANY OF THE 10 LOCATION-SEASON AVERAGED
46  STATISTICAL CLOUD MODELS (KMODEL=1,10), WT(1) IS
47  THE PROBABILITY THAT (A) THE CLOUD-CONFIGURATION
48  SET INDICATED BY THE INDEX I OCCURS AND (B) THE
49  DETECTOR LOS AT ZENITH ANGLE ANG INTERSECTS THE
50  CLOUD-CONFIGURATION SET. THE TOTAL PROBABILITY OF
51  THE DETECTOR LOS INTERSECTING CLOUDS IS SUM(WT(1))
52  (I=1,IDX-1). THE PROBABILITY THAT THE LOS DOES NOT
53  INTERSECT THE CLOUDS BUT SEES THROUGH GAPS IN THE
54  CLOUDS IS WTOLD(IDX). THE PROBABILITY OF THE LOS
55  SEEING THE GROUND FOR A 0.0 CLOUD-COVERAGE FRACTION
56  IS CCOVER(1,KMODEL) IN THE CODE, ALTHOUGH STRICTLY
57  THIS QUANTITY SHOULD BE MULTIPLIED BY CFLOS(0,ANG).
58  THE PROBABILITY OF THE LOS SEEING THE GROUND EITHER
59  WITH OR WITHOUT CLOUDS BEING PRESENT IS WTNEW(IDX)=
60  WTOLD(IDX)*CCOVER(1,KMODEL). THE PROBABILITY OF

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60 CLJ SEEING EITHER CLOUDS OR THE GROUND (WITH OR WITHOUT CLOUDS BEING PRESENT) IS SUM(I=1,IDX-1) +
CLJ WTIME(IDX) = 1.0
CLJ TRANS(I) = THE (ATTENUATED) IRRADIANCE-TO-RADIANCE TRANSFER
CLJ COEFFICIENT AT THE 12-KM ALTITUDE TRANSFER POINT
CLJ FOR CLOUD-CONFIGURATION SET I, 1/SR
CLJ (MORE INFORMATION IS GIVEN IN FUNCTION TRANSF.)
65 CLJ EMISS(I) = THE (ATTENUATED) SPECTRAL RADIANCE AT 12-KM
CLJ ALTITUDE FOR RADIATION EMITTED AT ZENITH ANGLE ANG
CLJ FROM THE HIGHEST CLOUD-TOP IN CLOUD-CONFIGURATION
CLJ SET I, WATTS/(KM**2 SR MICRON)
CLJ
CLJ FOR WT, TRANS, AND EMISS I=1,IDX-1
CLJ
CLJ DATA TYPEL /3HCUL,3HCU2,3HCUL,3HSC,3HST,3HCB1,3HNS,3HCLR /
CLJ DATA TYPEM /3HAC,3HAS1,3HCB2,3HCLR,3HCS,3HCLR /
CLJ DATA TYPEH /3HCB3,3HAS2,3HCI,3HCS,3HCLR /
CLJ DATA L1,L2,M1,M2,H1,H2,C1,C2 /1,7,1,3,1,4,2,5 /
CLJ DATA CTYPL / 3HCUL,3HCU2,3HCUL,3HSC,3HST,3HCB1,3HNS,3HCLR /
CLJ DATA CTYPM / 3HAC,3HAS1,3HCB2,3HCLR,3HCS,3HCLR /
CLJ DATA CTYPH / 3HCB3,3HAS2,3HCI,3HCS,3HCLR /
CLJ DATA ICC / 1,4,6,9,11 /
CLJ DATA CFLAG / 1 /
CLJ
CLJ INPUTS AND OUTPUTS
CLJ ALAM WAVELENGTH IN MICROMETERS
CLJ WT PROBABILITY FN 160 (OR OR FEWER) NUMBERS
85 CLJ TRANS TRANSFER COEF (SR-1)
CLJ EMISS THERMAL EMISSION FROM CLOUD (RADIANCE)
CLJ ANG LINE OF SIGHT EXIT ANGLE
CLJ
CLJ DO 10 I = 1,160
CLJ WT(I) = 0.
CLJ EMISS(I) = 0.
10 CLJ TRANS(I) = 0.0
CLJ
CLJ DO 500 II = C1,C2
CLJ CC = II
CLJ IDX = 0
CLJ CFLOS = CFLOS*(ICC(II), ANG)
CLJ W(CC) = CCOVER(CC,KMODEL)
CLJ WT = 17
CLJ DO 71 J = 1,NT
71 CLJ P(J) = CFREQ(J,CC-1,KMODEL)
CLJ TOTL=ALX(1) + ALX(2) + ALX(3) + ALX(4) + ALX(5) + ALX(6) + ALX(7)
CLJ TOTM = ALX(8) + ALX(9) + ALX(10)
CLJ TOTL = ALX(11) + ALX(12) + ALX(13) + ALX(14)
CLJ IF( TOTL .EQ. 0 ) TOTL = 1.
CLJ IF( TOTM .EQ. 0 ) TOTM = 1.
CLJ IF( TOTL .EQ. 0 ) TOTL = 1.
CLJ IF( TOTM .EQ. 0 ) TOTM = 1.
CLJ 1 LAYER
CLJ MM = 4
CLJ HH = 5
110 CLJ DO 101 LL = L1,L2
CLJ IF(CFLAG.NE. 0 .AND. CTYPL(LL) .NE. TYPEL(LL) ) GO TO 101
CLJ IF(CFLAG.NE. 0 .AND. CTYPM(MM) .NE. TYPEM(MM) ) GO TO 101
CLJ IF(CFLAG.NE. 0 .AND. CTYPH(HH) .NE. TYPEH(HH) ) GO TO 101

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[illegible]

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175      WT(160) = WT(160) + PIJKL * CPLOS
176      200 CONTINUE
177      C 2 LAYER CASE LL AND HH
178      MM = 4
179      DO 201 LL = LI,L2
180      DO 201 HH = HI,H2
181      IF(CFLAG-NE. 0 -AND. CTYPL(LL) -NE. TYPEL(LL)) GO TO 201
182      IF(CFLAG-NE. 0 -AND. CTYPM(HH) -NE. TYPEM(HH)) GO TO 201
183      IF(CFLAG-NE. 0 -AND. CTYPH(HH) -NE. TYPEH(HH)) GO TO 201
184      PL = ALX(LL) / TOTL
185      PH = ALX(HH+10) / TOTM
186      PIJKL = PL * PH * TOTL * TOTM / DEN * W(CC) * P(16)
187      IDX = IDX + 1
188      IF(TRANS(IDX) -NE. 0.) GO TO 1202
189      TRANS(IDX) = TRANSF(ALAM,LL,MM,HH)
190      EMISS(IDX) = EMISSF(ALAM,LL,MM,HH)
191      1202 CONTINUE
192      WT(IDX) = WT(IDX) + PIJKL*(1. - CPLOS)
193      WT(160) = WT(160) + PIJKL * CPLOS
194      201 CONTINUE
195      C 2 LAYER CASE MM AND HH
196      LL = 8
197      DO 202 MM = MI,M2
198      DO 202 HH = HI,H2
199      IF(CFLAG-NE. 0 -AND. CTYPL(LL) -NE. TYPEL(LL)) GO TO 202
200      IF(CFLAG-NE. 0 -AND. CTYPM(HH) -NE. TYPEM(HH)) GO TO 202
201      IF(CFLAG-NE. 0 -AND. CTYPH(HH) -NE. TYPEH(HH)) GO TO 202
202      PL = ALX(MM+7) / TOTM
203      PH = ALX(HH+10) / TOTL
204      PIJKL = PL * PH * TOTM * TOTL / DEN * W(CC) * P(16)
205      IDX = IDX + 1
206      IF(TRANS(IDX) -NE. 0.) GO TO 1203
207      TRANS(IDX) = TRANSF(ALAM,LL,MM,HH)
208      EMISS(IDX) = EMISSF(ALAM,LL,MM,HH)
209      1203 CONTINUE
210      WT(IDX) = WT(IDX) + PIJKL*(1. - CPLOS)
211      WT(160) = WT(160) + PIJKL * CPLOS
212      202 CONTINUE
213      C 3 LAYER CASE
214      DO 300 LL = LI,L2
215      DO 300 MM = MI,M2
216      DO 300 HH = HI,H2
217      IF(CFLAG-NE. 0 -AND. CTYPL(LL) -NE. TYPEL(LL)) GO TO 300
218      IF(CFLAG-NE. 0 -AND. CTYPM(MM) -NE. TYPEM(MM)) GO TO 300
219      IF(CFLAG-NE. 0 -AND. CTYPH(HH) -NE. TYPEH(HH)) GO TO 300
220      PL = ALX(LL) / TOTL
221      PM = ALX(MM+7) / TOTM
222      PH = ALX(HH+10) / TOTL
223      PIJKL = PL * PM * PH * W(CC) * P(17)
224      IDX = IDX + 1
225      IF(TRANS(IDX) -NE. 0.) GO TO 1301
226      TRANS(IDX) = TRANSF(ALAM,LL,MM,HH)
227      EMISS(IDX) = EMISSF(ALAM,LL,MM,HH)
228      1301 CONTINUE
229      WT(IDX) = WT(IDX) + PIJKL*(1. - CPLOS)
230      WT(160) = WT(160) + PIJKL * CPLOS
231      300 CONTINUE

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230 CLDWT
 231 CLDWT
 232 CLDWT
 233 CLDWT
 234 CLDWT
 235 CLDWT
 236 CLDWT
 237 CLDWT
 238 CLDWT

500 CONTINUE
 C ADD IN CLEAR SKY
 WT(160) = WT(160) + CCOVER(1,KMODEL)
 IDX = IDX + 1
 WT(IDX) = WT(160)
 CLJ TRANS(IDX) AND EMISS(IDX) WILL BE COMPUTED
 CLJ IN SUBROUTINE SCLOUD.
 1112 RETURN
 END

230

235

```

1      SUBROUTINE CLOUDO(MODE)
COMMON/CLOUD/ NCLCDD,
2      HCLCDD(20),THETCD(20),PHICD(20),CLOUDA(20),CLOUDB(20),
3      CLOUDC(20),CLOUDSI(20),KCLCDD(20)
4      COMMON /PARAMS/ IN,OUT,PL,RE, DTR,RTD
5      COMMON /CONFIG/CTYPL(8),CTYPM(4),CTYPH(5),CFLAG,C1,C2
COMMON /CLDFREQ/ KMODEL,CCOVER(5,11),CFREQ(17,4,11)

10     SUBROUTINE CLOUDO FIRST READS A FLAG (MODE) INDICATING BY A VALUE
      OF 0 OR 1 WHETHER THE DETERMINISTIC- OR STATISTICAL-CLOUD SUB-
      MODEL IS DESIRED. THE ROUTINE THEN READS CLOUD DATA APPROPRIATE
      TO THE INDICATED SUBMODEL AND MAKES THEM AVAILABLE TO THE
      APPROPRIATE ROUTINES.
15     FOR THE DETERMINISTIC SUBMODEL (MODE=0), THE NUMBER OF CLOUDS,
      THEIR LOCATIONS, TYPES, SIZES, AND (AZIMUTHAL) ORIENTATIONS ARE
      READ AND OUTPUTTED THROUGH CLOUD COMMON.
      FOR THE STATISTICAL SUBMODEL (MODE=1), THE ROUTINE READS AN INDEX
      KMODEL WHICH SELECTS DATA FROM THAT IN THE CODE OR ALLOWS THE
      USER TO INPUT HIS OWN DATA. OTHER FLAGS ARE READ WHICH ALLOW
      SELECTED PORTIONS OF THE PROVIDED DATA TO BE OVERRIDDEN. THESE
      USER-PROVIDED DATA ARE OUTPUTTED THROUGH CLDFREQ AND CONFIG
      COMMONS AND OVERRIDE DATA IN BLOCK DATA.

20     INPUT VARIABLES
      READ IN
      MODE = FLAG FOR DETERMINISTIC- OR STATISTICAL-CLOUD
      SUBMODEL
      = 0 FOR DETERMINISTIC-CLOUD SUBMODEL
      = 1 FOR STATISTICAL-CLOUD SUBMODEL
      FOR MODE=0 READ... (DETERMINISTIC SUBMODEL)
      NCLCDD = NUMBER OF CLOUDS
      FOR I=1,NCLCDD...
      KCLCDD(I) = CLOUD-TYPE INDEX, 1,2,...,14
      HCLCDD(I) = ALTITUDE OF CLOUD-I CENTER ABOVE THE
      SURFACE, KM
      THETCD(I) = COLATITUDE OF CLOUD-I, DEGREES
      PHICD(I) = EAST LONGITUDE OF CLOUD-I, DEGREES
      CLOUDA(I) = PRINCIPAL SEMIAXIS OF ELLIPSOIDAL CLOUD-I
      IN HORIZONTAL DIRECTION, KM
      CLOUDB(I) = PRINCIPAL SEMIAXIS OF ELLIPSOIDAL CLOUD-I
      IN HORIZONTAL DIRECTION, KM
      CLOUDC(I) = PRINCIPAL SEMIAXIS OF ELLIPSOIDAL CLOUD-I
      IN VERTICAL DIRECTION, KM
      CLOUDSI(I) = AZIMUTHAL ANGLE, MEASURED COUNTERCLOCKWISE,
      LOOKING DOWN, ORIENTED CLOUD ABOUT (VECTICAL)
      Z-AXIS. CLOUDS ARE NORMALLY ORIENTED WITH
      (+A)-AXIS EASTWARD (PSI=0), DEGREES
      FOR MODE=1 READ... (STATISTICAL SUBMODEL)
      KMODEL = FLAG CONTROLLING THE READING OF USER-SUPPLIED
      STATISTICAL CLOUD DATA (FURTHER DESCRIPTION IN
      BLOCK DATA)
      - 1,10 CODE USES DATA IN BLOCK DATA
      - 11 USER MUST READ IN FOLLOWING QUANTITIES...
      CCOVER(ICC,11) ICC=1,5
      CFREQ(K,ICC-1,11) K=1,17 ICC=2,5
      (DEFINITIONS IN BLOCK DATA)
      KCOVER = FLAG CONTROLLING THE READING OF OVERRIDE DATA

```

CLOUDO 2
 CLOUD 2
 CLOUD 3
 CLOUD 4
 CLOUD 4
 PARAMS 2
 CONFIG 2
 CLDFREQ 2
 CLOUDO 7
 CLOUDO 8
 CLOUDO 8
 CLOUDO 9
 CLOUDO 10
 CLOUDO 11
 CLOUDO 12
 CLOUDO 13
 CLOUDO 14
 CLOUDO 15
 CLOUDO 16
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 CLOUDO 53
 CLOUDO 54
 CLOUDO 55
 CLOUDO 56

B-34

B-35


```

1      SUBROUTINE CLOUD01
2
3      GET SOURCE POSITIONS AND DETECTOR POSITION IN CLOUD COORDINATES
4
5      INPUT PARAMETERS
6      CLOUD COMMON
7      MLCLOUD = NUMBER OF DETERMINISTIC CLOUDS (READ IN SUBROUTINE
8      CLOUD00)
9
10     DETECT COMMON
11     HD = ALTITUDE OF DETECTOR, KM
12     THETAD = COLATITUDE OF DETECTOR, DEGREES
13     PHID = EAST LONGITUDE OF DETECTOR, DEGREES
14
15     PARAMS COMMON
16     RE = EARTH'S RADIUS, KM
17
18     SOURCE COMMON
19     NSORCE = NUMBER OF SOURCES (CURRENTLY RESTRICTED TO ONE)
20     RSORCE(I) = ALTITUDE OF SOURCE-I ABOVE SURFACE, KM
21     THETAS(I) = COLATITUDE OF SOURCE-I, DEGREES
22     PHIS(I) = EAST LONGITUDE OF SOURCE-I, DEGREES
23
24     OUTPUT PARAMETERS
25     CDCORD COMMON
26     XI(I,K), = COORDINATES OF SOURCE-I IN K-TH CLOUD-CENTERED
27     ZETA(I,K), = CARTESIAN SYSTEM, KM I=1 K=1,20
28     XID(K), = COORDINATES OF DETECTOR IN K-TH CLOUD-CENTERED
29     ETAD(K), = CARTESIAN SYSTEM, KM K=1,20
30     ZETAD(K)
31
32     COMMON/CLOUD/ MLCLOUD,
33     1 HCLD(20),THETCD(20),PHICD(20),CLOUDA(20),CLOUDB(20),
34     2 CLOUDC(20),CLDPSI(20),KLCLOUD(20)
35     COMMON /PARAMS/ IN, IOUT, PI, RE, DTR, RTD
36     COMMON/CDCORD/ XI(1,20),ETA(1,20),ZETA(1,20),
37     1 X, ASQ(20),RSQ(20),CSQ(20)
38     2,CPHIBAR(16,20),CTHBAR(8,20),CRBAR(4,4,20),CAREA(4,4,20)
39     COMMON/SORCE/ NSORCE,RSORCE(1),RSORCE(1),THETAS(1),PHIS(1)
40     COMMON / DETECT/ HD, THETAD,PHID,FOV
41     DO 58 K=1,MLCLOUD
42     DO 55 I=1,NSORCE
43
44     CALL CLD E TO C(RE+RSORCE(I),THETAS(I),PHIS(I),XI(I,K),
45     X ETA(I,K),ZETA(I,K),K )
46
47     55 CONTINUE
48
49     CALL CLD E TO C(RE +HD,THETAD,PHID,XID(K),ETAD(K),ZETAD(K),K)
50
51     58 CONTINUE
52     RETURN
53     END

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1      CLJ      SUBROUTINE CLOUD2(UL,VL,ML)
2      CLJ      SUBROUTINE CLOUD2 IS AN AUXILIARY SUBROUTINE, OUTSIDE THE MAIN
3      CLJ      FLOW OF INFORMATION IN THE DETERMINISTIC CLOUD SUBMODEL. ITS
4      CLJ      OUTPUT IS NOT USED BY ANY OF THE OTHER ROUTINES IN THE NATURAL
5      CLJ      CLOUD MODEL. HOWEVER, CLOUD2 IS AN IMPORTANT ROUTINE, DESIGNED
6      CLJ      MAINLY FOR THE USE OF THE SIGHT-PATH-INTEGRATION MODELER IN
7      CLJ      ROSCOE-IR. GIVEN THE DIRECTION COSINES OF AN ARBITRARY LOS (NOT
8      CLJ      NECESSARILY ONE OF THE IMPORTANT SET SELECTED BY SUBROUTINE LOS),
9      CLJ      CLOUD2 WILL DETERMINE WHETHER OR NOT THE LOS INTERCEPTS ANY OF THE
10     CLJ      DETERMINISTIC CLOUDS. FOR EACH INTERCEPT THE ALTITUDE (ALTK(K))
11     CLJ      AND GEOGRAPHIC (POLAR) COORDINATES (THETALK(K),PHILK(K)) OF THE
12     CLJ      INTERCEPT ARE SET IN INTRCPT COMMON.
13     CLJ
14     CLJ      INPUT PARAMETERS
15     CLJ      ARGUMENT LIST
16     CLJ      UL, = DIRECTION COSINES IN EARTH-CENTERED CARTESIAN
17     CLJ      VL, = SYSTEM OF A USER-SPECIFIED LOS (SET IN DRIVER)
18     CLJ      ML
19     CLJ
20     CLJ      CORD COMMON
21     CLJ      XID(K), = COORDINATES OF DETECTOR IN K-TH CLOUD-CENTERED
22     CLJ      ETAD(K), = CARTESIAN SYSTEM, KM      K=1,20
23     CLJ      ZETAD(K)
24     CLJ      CLOUD COMMON
25     CLJ      NCLCUD = NUMBER OF DETERMINISTIC CLOUDS (READ IN SUBROUTINE
26     CLJ      CLOUDO)
27     CLJ
28     CLJ      DETECT COMMON
29     CLJ      HD = ALTITUDE OF DETECTOR, KM
30     CLJ      THETAD = ALTITUDE OF DETECTOR, DEGREES
31     CLJ      PHIO = EAST LONGITUDE OF DETECTOR, DEGREES
32     CLJ
33     CLJ      PARAMS COMMON
34     CLJ      DTR = CONVERSION FACTOR FROM DEGREES TO RADIANS
35     CLJ      RE = EARTH'S RADIUS, KM
36     CLJ
37     CLJ      OUTPUT PARAMETERS
38     CLJ      INTRCPT COMMON
39     CLJ      ALTK(K) = ALTITUDE AT WHICH THE USER-SPECIFIED LOS
40     CLJ      INTERCEPTS CLOUD-K, KM
41     CLJ      THETALK(K) = GEOGRAPHIC POLAR COORDINATE AT WHICH THE USER-
42     CLJ      SPECIFIED LOS INTERCEPTS CLOUD-K, DEG
43     CLJ      PHILK(K) = GEOGRAPHIC AZIMUTHAL COORDINATE AT WHICH THE USER-
44     CLJ      SPECIFIED LOS INTERCEPTS CLOUD-K, DEG
45     CLJ
46     CLJ      COMMON/CLOUD/ NCLCUD,
47     CLJ      1 HCLCUD(20),THETCD(20),PHICD(20),CLOUDA(20),CLOUDB(20),
48     CLJ      2 CLOUDC(20),CLDPSI(20),KCLCUD(20)
49     CLJ      COMMON /PARAMS/ IN,IOU,PL,RE, DTR,RTD
50     CLJ      COMMON / DETECT/ HD, THETAD,PHIO,FOV
51     CLJ      COMMON/COCORD/ XI(1,20),ETA(1,20),ZETA(1,20),
52     CLJ      1 XID(20),ETAD(20),ZETAD(20),CPH(5,20),CTH(5,20)
53     CLJ      X, ASQ(20),RSQ(20),CSQ(20)
54     CLJ      2 CPHIBAR(16,20),CTHBAR(8,20),CRBAR(4,4,20),CARBA(4,4,20)
55     CLJ      COMMON/INTRCPT/ ALTK(20),THETALK(20),PHILK(20)
56     CLJ      CT = COS(DTR * THETAD)
57     CLJ      CP = COS(DTR * PHIO)
58     CLJ      ST = SIN( DTR*THETAD )
59     CLJ      SP = SIN( DTR*PHIO )

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60      C
      CLJ      TRANSFORM LOS TO CLOUD CENTERED SYSTEM
      CLJ      ADD UNIT LOS VECTOR TO DETECTOR POSITION IN EARTH-CENTERED
      CLJ      CARTESIAN SYSTEM.
      RD = (RD + RE)
      X = RD*ST*CP + UL
      Y = RD*ST*SP + VL
      Z = RD + CT + WL

65      C
      CALL CT TO POL(RR,TH,PH,X,Y,Z)
      NOW HAVE GEOGRAPHIC POLAR COORDINATES (RH,TH,PH) OF TIP OF
      CLJ      UNIT LOS VECTOR STARTING FROM THE DETECTOR.
      CLJ
      DO 100 K = 1, N CLOUD
      CLJ      OBTAIN CLOUD-K CARTESIAN COORDINATES OF TIP OF UNIT LOS VECTOR
      CLJ      (XL,YL,ZL)
      CALL CLD E TO C (RH,TH,PH,XL,YL,ZL,K)
      CLJ      NOTE...RHO IS A UNIT VECTOR
      RHO = SQRT((XID(K)-XX)**2 + (ETAD(K)-YY)**2 + (ZETAD(K)-ZZ)**2)
      CLJ      WRITE(6,1001) K,RH,TH,PH,XL,YL,ZL,RHO
      1001 FORMAT (* PRINTED FROM CLOUD2 -FORMAT 1001 * /
      1 * K,RH,TH,PH,XL,YL,ZL,RHO * 12,1P7E13.5)
      C      LINE OF SIGHT VECTOR
      ULC = (XX - XID(K))/RHO
      VLC = (YY - ETAD(K))/RHO
      WLC = (ZZ - ZETAD(K))/RHO
      C      EVALUATE THE POSITION OF INTERCEPT ON
      C      K-TH CLOUD IN CLOUD COORD SYSTEM
      A = ULC**2 / ASQ(K) + VLC**2 / BSQ(K) + WLC**2 / CSQ(K)
      B = ULC*XID(K)/ASQ(K) + VLC*ETAD(K)/BSQ(K) + WLC*ZETAD(K)/CSQ(K)
      C = XID(K)**2/ASQ(K) + ETAD(K)**2/BSQ(K) + ZETAD(K)**2/CSQ(K) - 1.
      1003 FORMAT(14,'CLD2 K XYZ UVM ABC-12,1P9E12.5)
      C      NO INTERCEPT
      IF( B**2 - A*C - LI-0.) GO TO 100
      S = (-B - SQRT(B**2 - A*C))/A
      XIL = XID(K) + ULC*S
      ETAL = ETAD(K) + VLC*S
      ZETAL = ZETAD(K) + WLC*S
      C      CALL CLD C TO E ( R,THETALK(K),PHILK(K),XIL,ETAL,ZETAL,K )
      C      ALTK(K) = R - RE

100      C
      WRITE(6,1002) UL,VL,WL,K,ALTK(K),THETALK(K),PHILK(K)
      1002 FORMAT(* PRINTED FROM CLOUD2 */* THE LOS (* 3E12.4 * ) INTERCEPTS
      100      X CLOUD *12* AT*3E11.3 )
      100 CONTINUE
      RETURN
      END

105

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1	CLJ	SUBROUTINE CLOUD3(UL,VL,WL,K,ALAM,TCOEF,EMISS,SINCLD)	CLOUD3	2
	CLJ	SUBROUTINE CLOUD3, GIVEN THE DIRECTION COSINES UP A LOS FROM THE	CLOUD3	3
	CLJ	DETECTOR (AS SPECIFIED BY THE DRIVER) FIRST DETERMINES WHETHER OR	CLOUD3	4
5	CLJ	NOT THE LOS INTERSECTS CLOUD-K. IF NO INTERCEPT, TCOEF AND EMISS	CLOUD3	5
	CLJ	ARE SET TO ZERO AND A RETURN IS MADE TO THE CALLING ROUTINE (THE	CLOUD3	6
	CLJ	DRIVER). IF THE LOS INTERSECTS CLOUD-K, THE ROUTINE CONTINUES.	CLOUD3	7
	CLJ		CLOUD3	8
	CLJ		CLOUD3	9
10	CLJ	THE DO-100 LOOPS COMPUTE THE NORMAL PHOTON FLUX (IRRADIANCE)	CLOUD3	10
	CLJ	INCIDENT ON EACH FACET VIEWED BY THE SOURCE. SUBROUTINE DIFFUS	CLOUD3	11
	CLJ	THEN IS CALLED TO OBTAIN THE PHOTON FLUX (RADIANT EMISSION)	CLOUD3	12
	CLJ	EXITING FROM EACH FACET.	CLOUD3	13
	CLJ		CLOUD3	14
	CLJ	THE DO-200 LOOPS ARE OVER ALL FACETS.	CLOUD3	15
15	CLJ	1. ONE DETERMINES IF THE FACET CENTER IS VISIBLE TO THE DETECTOR	CLOUD3	16
	CLJ	2. IF THE FACET CENTER IS VISIBLE TO THE DETECTOR,	CLOUD3	17
	CLJ	A. THE CLOUD-CARTESIAN COORDINATES OF THE FACET CENTER ARE	CLOUD3	18
	CLJ	DETERMINED (XC,ETC,ZETC).	CLOUD3	19
	CLJ	B. THE DISTANCE (SDIST) FROM THE FACET CENTER NORMAL TO THE	CLOUD3	20
20	CLJ	LOS IS DETERMINED. THE SMALLEST VALUE OF SDIST IS ALWAYS	CLOUD3	21
	CLJ	SAVED.	CLOUD3	22
	CLJ	C. IF(SDIST-GE-0.7*SQRT(FOV)) AND IF THE CODE HAS PREVIOUSLY	CLOUD3	23
	CLJ	FOUND A FACET CENTER WITHIN (0.7*SQRT(FOV)) OF THE LOS,	CLOUD3	24
	CLJ	INDICATED BY KFLAG=1, THE FACET IS IGNORED. BUT IF THE	CLOUD3	25
25	CLJ	CODE HAS NOT PREVIOUSLY FOUND A FACET CENTER WITHIN	CLOUD3	26
	CLJ	(0.7*SQRT(FOV)) OF THE LOS, INDICATED BY KFLAG=0, AND IF	CLOUD3	27
	CLJ	(SDIST-GE-0.7*SQRT(FOV)), THEN A TRANSFER COEFFICIENT AND	CLOUD3	28
	CLJ	EMISSION WILL BE FOUND FOR ANY FACET FOR WHICH SDIST IS	CLOUD3	29
	CLJ	THE SMALLEST OF THOSE YET PROCESSED.	CLOUD3	30
30	CLJ	D. IF(SDIST-LE-0.7*SQRT(FOV)) THE DIRECTION COSINES TO THE	CLOUD3	31
	CLJ	SOURCE FROM THE FACET CENTER ARE DETERMINED.	CLOUD3	32
	CLJ	3. FURTHER TREATMENT OF THE FACET DEPENDS ON WHETHER OR NOT THE	CLOUD3	33
	CLJ	FACET CENTER IS VISIBLE TO THE SOURCE	CLOUD3	34
	CLJ	A. IF THE FACET IS NOT VISIBLE TO THE SOURCE, ONE DETERMINES	CLOUD3	35
35	CLJ	(1) THE COSINE OF THE ZENITH ANGLE (CTHOUT) TO THE DETECT.	CLOUD3	36
	CLJ	(2) THE AREA (AREAN) OF THE FACET NORMAL TO THE LOS	CLOUD3	37
	CLJ	(3) THE EMISSIVITY (EMISS) OF THE FACET, WEIGHTED BY AREAN	CLOUD3	38
	CLJ	(4) THE IRRADIANCE-TO-RADIANCE TRANSFER COEFFICIENT	CLOUD3	39
40	CLJ	(TCOEF) (AS DETERMINED BY DIFFUSION), WEIGHTED BY	CLOUD3	40
	CLJ	AREAN	CLOUD3	41
	CLJ	B. IF THE FACET IS VISIBLE TO THE SOURCE, ONE DETERMINES	CLOUD3	42
	CLJ	(1) THE INCIDENT ZENITH ANGLE AND THE EXIT ZENITH AND	CLOUD3	43
	CLJ	AZIMUTHAL ANGLE (FOR THE SOURCE-FACET-DETECTOR PATH)	CLOUD3	44
	CLJ	AND THE CORRESPONDING BIDIRECTIONAL REFLECTANCE	CLOUD3	45
45	CLJ	(2) THE AREA (AREAN) OF THE FACET NORMAL TO THE LOS	CLOUD3	46
	CLJ	(3) THE EMISSIVITY (EMISS) OF THE FACET, WEIGHTED BY AREAN	CLOUD3	47
	CLJ	(4) THE IRRADIANCE-TO-RADIANCE TRANSFER COEFFICIENT	CLOUD3	48
	CLJ	(TCOEF) (AS DETERMINED BY BIDIRECTIONAL REFLECTANCE),	CLOUD3	49
	CLJ	WEIGHTED BY AREAN	CLOUD3	50
50	CLJ	C. THE AVERAGE VALUES OF TCOEF AND EMISS ARE FOUND BY	CLOUD3	51
	CLJ	DIVIDING BY THE SUM OF THE WEIGHTED AREAS AREAN, TAREA,	CLOUD3	52
	CLJ	INCLUDED IN THE CALCULATION.	CLOUD3	53
	CLJ	D. IF THE FOV IS SO SMALL THAT NO FACET CENTER LIES WITHIN	CLOUD3	54
	CLJ	(0.7*SQRT(FOV)) OF THE LOS, THEN THE SUBROUTINE RETURNS	CLOUD3	55
55	CLJ	THE VALUE OF TCOEF AND EMISS FOR THAT FACET-CENTER THAT	CLOUD3	56
	CLJ	IS CLOSEST TO THE LOS.	CLOUD3	57
	CLJ	INPUT PARAMETERS	CLOUD3	58

60	CLJ	ARGUMENT LIST	CLOUD3	59
	CLJ	UL = DIRECTION COSINES IN EARTH-CENTERED CARTESIAN	CLOUD3	60
	CLJ	VL, SYSTEM OF A USER-SPECIFIED LOS (SET IN DRIVER)	CLOUD3	61
	CLJ	WL	CLOUD3	62
	CLJ	K = CLOUD NUMBER (SET IN DRIVER)	CLOUD3	63
	CLJ	ALAM = WAVELENGTH, MICRONS (SET IN DRIVER)	CLOUD3	64
	CLJ	ATNDUP COMMON	CLOUD3	65
65	CLJ	TT = TEMPERATURE OF AMBIENT ATMOSPHERE AT THE ALTITUDE	CLOUD3	66
	CLJ	IN THE ARGUMENT LIST OF SUBROUTINE ATMOSU, DEG K	CLOUD3	67
	CLJ	CDCORD COMMON	CLOUD3	68
	CLJ	XI(I,K) = COORDINATES OF SOURCE-I IN K-TH CLOUD-CENTERED	CLOUD3	69
	CLJ	ETAI(I,K), CARTESIAN SYSTEM, KM I=1 K=1,20	CLOUD3	70
70	CLJ	ZETA(I,K)	CLOUD3	71
	CLJ	XID(K) = COORDINATES OF DETECTOR IN K-TH CLOUD-CENTERED	CLOUD3	72
	CLJ	ETAD(K), CARTESIAN SYSTEM, KM K=1,20	CLOUD3	73
	CLJ	ZETAD(K)	CLOUD3	74
	CLJ	CLOUD COMMON	CLOUD3	75
75	CLJ	HICLOUD(K) = ALTITUDE OF CLOUD-K CENTER ABOVE THE SURFACE, KM	CLOUD3	76
	CLJ	CTHBAR(I,K) = POLAR ANGLE IN CLOUD-CENTERED COORDINATES OF THE	CLOUD3	77
	CLJ	CENTER OF THE I-TH POLAR SET OF SURFACE FACETS FOR	CLOUD3	78
	CLJ	ELLIPSOIDAL CLOUD-K, DEGREES I=1,8 K=1,20	CLOUD3	79
	CLJ	CPHIBAR(J,K) = AZIMUTHAL ANGLE IN CLOUD-CENTERED COORDINATES OF	CLOUD3	80
80	CLJ	THE CENTER OF THE J-TH AZIMUTHAL SET OF SURFACE	CLOUD3	81
	CLJ	FACETS FOR ELLIPSOIDAL CLOUD-K, DEGREES	CLOUD3	82
	CLJ	J=1,16 K=1,20	CLOUD3	83
	CLJ	CRBAR(I,J,K) = CLOUD-CENTERED RADIAL DISTANCE TO THE CENTER OF	CLOUD3	84
	CLJ	SURFACE FACET I,J IN PRINCIPAL OCTANT, KM	CLOUD3	85
85	CLJ	I=1,4 J=1,4 K=1,20	CLOUD3	86
	CLJ	(RESULTS FOR OTHER OCTANTS ARE OBTAINED BY SYMTY.)	CLOUD3	87
	CLJ	CAREA(I,J,K) = AREA OF SURFACE FACET I,J IN PRINCIPAL OCTANT OF	CLOUD3	88
	CLJ	ELLIPSOIDAL CLOUD-K, KM**2 I=1,4 J=1,4 K=1,20	CLOUD3	89
	CLJ	ASQ(K) = SQUARE OF LENGTH A, THE SEMI-MAJOR AXIS IN	CLOUD3	90
90	CLJ	HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2	CLOUD3	91
	CLJ	BSQ(K) = SQUARE OF LENGTH B, THE SEMI-MINOR AXIS IN	CLOUD3	92
	CLJ	HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2	CLOUD3	93
	CLJ	CSQ(K) = SQUARE OF LENGTH C, THE SEMI-MINOR AXIS IN	CLOUD3	94
95	CLJ	VERTICAL DIRECTION OF ELLIPSOIDAL CLOUD, KM**2	CLOUD3	95
	CLJ	DETECT COMMON	CLOUD3	96
	CLJ	HD = ALTITUDE OF DETECTOR, KM	CLOUD3	97
	CLJ	THETAD = CO-LATITUDE OF DETECTOR, DEGREES	CLOUD3	98
	CLJ	PHID = EAST LONGITUDE OF DETECTOR, DEGREES	CLOUD3	99
100	CLJ	FUV = FIELD OF VIEW OF DETECTOR AT EARTH'S SURFACE, KM**2	CLOUD3	100
	CLJ	PARAMS COMMON	CLOUD3	101
	CLJ	QTR = CONVERSION FACTOR FROM DEGREES TO RADIAN	CLOUD3	102
	CLJ	RE = EARTH'S RADIUS, KM	CLOUD3	103
	CLJ	FLUX COMMON	CLOUD3	104
105	CLJ	FOUR(I,J) = 4*PI TIMES THE OUTGOING PHOTON FLUX (RADIANT	CLOUD3	105
	CLJ	EMITTANCE) FROM ELLIPSOIDAL-SURFACE FACET (I,J)	CLOUD3	106
	CLJ	FOR A UNIT STRENGTH, ISOTROPIC POINT SOURCE	CLOUD3	107
	CLJ	(ONE PHOTON PER SEC), (4*PI*PHOTONS)/(KM**2 SEC)	CLOUD3	108
	CLJ	SORCE COMMON	CLOUD3	109
	CLJ	RSORCE = NUMBER OF SOURCES (CURRENTLY RESTRICTED TO ONE)	CLOUD3	110
110	CLJ	RSORCE(I) = RADIUS OF SOURCE-I, KM	CLOUD3	111
	CLJ	XX1111 COMMON	CLOUD3	112
	CLJ	KCLDK = A TEST FLAG USED TO DETERMINE WHETHER CLOUD3 IS	CLOUD3	113
	CLJ	NOW BEING CALLED WITH THE SAME CLOUD-NUMBER K AS	CLOUD3	114
	CLJ	FOR ITS LAST CALL.	CLOUD3	115


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IN THE EARTH SYSTEM
GENERATE THE FIN ARRAY BY CYCLING THROUGH THE SOURCES,
ADDING THE CONTRIBUTION OF EACH TO EVERY FIN(I,J)
ENTER WITH A SIGHT-PATH IN EARTH COORDINATES,
CLOUD NUMBER, WAVELENGTH, AND A SET OF NSORCE SOURCES.
THE SOURCES ARE IN COMMON/SORCE/ WHICH HAS TO BE FILLED
BY THE USER. DUPLICATE THE INSTRUCTIONS FROM CLOUD2 TO
TRANSFORM LOS TO CLOUD-CENTERED CARTESIAN SYSTEM.
RD = (RD + RE)
ST = SIN( DIR*THETAD )
SP = SIN( DIR*PHID )
CT = COS( DIR*THETAD )
CP = COS( DIR*PHID )
X = RD * ST * CP + UL
Y = RD * ST * SP + VL
Z = RD * CT + WL
WRITE(6,1001)K,X,Y,Z,SQRT(X**2+Y**2+Z**2),UL,VL,WL
FORMAT(* CLOUD3 FORMAT 1001 ---K,X,Y,Z,R,UVW* 13,1P7E11.3 )
1001 C
CALL CT TO POL(RHO,TH,PHI,X,Y,Z)
CALL CLD E TO C (RHO,TH,PHI,XX,YY,ZZ,K)
LOS VECTOR IN THE K-TH CLOUD COORD SYSTEM
NOTE---RHO IS OF UNIT LENGTH.
RHO=SQRT( (X-XID(K))**2 + (Y-ETAD(K))**2 + (Z-ZETAD(K))**2 )
ULC = ( X - XID(K) ) / RHO
VLC = ( Y - ETAD(K) ) / RHO
WLC = ( Z - ZETAD(K) ) / RHO
EVALUATE THE POSITION OF INTERCEPT ON
K-TH CLOUD IN CLOUD COORD SYSTEM
A = ULC**2 / ASQ(K) + VLC**2 / BSQ(K) + WLC**2 / CSQ(K)
B = ULC*XID(K)/ASQ(K)+VLC*ETAD(K)/BSQ(K)+WLC*ZETAD(K)/CSQ(K)
C = XID(K)**2 / ASQ(K) + ETAD(K)**2/BSQ(K) + ZETAD(K)**2/CSQ(K)-1.
IF ( (B**2 - A*C) .GT. 0.) GO TO 15
TCDEF = 0.
EMISS = 0.0
WRITE(6,10) UL,VL,WL,K
10 FORMAT(* CAUTION--- LOS (*3E12.5* ) DIDNT INTERSECT CLOUD *14,*
1 PRINTED FROM FORMAT 10 CLOUD3 *)
RETURN
15 CONTINUE
S = ( -B - SQRT(B**2 - A*C) ) / A
XIL, ETAL, ZETAL ARE THE COORDINATES OF THE INTERCEPT POINT
IN THE CLOUD-CENTERED CARTESIAN SYSTEM.
XIL = XID(K) + ULC*S
ETAL = ETAD(K) + VLC*S
ZETAL = ZETAD(K) + WLC*S
WRITE(6,1003)K,XIL,ETAL,ZETAL,SQRT(XIL**2+ETAL**2+ZETAL**2),S,ULC,
X VLC,WLC
1003 FORMAT(* 2 K XIL ETAL ZETAL R S ULC V W*13,1P8E10.2)
CIPALT = HCLD(K) + ZETAL
CALL ATMOSU(2,CIPALT)
TK = TT
WE HAVE JUST COMPUTED THE TEMPERATURE, TK, AT THE INTERCEPT
POINT THAT WILL BE USED LATER IN THE PLACK FUNCTION WHEN
COMPUTING THE EMISSION. WE IGNORE ANY DEPARTURE OF THE

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290      CLJ      Z = RS*RPZ
      CLJ      AT THE INTERSECTION POINT X,Y,Z THE UNIT OUTWARD NORMAL HAS
      CLJ      COMPONENTS VX,VY,VZ, OBTAINED FROM SUBROUTINE VXNORM...

295      CLJ      CALL VSNORM(X,Y,Z,VX,VY,VZ,K)
      CLJ      SAVE ORIGINAL SOURCE POSITION.
      CLJ      XISV = XI(1,K)
      CLJ      ETASV = ETA(1,K)
      CLJ      ZETASV = ZETA(1,K)
      CLJ      THE COMPONENT OF RPMS IN THE DIRECTION OF THE UNIT NORMAL AT
      CLJ      THE POINT X,Y,Z IS (V OUT RPMS = V OUT SP), I.E.,
      CLJ      VDOTSP = ( VX*RPX + VY*RPY + VZ*RPZ ) * RPMS
      CLJ      IF( VDOTSP.GE.RSOURCE(1) ) GO TO 40
      CLJ      OTHERWISE, WE MOVE THE SOURCE A DISTANCE DELP IN THE DIRECTION
      CLJ      OF THE UNIT NORMAL AT X,Y,Z, HAVING SAVED THE ORIGINAL SOURCE
      CLJ      POSITION. (WE USE THIS PARTICULAR UNIT NORMAL BECAUSE IT IS
      CLJ      READILY FOUND, WHEREAS THE PERPENDICULAR FROM THE SOURCE TO
      CLJ      THE CLOUD SURFACE IS NOT READILY FOUND.)
      CLJ      DELP = 0.5*(RSOURCE(1)-VDOTSP)
      CLJ      XI(1,K) = XI(1,K) + DELP*VX
      CLJ      ETA(1,K) = ETA(1,K) + DELP*VY
      CLJ      ZETA(1,K) = ZETA(1,K) + DELP*VZ
      CLJ      WRITE(6,1006) NS,K,XISV,ETASV,ZETASV,XI(1,K),ETA(1,K),ZETA(1,K)
310      CLJ      1006 FORMAT (*0 MESSAGE FROM SUBROUTINE CLOUD3 *)
      CLJ      1 *0 THE COORDINATES OF SOURCE NS=*,14,* , RELATIVE TO CLOUD K=*,
      CLJ      2 14,* , HAVE BEEN CHANGED...*/
      CLJ      3 * FROM XI,ETA,ZETA =*,3E14.5/* TO XI,ETA,ZETA =*,3E14.5)
315      CLJ      40 CONTINUE
      CLJ      IF( (K.EQ.KCLDK) .AND. (ALAM.EQ.CLDLAM) ) GO TO 110
      CLJ      START LOOP TO COMPUTE SOURCE-IRRADIATION OF CLOUD-K
      CLJ      OBTAIN FIN(I,J)
      CLJ      DO 100 I = 1,8
      CLJ      IP = IPRIME(I)
      CLJ      DO 100 J = 1,16
      CLJ      JP = JPRIME(J)
      CLJ      FIN(I,J) = 0.
      CLJ      CHECK TO SEE IF AREA(I,J) IS VISIBLE TO SOURCE
      CLJ      IF NOT, GO TO NEXT AREA
      CLJ      IF(PS(XI(NS,K),ETASV,K),ZETASV,K),CTHBAR(I,K),CPHIBAR(J,K),K)
325      CLJ      1 .LE. 0) GO TO 100
      CLJ      GET CLOUD-FACET CENTER IN CLOUD-CENTERED CARTESIAN
      CLJ      COORDINATES (XC,ETC,ZETC)
      CLJ      CALLPOL TO CT(CBAR(IP,JP,K),CTHBAR(I,K),CPHIBAR(J,K),K)
330      CLJ      GET UNIT VECTOR NORMAL TO ELLIPSOIDAL SURFACE AT (XC,ETC,ZETC)
      CLJ      CALL IT AN1,AN2,AN3
      CLJ      CALL VSNORM(XC,ETC,ZETC,AN1,AN2,AN3,K)
335      CLJ      RSQ=SUM OF SQUARE OF DISTANCE FROM SOURCE TO VISIBLE FACET-CENTER
      CLJ      RSQ=(CAC-XI(NS,K))**2 + (ETC-ETA(NS,K))**2 + (ZETC-ZETA(NS,K))**2
      CLJ      FIN(I,J) = FIN(I,J) +
      CLJ      1 (AN1*(XC-XI(NS,K)) + AN2*(ETC-ETA(NS,K)) + AN3*(ZETC-ZETA(NS,K)))
340      CLJ      1 / SQR(RSQ)**.5
      CLJ      100 CONTINUE
      CLJ

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333 C          CALCULATE FFOOT
334 C          CALL DIFPUS(K,ALAM)
335 C
336 C          110 KCLDK = K
337 C          CCLDAM = ALAM
338 C          LOOP OVER ALL AREAS VISIBLE TO AND IN FOV OF DETECTOR
339 C          SUM THE TOTAL AREA OF THE CLOUD FACETS NORMAL TO LOS
340 C
341 C          EMISS = 0.
342 C          TCOEF = 0.
343 C          TAREA = 0.
344 C
345 C          TO FORCE THE SUBROUTINE TO COMPUTE AND RETURN NOT ZERUS BUT
346 C          THE BEST POSSIBLE ANSWERS FOR TCOEF AND EMISS WHEN NO FACET
347 C          CENTER IS WITHIN (0.7*SQRT(FOV)) OF THE LOS, WE INTRODUCE TWO
348 C          VARIABLES, SSAVE AND KFLAG, TO FACILITATE TREATING THIS SMALL-
349 C          FOV CONDITION. SSAVE ULTIMATELY BECOMES THE SMALLEST VALUE OF
350 C          SDIST FOR THE SMALL-FOV CONDITION BUT IT IS INITIALIZED TO AN
351 C          ARBITRARILY LARGE VALUE. KFLAG IS INITIALIZED TO 0 BUT IS
352 C          RESET TO 1 IF AND WHEN THE CODE FINDS A FACET CENTER WITHIN
353 C          (0.7*SQRT(FOV)) OF THE LOS.
354 C          SSAVE = 1.0E+10
355 C          KFLAG = 0
356 C          DO 200 I = 1,8
357 C             IP = IPRIME(I)
358 C             DO 200 J = 1,16
359 C                JP = IPRIME(J)
360 C                IF (P(XID(K),ETAD(K),ZETAD(K),CTHBAR(L,K),CPHIBAR(J,K),K)
361 C                    .LT. 0.) GO TO 200
362 C                CALL PLOT TC,CTHBAR(IP,JP,K),CTHBAR(L,K),CPHIBAR(J,K),K)
363 C                CALL WSMJRM(XC,ETC,ZETC,AN1,AN2,AN3,K)
364 C
365 C                IF FACET CENTER IS NOT VISIBLE TO DETECTOR, GO TO NEXT FACET
366 C                IF (P(XID(K),ETAD(K),ZETAD(K),CTHBAR(L,K),CPHIBAR(J,K),K)
367 C                    .LT. 0.) GO TO 200
368 C                CALL PLOT TC,CTHBAR(IP,JP,K),CTHBAR(L,K),CPHIBAR(J,K),K,ETC,ZETC)
369 C                CALL WSMJRM(XC,ETC,ZETC,AN1,AN2,AN3,K)
370 C
371 C                THE CURRENT(L,J)-FACET CENTER IS VISIBLE TO A WIDE-ANGLE
372 C                DETECTOR, BUT IS IT WITHIN THE FOV OF THE DETECTOR SPECIFIED.
373 C                LET SDIST BE THE DISTANCE, (APPROXIMATELY) NORMAL TO THE LOS,
374 C                TO THE FACET CENTER.
375 C                GET ARG, THE COSINE OF THE ANGLE BETWEEN THE LOS AND THE
376 C                DIRECTION TO THE FACET CENTER FROM THE DETECTOR.
377 C                LET SDIST TEMPORARILY BE THE INVERSE DISTANCE FROM THE
378 C                DETECTOR TO THE FACET CENTER.
379 C                SDIST = 1.
380 C                1 / SQRT( (XC-XID(K))**2 + (ETC-ETAD(K))**2 + (ZETC-ZETAD(K))**2)
381 C                ARG = (ULC*(XC-XID(K)) + VLC*(ETC-ETAD(K)) + WLC*(ZETC-ZETAD(K)) )
382 C                1 / SDIST
383 C                IF (ABS(ARG) .GT. 1.) ARG = 1.
384 C                SDIST = ACOS(ARG) / SDIST
385 C                IF( SDIST.GT.SSAVE ) GO TO 150
386 C                SSAVE = SDIST
387 C                150 IF( (KFLAG.EQ.1) .AND. (SDIST.GT.0.7*SQRT(FOV)) ) GO TO 200
388 C                RR=DISTANCE FROM THE SOURCE TO THE FACET CENTER
389 C                RR = SQRT( (XC - XI(NS,K))**2 + (ETC-ETA (NS,K))**2 +
390 C                    (ZETC - ZETA(NS,K))**2 )
391 C                ULS-VLS-WLS ARE THE DIRECTION COSINES OF A UNIT VECTOR TOWARD
392 C                THE SOURCE FROM A FACET CENTER THAT IS EITHER WITHIN THE FOV
393 C                OF THE DETECTOR OR IS A CANDIDATE FOR BEING THE CLOSEST TO
394 C                THE FOV.
395 C                ULS = (XI(NS,K)-XC)/RR

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400      VLS = (ETA(NS,K)-ETC)/RR
      WLS = (ZETA(NS,K)-ZETC)/RR
      CLJ
      CLJ
      CLJ
      IF THE DETECTOR-VIEWED FACET-CENTER IS VISIBLE TO THE SOURCE,
      SKIP TO STATEMENT-201 TO COMPUTE THE TRANSFER COEFFICIENT
      FOR REFLECTANCE.
405      IF (PS(X(NS,K),ETA(NS,K),ZETA(NS,K),CTHAR(I,K),CPHAR(J,K),K)
      -GT. 0) GO TO 201
      CLJ
      CLJ
      THE DETECTOR-VIEWED FACET-CENTER IS NOT VISIBLE TO THE SOURCE
      SO COMPUTE THE TRANSFER COEFFICIENT FOR TRANSMISSION.
      CTHOUT = -( ANI*ULC+AN2*VLC+AN3*WLC)
      AREAN = CTHOUT * CAREA(IP,JP,K)
      IF ( KFLAG.EQ.1) -OR. (SDIST.LE.0.7*SQR(FOV)) ) GO TO 160
      IF (SDIST.NE.SSAVE) GO TO 200
      ESAVE = (1.-RHOEPS(ALAM,CTHOUT)) * PLANK(ALAM,TK) * AREAN
      TSAVE = 0.25*AREAN*FOOT(I,J)/(PI*PI)
      ASAVE = AREAN
      GO TO 200
410
415      160 CONTINUE
      EMISS = EMISS + (1.-RHOEPS(ALAM,CTHOUT))*PLANK(ALAM,TK)*AREAN
      CLJ
      CLJ
      THE FOLLOWING EXPRESSION FOR TCOEF, WHILE CORRECT AS USED,
      LACKS BEING A TRANSFER COEFFICIENT (FOR TRANSMISSION) BECAUSE
      (1) IT LACKS THE FACTORS 4*PI*DISTANCE**2 SUPPLIED AT THE END
      OF THE ROUTINE AND (2) IT INCLUDES A WEIGHTING FACTOR, AREAN,
      USED IN DETERMINING AN AVERAGE VALUE. (STRICTLY, A FACTOR
      DISTANCE**2 SHOULD HAVE BEEN INCLUDED IN THE QUANTITY BEING
      AVERAGED.) THE FACTOR 0.25/PI COMPENSATES FOR THE RADIANT
      EXITANCE, FOOT, BEING LARGE BY A FACTOR OF 4*PI. THE FACTOR
      1./PI CONVERTS THE RADIANT EXITANCE TO RADIANCE.
      TCOEF = FOOT(I,J) / PI**2*0.25 * AREAN * TCOEF
      TAREA = TAREA + AREAN
      CLJ
      CLJ
      WE HAVE FOUND A FACET CENTER WITHIN (0.7*SQR(FOV)) OF THE
      LOS SO SET KFLAG EQUAL TO 1.
      KFLAG = 1
      GO TO 200
420
425      201 CONTINUE
      THE DETECTOR-VIEWED FACET-CENTER IS VISIBLE TO THE SOURCE.
      CTHIN = ULS * AN1 + VLS * AN2 + WLS * AN3
      CTHOUT = -( ANI*ULC+AN2*VLC+AN3*WLC)
      AREAN = CTHOUT * CAREA(IP,JP,K)
      THE = ACOS( CTHIN )
      THI = ACOS( CTHIN )
      TPROUT = 1.0
      IF (THE.EQ.0.0) -OR. (THI.EQ.0.0) ) GO TO 165
      CPHOUT = (CTHOUT*CTHIN + (ULS*ULC + VLS*VLC + WLS*WLC)) /
      $ (SIN(THI) * SIN(THI))
430
435      165 CONTINUE
      IF (KFLAG.EQ.1) -OR. (SDIST.LE.0.7*SQR(FOV)) ) GO TO 170
      IF (SDIST.NE.SSAVE) GO TO 200
      ESAVE = (1.-RHOEPS(ALAM,CTHOUT)) * PLANK(ALAM,TK) * AREAN
      TSAVE = CLODDR(CTHIN,CTHOUT,CPHOUT,ALAM,KCLOUD(K))
      $ * AREAN*PI(I,J)/(4*PI)
      ASAVE = AREAN
      GO TO 200
440
445      170 CONTINUE
      THE FOLLOWING EXPRESSION FOR TCOEF, WHILE (ESSENTIALLY)
      CORRECT AS USED, LACKS BEING A TRANSFER COEFFICIENT (FOR
      REFLECTANCE) BECAUSE (1) IT (EFFECTIVELY) INCLUDES IN ITS
450
455

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460 CLJ DENOMINATOR THE FACTORS 4.*PI*DISTANCE**2 TO COMPENSATE FOR
CLJ THE SIMILAR FACTORS SUPPLIED AT THE END OF THE ROUTINE AND (2)
CLJ IT INCLUDES A HEIGHTING FACTOR, AREAN, USED IN DETERMINING AN
CLJ AVERAGE VALUE. THE USE OF FIN(I,J) IS A WAY OF INTRODUCING
CLJ THE REQUIRED CTIN FACTOR AND THE COMPENSATING 1./DISTANCE**2
CLJ FACTOR. (STRICTLY, THE VARIOUS FACTORS OF DISTANCE**2 USED
CLJ HERE DO NOT EXACTLY COMPENSATE FOR THE SINGLE DISTANCE**2
CLJ FACTOR USED AT THE END OF THE ROUTINE.)
465 TCOEF = AREAN*FIN(I,J)*CLOSOR(CTIN,CTHOUT,CPHOUT,ALAM,KCLOUD(K))
$ / (4.*PI) + TCOEF
TAREA = TAREA + AREAN
EMISS = EMISS + (1. - RHOEPS(ALAM,CTHOUT))*PLANK(ALAM,TK)*AREAN
KFLAG = 1
200 CONTINUE
C XIL,ETAL,ZETAL IS THE POSITION IN THE K'TH CLOUD COORDINATE
C SYSTEM OF INTERSECTION .. GET DISTANCE FROM SOURCE TO THIS PT
CLJ RDIS12=SQUARF OF DISTANCE FROM SOURCE TO CLOUD-INTERCEPT POINT
475 RDIS12 = (XIL - XI(NS,K))**2 + (ETAL - ETA(NS,K))**2
X + (ZETAL - ZETA(NS,K))**2
IF( TCOEF.GT.0.0 ) GO TO 220
EMISS = ESAVE
TCOEF = TSAVE
TAREA = ASAVE
480 IN THE FOLLOWING TWO EXPRESSIONS THE DIVISION BY POV IF POV
CLJ EXCEEDS TAREA (WHEN THE CLOUD EFFECTIVELY BECOMES A POINT
CLJ SOURCE) IS PROPER IF THE USER MULTIPLIES THE RADIANCES
CLJ CORRESPONDING TO TCOEF AND EMISS BY THE SOLID ANGLE OF THE
CLJ DETECTOR, POV/R**2, TO OBTAIN THE IRRADIANCE AT THE DETECTOR,
CLJ AT DISTANCE R FROM THE CLOUD.
220 TAPOV = AMAX1( TAREA,POV )
TCOEF = TCOEF / TAPOV * (4.*PI*RDIS12)
EMISS = EMISS / TAPOV
CLJ RESTORE SOURCE POSITION...
XI(1,K) = XISV
ETA(1,K) = ETASV
ZETA(1,K) = ZETASV
RETURN
END
490

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1      SUBROUTINE CLOUD9(RTP1,RTP2,RTP3,EC1,EC2,EC3,K)
2      CLOUD9
3      CLOUD9
4      CLOUD9
5      SUBROUTINE CLOUD9 HAS TWO ENTRY POINTS.
6      ENTRY-(CLD E TO C) CONVERTS FROM GEOGRAPHIC POLAR COORDINATES TO
7      CLOUD-CENTERED CARTESIAN COORDINATES.
8      ENTRY-(CLD C TO E) CONVERTS FROM CLOUD-CENTERED CARTESIAN
9      COORDINATES TO GEOGRAPHIC POLAR COORDINATES.
10     INPUT PARAMETERS
11     ARGUMENT LIST (FOR ENTRY CLD E TO C)
12     RTP1, = GEOGRAPHIC POLAR COORDINATES (RTP1=RADIUS, KM,
13     RTP2, = POLAR ANGLE (COLATITUDE), DEG.
14     RTP3, = AZIMUTHAL ANGLE (EAST LONGITUDE), DEG.)
15     K = CLOUD NUMBER
16     ARGUMENT LIST (FOR ENTRY CLD C TO E)
17     EC1, = CLOUD-K CENTERED CARTESIAN COORDINATES, KM
18     EC2, AND EC3
19     K = CLOUD NUMBER
20     CLOUD COMMON
21     THETCD(K) = COLATITUDE OF CLOUD-K, DEG
22     PHICD(K) = EAST LONGITUDE OF CLOUD-K, DEG
23     CLOPSI(1) = AZIMUTHAL ANGLE, MEASURED COUNTERCLOCKWISE
24     LOOKING DOWN, ORIENTING CLOUD ABOUT (VERTICAL)
25     Z-AXIS. CLOUDS ARE NORMALLY ORIENTED WITH
26     (*A)-AXIS EASTWARD (PSI=0.) DEGREES
27     PARAMS COMMON
28     DTR = CONVERSION FACTOR FROM DEGREES TO RADIAN
29     RE = EARTH'S RADIUS, KM
30     OUTPUT PARAMETERS
31     ARGUMENT LIST (FOR ENTRY CLD E TO C)
32     EC1, = CLOUD-K CENTERED CARTESIAN COORDINATES, KM
33     EC2, AND EC3
34     ARGUMENT LIST (FOR ENTRY CLD C TO E)
35     RTP1, = GEOGRAPHIC POLAR COORDINATES (RTP1=RADIUS, KM,
36     RTP2, = POLAR ANGLE (COLATITUDE), DEG.
37     RTP3, = AZIMUTHAL ANGLE (EAST LONGITUDE), DEG.)
38     COMMON/CLOUD/ NLCLOUD,
39     1 HLCLOUD(20),THETCD(20),PHICD (20),CLOUDA(20),CLOUDB(20),
40     2 CLOUDC(20),CLOPSI(20),KLCLOUD(20)
41     COMMON /PARAMS/ IN,LOUT,PI,RE, DTR,RTD
42     DIMENSION DA(3,3),XYZ(3)
43     EQUIVALENCE (DR,DTR),(REARTH,RE)
44     ENTRY CLD E TO C
45     ENTRY CLD E TO C CONVERTS FROM GEOGRAPHIC POLAR COORDINATES
46     (RTP(1,2,3) IN THE ARGUMENT LIST) TO CLOUD-CENTERED CARTESIAN
47     COORDINATES (EC(1,2,3) IN THE ARGUMENT LIST).
48     ENTRY CLD E TO C
49     IFLAG = 1
50     C***** DEFINE (X,Y,Z) EARTH CENTERED COORDINATES
51     C
52     CALL POL TO CT ( RTP1,RTP2,RTP3,X,Y,Z )
53     XYZ(1) = X
54     XYZ(2) = Y
55     C

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60      C ***** SET UP MATRIX DA( 3 BY 3 )
        SINPHI = SIN( DR*PHICD(K) )
        COSPHI = COS( DR*PHICD(K) )
        SINRHE = SIN( DR*THETCD(K) )
        COSRHE = COS( DR*THETCD(K) )
65      DA(1,1) = -SINPHI
        DA(2,1) = -COSTHE*COSPHI
        DA(3,1) = SINRHE*COSPHI
        DA(1,2) = COSPHI
        DA(2,2) = -COSTHE*SINPHI
        DA(3,2) = SINRHE*SINPHI
        DA(1,3) = 0.0
        DA(2,3) = SINRHE
        DA(3,3) = COSTHE
70
75      C ***** CALCULATE FINAL CLOUD CENTERED COORDINATE SYSTEM
        1 CONTINUE
        K=0. $ Y=0. $ Z=0.
        DO 11 J=1,3
            K = X + DA(1,J)*XYZ(J)
            Y = Y + DA(2,J)*XYZ(J)
            Z = Z + DA(3,J)*XYZ(J)
80      11 Z = Z + DA(3,J)*XYZ(J)
        C
        IF( IFLAG .EQ. 2 ) GO TO 14
        EC1 = X*COS( DR*CLDPSI(K) ) + Y*SIN( DR*CLDPSI(K) )
        EC2 = Y*COS( DR*CLDPSI(K) ) - X*SIN( DR*CLDPSI(K) )
        EC3 = Z - ( REARTH + HCLDUD(K) )
        RETURN
85
90      C 14 CALL CT TO POL(RTP1,RTP2,RTP3,X,Y,Z)
        C
        CLJ      RETURN
        CLJ      ENTRY CLD C TO E CONVERTS FROM CLOUD-CENTERED CARTESIAN
        CLJ      COORDINATES (EC(1,2,3) IN THE ARGUMENT LIST) TO GEOGRAPHIC
        CLJ      POLAR COORDINATES (RTP(1,2,3) IN THE ARGUMENT LIST).
95
        C      ENTRY CLD C TO E
        C      IFLAG = 2
100      C
        XYZ(1) = EC1*COS( DR*CLDPSI(K) ) - EC2*SIN( DR*CLDPSI(K) )
        XYZ(2) = EC1*SIN( DR*CLDPSI(K) ) + EC2*COS( DR*CLDPSI(K) )
        XYZ(3) = EC3 + ( RE + HCLDUD(K) )
105      C
        C      TRANSPOSE MATRIX
        SINPHI = SIN( DR*PHICD(K) )
        COSPHI = COS( DR*PHICD(K) )
        SINRHE = SIN( DR*THETCD(K) )
        COSRHE = COS( DR*THETCD(K) )
110      DA(1,1) = -SINPHI
        DA(1,2) = -COSTHE*COSPHI
        DA(1,3) = SINRHE*COSPHI
        DA(2,1) = COSPHI
        DA(2,2) = -COSTHE*SINPHI
        DA(2,3) = SINRHE*SINPHI
        DA(3,1) = 0.0
        DA(3,2) = SINRHE
        DA(3,3) = COSTHE
115
120      C      CALCULATE FINAL GEOGRAPHIC POLAR COORDINATES.
        CLJ      GO TO 1
        END

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1      SUBROUTINE CONVERT(R,TH,PH,X,Y,Z)
2
3      SUBROUTINE CONVERT HAS TWO ENTRY POINTS.
4      ENTRY-CT TO POL) CONVERTS FROM THE CARTESIAN COORDINATES (X,Y,Z)
5      TO THE POLAR COORDINATES (R,TH,PH).
6      ENTRY-POL TO CT) CONVERTS FROM THE POLAR COORDINATES (R,TH,PH)
7      TO THE CARTESIAN COORDINATES (X,Y,Z).
8
9      INPUT PARAMETERS
10     ARGUMENT LIST (FOR ENTRY CT TO POL)
11     X, = CARTESIAN COORDINATES, USUALLY IN KM
12     Y, AND Z
13     ARGUMENT LIST (FOR ENTRY POL TO CT)
14     R = RADIUS, USUALLY IN KM
15     TH = POLAR ANGLE (COLATITUDE), DEG
16     PH = AZIMUTHAL ANGLE (EAST LONGITUDE), DEG
17
18     OUTPUT PARAMETERS
19     ARGUMENT LIST (FOR ENTRY CT TO POL)
20     R = RADIUS, SAME UNITS AS X,Y,Z
21     TH = POLAR ANGLE (COLATITUDE), DEG
22     PH = AZIMUTHAL ANGLE (EAST LONGITUDE), DEG
23     ARGUMENT LIST (FOR ENTRY POL TO CT)
24     X, = CARTESIAN COORDINATES, SAME UNITS AS R
25     Y,Z (EARTH-CENTERED IF (R,TH,PH) ARE EARTH-CENTERED)
26
27     DATA DTR,RTD / -.01745329251994,57.2957795131 /
28
29     ENTRY CT TO POL
30
31     R= SQRT( X**2 + Y**2 + Z**2 )
32     TH= ACOS( Z/R)*RTD
33     PH = ATAN2( Y,X )*RTD
34     RETURN
35
36     ENTRY POL TO CT
37
38     CT = COS( DTR*TH ) $ ST = SIN( DTR*TH )
39     CP = COS( DTR*PH ) $ SP = SIN( DTR*PH )
40     X= R*ST*CP
41     Y= R*ST*SP
42     Z= R*CT
43     RETURN
44     END

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1	CLJ	SUBROUTINE DIFFUS(K,ALAM)	DIFFUS	2
	CLJ		DIFFUS	3
	CLJ	SUBROUTINE DIFFUS PROVIDES THE OUTGOING PHOTON FLUX (RADIANT	DIFFUS	4
5	CLJ	EMITTANCE) FROM A SURFACE ELEMENT ON AN ELLIPSOIDAL CLOUD	DIFFUS	5
	CLJ	IRRADIATED BY A UNIT-STRENGTH, ISOTROPIC POINT SOURCE (BASED ON AN	DIFFUS	6
	CLJ	APPROXIMATE, ITERATIVE SOLUTION OF THE DIFFUSION EQUATION).	DIFFUS	7
	CLJ		DIFFUS	8
	CLJ	INPUT PARAMETERS	DIFFUS	9
	CLJ	ARGUMENT LIST	DIFFUS	10
	CLJ	K = CLOUD NUMBER	DIFFUS	11
10	CLJ	ALAM = WAVELENGTH, MICRONS	DIFFUS	12
	CLJ	CDCORD COMMON	DIFFUS	13
	CLJ	ASQ(K) = SQUARE OF LENGTH A, THE SEMI-MAJOR AXIS IN	DIFFUS	14
	CLJ	HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2	DIFFUS	15
15	CLJ	BSQ(K) = SQUARE OF LENGTH B, THE SEMI-MINOR AXIS IN	DIFFUS	16
	CLJ	HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2	DIFFUS	17
	CLJ	CSQ(K) = SQUARE OF LENGTH C, THE SEMI-MINOR AXIS IN	DIFFUS	18
	CLJ	VERTICAL DIRECTION OF ELLIPSOIDAL CLOUD, KM**2	DIFFUS	19
	CLJ	CTHBAR(I,K) = POLAR ANGLE IN CLOUD-CENTERED COORDINATES OF THE	DIFFUS	20
	CLJ	CENTER OF THE I-TH POLAR SET OF SURFACE FACETS FOR	DIFFUS	21
20	CLJ	ELLIPSOIDAL CLOUD-K, DEGREES I=1,8 K=1,20	DIFFUS	22
	CLJ	CPHIBAR(J,K) = AZIMUTHAL ANGLE IN CLOUD-CENTERED COORDINATES OF	DIFFUS	23
	CLJ	THE CENTER OF THE J-TH AZIMUTHAL SET OF SURFACE	DIFFUS	24
	CLJ	FACETS FOR ELLIPSOIDAL CLOUD-K, DEGREES	DIFFUS	25
25	CLJ	J=1,16 K=1,20	DIFFUS	26
	CLJ	CRBAR(I,J,K) = CLOUD-CENTERED RADIAL DISTANCE TO THE CENTER OF	DIFFUS	27
	CLJ	SURFACE FACET I,J IN PRINCIPAL OCTANT, KM	DIFFUS	28
	CLJ	I=1,4 J=1,4 K=1,20	DIFFUS	29
30	CLJ	(RESULTS FOR OTHER OCTANTS ARE OBTAINED BY SYMTRY.)	DIFFUS	30
	CLJ	CAREA(I,J,K) = AREA OF SURFACE FACET I,J IN PRINCIPAL OCTANT OF	DIFFUS	31
	CLJ	ELLIPSOIDAL CLOUD-K, KM**2 I=1,4 J=1,4 K=1,20	DIFFUS	32
	CLJ	CDDATA COMMON	DIFFUS	33
	CLJ	ALAMT(I) = WAVELENGTHS AT WHICH OPTICAL PROPERTIES ARE	DIFFUS	34
35	CLJ	TABULATED, MICRONS	DIFFUS	35
	CLJ	SIGT(I,K) = TOTAL MICROSCOPIC EXTINCTION CROSS-SECTION AT	DIFFUS	36
	CLJ	WAVELENGTH ALAMT(I) FOR CLOUD-TYPE K, MICRON**2	DIFFUS	37
	CLJ	SIGS(I,K) = MICROSCOPIC SCATTERING CROSS-SECTION AT	DIFFUS	38
	CLJ	WAVELENGTH ALAMT(I) FOR CLOUD-TYPE K, MICRON**2	DIFFUS	39
40	CLJ	W(I) = (NORMALIZED) CONTRIBUTION OF SPECULARLY-	DIFFUS	40
	CLJ	REFLECTED RADIATION TO SCATTERED RADIATION WITH	DIFFUS	41
	CLJ	THE DIFFRACTED RADIATION CONTRIBUTING UNITY.	DIFFUS	42
	CLJ	USED ONLY FOR THE LARGE-PARTICLE-SIZE CLOUDS,	DIFFUS	43
	CLJ	TYPES 11 THROUGH 14. (DIMENSIONLESS)	DIFFUS	44
45	CLJ	XHUBAR(I,K) = AVERAGE COSINE OF SCATTERING ANGLE AT	DIFFUS	45
	CLJ	WAVELENGTH ALAMT(I) FOR CLOUD-TYPE K	DIFFUS	46
	CLJ	DNO(K) = NUMBER DENSITY OF WATER DROPLETS IN	DIFFUS	47
	CLJ	CLOUD-TYPE K, 1/CM**3	DIFFUS	48
	CLJ	CLOUD COMMON	DIFFUS	49
50	CLJ	KCLOUD(K) = CLOUD-TYPE INDEX (1,14) FOR CLOUD K, K=1,20	DIFFUS	50
	CLJ	FLUX COMMON	DIFFUS	51
	CLJ	FIN(I,J) = 4*PI TIMES THE INCOMING (NORMAL) PHOTON FLUX	DIFFUS	52
	CLJ	(IRRADIANCE) AT ELLIPSOIDAL-SURFACE FACET (I,J) AT	DIFFUS	53
	CLJ	DISTANCE R FROM A UNIT STRENGTH, ISOTROPIC POINT	DIFFUS	54
55	CLJ	SOURCE (I.E., (R DOT N)/R**3), I=1,8 J=1,16	DIFFUS	55
	CLJ	4*PI*PHOTONS/(KM**2 SEC) FOR UNIT SOURCE	DIFFUS	56
	CLJ	PARAMS COMMON	DIFFUS	57
	CLJ	PI = 3.14159265	DIFFUS	58


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60 CLJ OUTPUT PARAMETER
CLJ FLUX COMMON
CLJ FOUR(I,J) = 4.*PI TIMES THE OUTGOING PHOTON FLUX (RADIANT
CLJ EMITTANCE) FROM ELLIPSOIDAL-SURFACE FACET (I,J)
CLJ FOR A UNIT STRENGTH, ISOTROPIC POINT SOURCE
CLJ (ONE PHOTON PER SEC), (4.*PI*PHOTONS)/(KM**2 SEC)
CLJ

65 COMMON/CLOUD/ N CLOUD,
1 H CLOUD(20),THETC(20),PHICD(20),CLOUDA(20),CLOUDB(20),
2 CLOUDC(20),CLDPSI(20),K CLOUD(20)
COMMON /PARAMS/ IN,LOUT,PI,RE, DTR,RTD
COMMON/CDCORD/ XI( 1,20),ETA( 1,20),ZETA( 1,20),
1 XID(20),ETAD(20),ZETAD(20),CPH(5,20),CTH(5,20)
X , ASQ(20),BSQ(20),CSQ(20)
2 ,CPHIBAR(15,20),CTHBAR(8,20),CRBAR(4,4,20),CAREA(4,4,20)
DIMENSION SR(8,16),QR(8,16),FI(8,16)
COMMON/CDDATA/ ALAMT(10),SIGT(10,14),SIGS(10,14),W(10),
1 XMUBAR(10,14),DNOC(14),RAD(14),CLDBASE(14),CLDTHK(14)
COMMON/FLUX/ FIM(8,16),FOUT(8,16)
DIMENSION XIK(8,16),ETAK(8,16),ZETAK(8,16)
2 DIMENSION CXTRAP(11),XTRAP(11),CRELAX(29),RELAX(29)

80 CLJ XTRAP(CXTRAP(I)) AND RELAX(CRELAX(I)) ARE, RESPECTIVELY, THE
CLJ (DIMENSIONLESS) LINEAR EXTRAPOLATION LENGTHS AND RELAXATION
CLJ RATES, AT MATRPC AND NRELX VALUES CXTRAP(I) AND CRELAX(I) OF
CLJ THE PARAMETER C (RATIO OF SCATTERING TO TOTAL CROSS-SECTION),
CLJ TAKEN FROM TABLES 23 AND 9, RESPECTIVELY, OF INTRODUCTION TO
CLJ THE THEORY OF NEUTRON DIFFUSION, VOLUME 1, BY K.M. CASE,
CLJ F. DE HUFFMANN, AND G. PLACZEK, LASL, JUNE 1953.
CLJ

90 DATA MATRPC,NRELX / 11, 29 /
DATA CXTRAP / 0.0 , 0.1 , 0.2 , 0.3 , 0.4 , 0.5 ,
1 0.6 , 0.7 , 0.8 , 0.9 , 1.0 /
DATA XTRAP / 1.0000, 1.0000, 0.9993, 0.9889, 0.9606, 0.9201,
1 0.8750, 0.8300, 0.7871, 0.7472, 0.7104 /
DATA CRELAX/0.00 , 0.10 , 0.20 , 0.30 , 0.35 , 0.40 ,
1 0.45 , 0.50 , 0.55 , 0.60 , 0.65 , 0.70 ,
2 0.75 , 0.80 , 0.82 , 0.84 , 0.86 , 0.88 ,
3 0.90 , 0.91 , 0.92 , 0.93 , 0.94 , 0.95 ,
4 0.96 , 0.97 , 0.98 , 0.99 , 1.00 /
DATA RELAX/1.000000,1.000000,0.999909,0.997414,0.993164,0.985624,
1 0.973976,0.957504,0.935529,0.907332,0.872065,0.828635,
2 0.775516,0.710412,0.680241,0.647220,0.610884,0.570591,
3 0.525430,0.500615,0.474002,0.445270,0.413976,0.379485,
4 0.340829,0.296381,0.242983,0.172511,0.0 /
CLJ THE ARITHMETIC FUNCTION DIST(X1,V1,X2,V2,Z2) COMPUTES THE
CLJ DISTANCE BETWEEN THE POINTS (X1,V1,Z1) AND (X2,V2,Z2).
C DIST(X1,V1,Z1,X2,V2,Z2) = SORT((X2-X1)**2+(V2-V1)**2+(Z2-Z1)**2)
EVALUATE THE CART COORD OF THE 128 AREAS IN THE K TH CLD
DO 10 I = 1,8
IP = IPRIME(I)
DO 10 J = 1,16
JP = JPRIME(J)
CALL POL TO CT(CRBAR(IP,JP,K),CTHBAR(L,K),CPHIBAR(J,K),
X XIK(I,J),ETAK(I,J),ZETAK(I,J) )
10 CONTINUE
C

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B-53

B-54

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230      WRITE(6,4000) (J,(SR (1,J),I=1,8),J=1,16)
      WRITE(6,4000) (J,(QR (1,J),I=1,8),J=1,16)
      WRITE(6,4000) (J,(FOUT(1,J),I=1,8),J=1,16)
      FORMAT(1H0,14,1P8E12.4/(1X,14,1P8E12.4))
210 CONTINUE
      RETURN
235      HAVING OBTAINED THE FIRST-APPROXIMATION SOLUTION FOR THE
      PHOTON FLUX, WE PROCEED TO OBTAIN THE SECOND-APPROXIMATION
      SOLUTION. MOST OF THE STEPS ARE A REPETITION OF THOSE ABOVE.
240      DO-400 LOOPS ARE OVER THE OUT-FACETS
      DO 400 IJ = 1,8
      IOP = IPRIME(IJ)
      DO 400 JO = 1,16
      JOP = IPRIME(JO)
      FOUT(IJ,JO) = F1(IJ,JO)
      DO 300 II = 1,8
      IIP = IPRIME(II)
      DO 300 JI = 1,16
      IF(IJ.EQ.II .AND. JO.EQ.JI) GO TO 300
      JIP = IPRIME(JI)
      R = DIST(XIK(IJ,JO),ETAK(IJ,JO),ZETAK(IJ,JO),
      1 XIK(II,JI),ETAK(II,JI),ZETAK(II,JI) )
      GR = EXP(-DK*R) / R
      EN DOT DG = GR * (DK + 1. / R)
      CALL VSNDQM(XIK(II,JI),ETAK(II,JI),ZETAK(II,JI),AN1,AN2,AN3,K)
      EN DOT DG = EN DOT DG + (( XIK(IJ,JO) - XIK(II,JI) ) * AN1
      1 X + ( ZETAK(IJ,JO) - ZETAK(II,JI) ) * AN3) / R
      PP = DA * GR + EN DOT DG * DDD/2.
      PM = -DA * GR + EN DOT DG * DDD/2.
      FOUT(IJ,JO) = FOUT(IJ,JO) - (F1(II,JI) - F1(IJ,JO)) *
      X PP * CAREA(IIP,JIP,K) / (PI*DDD*QR(IJ,JO))
      300 CONTINUE
      400 CONTINUE
      RETURN
      END
245      CLJ
250      CLJ
255      CLJ
260      CLJ
265      CLJ

```

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 225 DIFFUS
 226 DIFFUS
 227 DIFFUS
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1      SUBROUTINE DIFFRM(ALAM)
2      ALAM = WAVELENGTH TABLE IN MICRONS
3      SIGT,SIGS, MICROSCOPIC CROSS SECTIONS IN MICRONS SQUARED
4      DNO      PARTICLE DENSITY IN CM**3
5      C
6      DALFA,DRETA,DKAPPA ARE DIFFUSION PARAMETERS
7      C
8      SUBROUTINE DIFFRM PROVIDES THREE DIFFUSION PARAMETERS FOR EACH
9      OF THE 14 CLOUD TYPES AT WAVELENGTH ALAM.
10     C
11     INPUT PARAMETERS
12     ARGUMENT LIST
13     ALAM = WAVELENGTH, MICRONS
14     C
15     CDDATA COMMON
16     ALAM(I) = WAVELENGTHS AT WHICH OPTICAL PROPERTIES ARE
17     TABULATED, MICRONS
18     SIGT(I,K) = TOTAL MICROSCOPIC EXTINCTION CROSS-SECTION
19     AT WAVELENGTH ALAM(I) FOR CLOUD-TYPE K,
20     (MICRONS)**2
21     SIGS(I,K) = MICROSCOPIC SCATTERING CROSS-SECTION
22     AT WAVELENGTH ALAM(I) FOR CLOUD-TYPE K,
23     (MICRONS)**2
24     W(I) = (NORMALIZED) CONTRIBUTION OF SPECULARLY-
25     REFLECTED RADIATION TO SCATTERED RADIATION WITH
26     THE DIFFRACTED RADIATION CONTRIBUTING UNITY.
27     USED ONLY FOR THE LARGE-PARTICLE-SIZE CLOUDS,
28     TYPES 11 THROUGH 14. (DIMENSIONLESS)
29     XMURAR(I,K) = AVERAGE COSINE OF SCATTERING ANGLE AT
30     WAVELENGTH ALAM(I) FOR CLOUD-TYPE K
31     DNO(K) = NUMBER DENSITY OF WATER DROPLETS IN
32     CLOUD-TYPE K, 1/CM**3
33     RAD(K) = MEAN RADII OF WATER DROPLETS IN
34     CLOUD-TYPE K, MICRONS
35     FOR ABOVE VARIABLES I=1,10 AND K=1,14
36     C
37     OUTPUT PARAMETERS
38     DIFFUS COMMON
39     DALFA(K) = 0.25 TIMES THE RATIO OF SCATTERING CROSS-
40     SECTION TO TOTAL CROSS-SECTION FOR PHOTONS OF
41     WAVELENGTH ALAM IN CLOUD-TYPE K, DIMENSIONLESS
42     DBETA(K) = 0.50 TIMES THE DIFFUSION COEFFICIENT FOR
43     PHOTONS OF WAVELENGTH ALAM IN CLOUD-TYPE K, KM
44     DKAPPA(K) = INVERSE DIFFUSION LENGTH FOR PHOTONS OF
45     WAVELENGTH ALAM IN CLOUD-TYPE K, 1/KM
46     C
47     FOR ABOVE VARIABLES K=1,14
48     THE ABOVE DEFINITIONS FOR THE DIFFUSION PARAMETERS APPLY TO A
49     WEAKLY ABSORBING MEDIUM. FOR A STRONGLY ABSORBING MEDIUM,
50     MODIFIED DIFFUSION PARAMETERS ARE REQUIRED. WE ALSO COMPUTE
51     THE LATTER TYPE AND USE THEM AFTER 9/30/78.
52     C
53     COMMON /PARAMS/ IN,IOU,P1,RE, DTR,RTD
54     COMMON/CDDATA/ ALAM(10),SIGT(10,14),SIGS(10,14),W(10),
55     1 XMURAR(10,14),DNO(14),RAD(14),CLDBASF(14),CLDTHR(14)
56     COMMON/DIFFUS/DALFA(14),DBETA(14),DKAPPA(14)
57     DIMENSION CXTRAP(11),XTRAP(11),CRELAX(29),RELAX(29)

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60 CLJ XTRAP(CXTRAP(I)) AND RELAX(CRELAX(I)) ARE, RESPECTIVELY, THE
CLJ (DIMENSIONLESS) LINEAR EXTRAPOLATION LENGTHS AND RELAXATION
CLJ RATES, AT NTRPC AND ARELC VALUES CXTRAP(I) AND CRELAX(I) OF
CLJ THE PARAMETER C (RATIO OF SCATTERING TO TOTAL CROSS-SECTION),
CLJ TAKEN FROM TABLES 23 AND 9, RESPECTIVELY, OF INTRODUCTION TO
CLJ THE THEORY OF NEUTRON DIFFUSION, VOLUME 1, BY K. M. CASE,
CLJ P. DE HOFFMANN, AND G. PLATZKE, LASL, JUNE 1953.
CLJ
CLJ DATA NTRPC,NRELXC / 11, 29 /
CLJ DATA CXTRAP / 0.0 , 0.1 , 0.2 , 0.3 , 0.4 , 0.5 ,
CLJ 1 0.6 , 0.7 , 0.8 , 0.9 , 1.0 /
CLJ DATA XTRAP / 1.0000, 1.0000, 0.9993, 0.9889, 0.9606, 0.9201,
CLJ 1 0.8750, 0.8300, 0.7871, 0.7472, 0.7104/
CLJ DATA CRELAX/0.00 ,0.10 ,0.20 ,0.30 ,0.35 ,0.40
CLJ 1 0.45 ,0.50 ,0.55 ,0.60 ,0.65 ,0.70
CLJ 2 0.75 ,0.80 ,0.82 ,0.84 ,0.86 ,0.88
CLJ 3 0.90 ,0.91 ,0.92 ,0.93 ,0.94 ,0.95
CLJ 4 0.96 ,0.97 ,0.98 ,0.99 ,1.00
CLJ DATA RELAX/1.00000,1.00000,0.99909,0.99741,0.99316,0.98562,
CLJ 1 0.97397,0.95750,0.93552,0.90733,0.87206,0.82863,
CLJ 2 0.77516,0.71041,0.68024,0.64722,0.61088,0.57059,
CLJ 3 0.52530,0.50061,0.47400,0.44527,0.41397,0.37948,
CLJ 4 0.34082,0.29638,0.24298,0.17251,0.0
CLJ
CLJ COSH(ARG) = (EXP(ARG) + EXP(-ARG)) / 2.
CLJ SINH(ARG) = (EXP(ARG) - EXP(-ARG)) / 2.
CLJ
CLJ TRANSMITTANCE T AND REFLECTANCE R OF PLANAR SLAB, PER
CLJ EQUATIONS (31A) AND (31B) OF APPENDIX A, NATURAL CLOUDS, THE
CLJ ROSCOE MANUAL VOL. 24.
CLJ
CLJ T(X,Y) = 1.0 / ( COSH(X) + 0.5*( Y+1./Y )*SINH(X) )
CLJ R(X,Y) = 0.5*T(X,Y)*( Y-1./Y )*SINH(X)
CLJ
CLJ DO 20 I = 2,10
CLJ IF (ALAMT(I) .GT. ALAM) GO TO 25
CLJ 20 CONTINUE
CLJ I = 10
CLJ 25 XX = (ALAM - ALAMT(I-1)) / (ALAMT(I) - ALAMT(I-1))
CLJ
CLJ C
CLJ C INTERPOLATE FOR DIFFUSION PARAMETERS AT GIVEN WAVELENGTH
CLJ C FOR ALL 14 CLOUD TYPES
CLJ C
CLJ W1 = W(I-1) + ( W(I)-W(I-1) ) * XX
CLJ GO TO 111
CLJ
CLJ FOR EDUCATIONAL PURPOSES, THE TRANSMITTANCE T AND REFLECTANCE
CLJ R OF CLOUD-TYPE KK WITH THICKNESS CLOTHK(KK) ARE EVALUATED
CLJ FIRST FOR THE STANDARD DIFFUSION PARAMETERS AND THEN FOR THE
CLJ MODIFIED DIFFUSION PARAMETERS FOR AN ABSORBING MEDIUM. THE
CLJ LATTER PARAMETERS HAVE BEEN USED SINCE 9/30/78.
CLJ
CLJ WRITE(6,110)
CLJ 110 FORMAT (2H1 ,* KK ALPHA BETA KAPPA CLOTHK

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115      $      T      R      *
111 CONTINUE
DO 30 KK = 1,14
SGT = (SIGS(I-1, KK) + (SIGT(I, KK) - SIGT(I-1, KK))) * XX * DMO(KK) * 1.E-3
SGS = (SIGS(I-1, KK) + (SIGS(I, KK) - SIGS(I-1, KK))) * XX * DMO(KK) * 1.E-3
IF(KK.GT. 10) SGT = 2.*PI*RD(KK)**2 * DMO(KK) * 1.E-3
IF(KK.GT. 10) SGS = 0.5*(1.*W1)*SGT
XWU = XWUBAR(I-1, KK) + (XWUBAR(I, KK) - XWUBAR(I-1, KK)) * XX
SGTR = SGT - XWU * SGS
GO TO 27
DD = SGS / (3.*SGT*SGTR)
DK = SQRT((SGT - SGS)/DD)
DA = 0.25 * SGS / SGT
DALFA(KK) = DA
DBETA(KK) = DD / 2.
DKAPPA(KK) = DK
X = DKAPPA(KK) * CLDTH(KK)
Y = DALFA(KK) / (DKAPPA(KK) * DBETA(KK))
TKK = T(X, Y)
RKK = R(X, Y)
WRITE(6,120) KK, DALFA(KK), DBETA(KK), DKAPPA(KK), CLDTH(KK), TKK, RKK
120 FORMAT (5X, I3, IP6E12.4)
27 CONTINUE
CLJ
CLJ
CLJ
CLJ
140      WE NOW COMPUTE THE MODIFIED DIFFUSION PARAMETERS FOR AN
      ABSORBING MEDIUM.
C = SGS/SGT
CALL LINEAR( C, XTRAPC, CXTRAP, XTRAP, MXTRPC )
CALL LINEAR( C, RELAXC, CRELAX, RELAX, HRELAX )
DD = (1.-C)/(RELAXC*RELAXC*SGTR)
DKAPPA(KK) = RELAXC*SQRT( SGT*SGTR )
DBETA(KK) = DD/2.
DALFA(KK) = DBETA(KK)*DKAPPA(KK)/(XTRAPC*RELAXC)
GO TO 29
X = DKAPPA(KK) * CLDTH(KK)
Y = DALFA(KK)/(DKAPPA(KK) * DBETA(KK))
TKK = T(X, Y)
RKK = R(X, Y)
WRITE(6,120) KK, DALFA(KK), DBETA(KK), DKAPPA(KK), CLDTH(KK), TKK, RKK
29 CONTINUE
30 RETURN
END

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1      I      FUNCTION DSURF(THETA,PHI,K)
2      C EVALUATES ELLIPSOIDAL SURFACE ELEMENT AT THETA,PHI
3      C ( INPUT ANGLES IN RADIAN )
4      C
5      COMMON/CCORD/ XI( 1,20),ETA( 1,20),ZETA( 1,20),
6      X , ASQ(20),BSQ(20),CSQ(20)
7      2 ,CPHIBAR(16,20),CTHBAR(8,20),CKRAR(4,4,20),CAREA(4,4,20)
8
9      CCC
10     CLJ      INPUT PARAMETERS
11     CLJ      ARGUMENT LIST
12     CLJ      THETA = POLAR ANGLE IN CLOUD-CENTERED COORDINATE SYSTEM
13     CLJ      AT WHICH FUNCTION DSURF IS TO BE EVALUATED, RADIAN
14     CLJ      PHI = AZIMUTHAL ANGLE IN CLOUD-CENTERED COORDINATE
15     CLJ      SYSTEM AT WHICH FUNCTION DSURF IS TO BE EVALUATED,
16     CLJ      RADIAN
17     CLJ      K = CLOUD-NUMBER INDEX
18
19     CLJ      CORD COMMON
20     CLJ      FOLLOWING PARAMETERS ARE SET IN SUBROUTINE CLDGEOM FOR
21     CLJ      K=1,NCLOUD (1,4,20)
22     CLJ      ASQ(K) = SQUARE OF LENGTH A, THE SEMI-MAJOR AXIS IN
23     CLJ      HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, K**2
24     CLJ      BSQ(K) = SQUARE OF LENGTH B, THE SEMI-MINOR AXIS IN
25     CLJ      HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, K**2
26     CLJ      CSQ(K) = SQUARE OF LENGTH C, THE SEMI-MINOR AXIS IN
27     CLJ      VERTICAL DIRECTION OF ELLIPSOIDAL CLOUD, K**2
28
29     CLJ      OUTPUT PARAMETER
30     CLJ      FUNCTION
31
32     CLJ      DSURF = FOR CLOUD K, THE PRODUCT OF SIN(THETA) AND THE
33     CLJ      ELLIPSOIDAL SURFACE AREA PER UNIT SOLID ANGLE IN
34     CLJ      THE DIRECTION (THETA,PHI), ( SIN(THETA)*PH**2)/SR
35
36     ST = SIN(THETA)
37     CT = COS(THETA)
38     SP = SIN(PHI)
39     CP = COS(PHI)
40     R = ST*ST*(CP*CP/ASQ(K)+SP*SP/BSQ(K))+CT*CT/CSQ(K)
41     RSQ = 1. / R
42     S = RSQ * ST*CT*(CP*CP/ASQ(K)+SP*SP/BSQ(K) - 1./CSQ(K) )
43     T = RSQ*ST*SP*CP* (1./ASQ(K) - 1. / BSQ(K) )
44     DSURF=RSQ*ST*SQRT(1.0+S*S+T*T)
45     RETURN
46     END

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1      SUBROUTINE ESURF(T1,T2,T3,T4,MSM,DD,T7,T8,T9,T10,T11,SFR,EPSPD,TKS)
2      ESURF
3      ESURF
4      ESURF
5      THIS IS A DUMMY ROUTINE REQUIRED IF THE CLOUD PACKAGE
6      IS EXERCISED AS A STAND-ALONE PROGRAM.
7      ESURF
8      INPUT PARAMETERS(SELECTED)
9      ESURF
10     ARGUMENT LIST
11     MSM = INDEX FOR CATEGORY OF SURFACE MATERIAL.
12     = 1, LAMBERTIAN DIFFUSE SURFACE WITH SPECTRALLY-
13     INDEPENDENT REFLECTANCE SET BY DD(1) AND
14     EMISSIVITY BY (1-DD(1)).
15     DD(M) = ADDITIONAL DESCRIPTOR FOR SELECTED SURFACE
16     MATERIAL.
17     FOR M = 1, (LAMBERTIAN SURFACE), DD(1) = DIFFUSE
18     REFLECTANCE. TYPICAL VALUE IS 0.10
19     OUTPUT PARAMETERS
20     ARGUMENT LIST
21     SFR = PSUBR(M,DD(M),ZLAM*THI,THR,PSI)
22     = BIDIRECTIONAL REFLECTANCE DISTRIBUTION
23     FUNCTION, 1./SR
24     EPSPD = 1.0 - RHOSUBM(ZLAM*THETA,2*PI)
25     TKS = SURFACE TEMPERATURE, DEG K.
26     DIMENSION DD(7)
27     DATA PI / 3.14159265 /
28     SFR = DD(1)/PI
29     EPSPD = 1.0-DD(1)
30     TKS = 288.
31     RETURN
32     END
33     ESURF

```


1	FUNCTION IPRIIME(II)	IP	2
	IPRIIME = AND(KOR(II-1,4)*1-II ,II-1), 3) + 1	IP	3
		IP	4
5	THE VALUES THAT IPRIIME SHOULD RETURN ARE GIVEN IN SUBROUTINE	IP	5
	CLOGEON FOR II=1,16.	IP	6
	NOTE...	IP	7
	USING THIS ROUTINE MAY GIVE ERRONEOUS RESULTS.	IP	8
		IP	9
10	FOR CERTAIN VALUES OF THE INPUT VARIABLE II	IP	10
	A ONE'S COMPLEMENT MACHINE (CDC-6600, CDC-7600)	IP	11
	AND A TWO'S COMPLEMENT MACHINE (IBM-360, IBM-370)	IP	12
	DO NOT RETURN THE SAME VALUE FOR IPRIIME.	IP	13
		IP	14
		IP	15
15	A MACHINE INDEPENDENT SCHEME SHOULD BE USED.	IP	16
		IP	17
	RETURN	IP	18
	END	IP	19

CCC
 CLJ
 CLJ
 CLJ
 CLJ
 CLJ
 CCC
 CLJ
 CLJ
 CLJ
 CLJ
 CLJ
 CCC
 CLJ
 CCC

```

1      SUBROUTINE LINEAR(XO,FXO,XX,FX,XX,NX)
2      CCC
3      C
4      C      GIVEN THE INDEPENDENT VARIABLE ARRAY, XX(1), AND THE
5      C      CORRESPONDING DEPENDENT VARIABLE ARRAY, FX(1), AND THE
6      C      SUBROUTINE LINEAR WILL DO A LINEAR INTERPOLATION AND
7      C      RETURN FXO AT A GIVEN XO.
8      C
9      C      NX IS THE LENGTH OF THE ARRAYS XX AND FX.
10     C
11     C      IF XO IS NOT WITHIN THE RANGE OF XX(1), FXO IS SET TO ZERO.
12     C
13     C      DIMENSION XX(1), FX(1)
14     C      IF( XO .LT. XX(1) .OR. XO .GT. XX(NX) ) GO TO 22
15     C      NX1 = 1
16     C      NX3 = NX
17     C      IF(NX.EQ.2) GO TO 6
18     C      NX2 = (NX1 + NX3)/2
19     C      IF( XO-XX(NX2) ) 4,18,10
20     C      4 IF( NX2-NX1-1 ) 8,6,8
21     C      6 NX1 = NX1
22     C      GO TO 16
23     C      8 NX3 = NX2
24     C      GO TO 2
25     C      10 IF( NX3-NX2-1 ) 14,12,14
26     C      12 NX1 = NX2
27     C      GO TO 16
28     C      14 NX1 = NX2
29     C      GO TO 2
30     C      16 FXO = FX(NX) + ( XO-XX(NX) )*( FX(NX+1)-FX(NX) )/
31     C      X ( XX(NX+1)-XX(NX) )
32     C      GO TO 20
33     C      18 FXO = FX(NX2)
34     C      20 RETURN
35     C      22 FXO = 0.0
36     C      RETURN
37     C      END

```



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1      SUBROUTINE LOS(K)
2
3      C
4      C
5      C
6      C
7      C
8      C
9      C
10     C
11     C
12     C
13     C
14     C
15     C
16     C
17     C
18     C
19     C
20     C
21     C
22     C
23     C
24     C
25     C
26     C
27     C
28     C
29     C
30     C
31     C
32     C
33     C
34     C
35     C
36     C
37     C
38     C
39     C
40     C
41     C
42     C
43     C
44     C
45     C
46     C
47     C
48     C
49     C
50     C
51     C
52     C
53     C
54     C
55     C
56     C
57     C
58     C

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TO BE CALLED FOR EACH CLOUD

SUBROUTINE LOS COMPUTES THE DIRECTION COSINES, IN THE EARTH-CENTERED CARTESIAN SYSTEM, OF A SELECTED SET OF LINE-OF-SIGHTS FROM THE DETECTOR TO FACETS OF THE DETERMINISTIC CLOUDS. THE ALTITUDE AT WHICH EACH LOS INTERCEPTS A FACET IS ALSO COMPUTED. THE SELECTED SET OF LINES-OF-SIGHT CONSISTS OF TWO SUBSETS. THE FIRST SUBSET CONSISTS OF THOSE TO REFLECTIVE POINTS (I-E., VISIBLE TO DETECTOR AND SOURCE), THE SECOND TO DIFFUSIVE POINTS (VISIBLE TO DETECTOR BUT NOT TO SOURCE). BY CONSIDERING ONLY EVERY OTHER FACET, ONE HAS ONLY 32 (INSTEAD OF 128) POINTS ON THE ELLIPSOID OF WHICH A MAXIMUM OF 16 ARE VISIBLE TO THE DETECTOR. ANY REFLECTIVE POINT THAT WOULD BE LESS THAN 0.7*SORI(FOV) FROM ANOTHER REFLECTIVE POINT IS ELIMINATED. DIFFUSIVE POINTS ARE LIMITED TO A MAXIMUM OF EIGHT CLOSEST TO THE PERIMETER OF THE CLOUD.

INPUT PARAMETERS

ARGUMENT LIST

DETECT COMMON

K = DETERMINISTIC CLOUD NUMBER (SET IN DRIVER)

HD = ALTITUDE OF DETECTOR, KM

THETAD = COLATITUDE OF DETECTOR, DEGREES

PHID = EAST LONGITUDE OF DETECTOR, DEGREES

FOV = FIELD OF VIEW OF DETECTOR AT EARTH'S SURFACE, KM**2

COORD COMMON

XI(I,K) = COORDINATES OF SOURCE-I IN K-TH CLOUD-CENTERED

ETA(I,K) = CARTESIAN SYSTEM, KM I=1, 20 K=1, 20

ZETA(I,K) = (SET IN CLOUD1)

XID(K) = COORDINATES OF DETECTOR IN K-TH CLOUD-CENTERED

ETAD(K) = CARTESIAN SYSTEM, KM K=1, 20

ZETAD(K) = (SET IN CLOUD1)

CTHBAR(I,K) = POLAR ANGLE IN CLOUD-CENTERED COORDINATES OF THE CENTER OF THE I-TH POLAR SET OF SURFACE FACETS FOR ELLIPSOIDAL CLOUD-K, DEGREES I=1, 8 K=1, 20

C*PHIBAR(J,K) = AZIMUTHAL ANGLE IN CLOUD-CENTERED COORDINATES OF THE CENTER OF THE J-TH AZIMUTHAL SET OF SURFACE FACETS FOR ELLIPSOIDAL CLOUD-K, DEGREES J=1, 16 K=1, 20

CRBAR(I,J,K) = CLOUD-CENTERED RADIAL DISTANCE TO THE CENTER OF SURFACE FACET I, J IN PRINCIPAL OCTANT, KM I=1, 4 J=1, 4 K=1, 20

(RESULTS FOR OTHER OCTANTS ARE OBTAINED BY SYMTY.)

CLOUD COMMON

H*CLOUD(K) = ALTITUDE OF CLOUD-K CENTER ABOVE THE SURFACE, KM K=1, N*CLOUD (READ IN CLOUD0)

OUTPUT PARAMETERS

LOS COMMON

HL*LOS(I,L) = ALTITUDE AT WHICH LOS FROM DETECTOR INTERCEPTS I-TH FACET OF (IMPLICITLY) CLOUD-K, KM (I-E. L-LE-16)

UL*LOS(I,L) = DIRECTION COSINES, IN EARTH-CENTERED CARTESIAN

VL*LOS(I,L) = SYSTEM, OF ABOVE-DESCRIBED LINES-OF-SIGHT.

ML*LOS(I,L) = FOR THESE VARIABLES, (I-E. L-LE-16). MAXIMUM

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60      CLJ      VALUE OF L DETERMINED BY INTERNAL SELECTION
      CLJ      PROCESS ACCORDING TO SEVERAL CRITERIA.
      CLJ
      COMMON/CLOUD/ NCLOND,
      1 HCLUD(20),THETCD(20),PHICD(20),CLOUDA(20),CLOUDB(20),
      2 CLOUDC(20),CLOPSI(20),KCLUD(20)
      COMMON/CDCORD/ X(1,20),ETA(1,20),ZETA(1,20),
      1 XID(20),ETAD(20),ZETAD(20),CPH(5,20),CTH(5,20)
      X ASQ(20),BSQ(20),CSQ(20)
      2 CPHBAR(16,20),CTHBAR(8,20),CRBAR(4,4,20),CAREA(4,4,20)
      COMMON /PARAMS/ IN,LOUT,PL,KE, DTR,RTD
      COMMON / DETECT/ HD, THSTAD,PHID,FOV
      COMMON/ LOS / HLOS(1,16),ULOS(1,16),VLOS(1,16),WLOS(1,16)
      DIMENSION THSCAT(8,16),PSS(8,16),PDD(8,16)
      DIMENSION THSCAT(8,16),XX(8,16),YY(8,16),ZZ(8,16)
      DIMENSION THS(16),II(16),JJ(16),IS(16),JS(16)

75      THE ARITHMETIC FUNCTION CTSCAT COMPUTES THE COSINE OF THE
      SCATTERING ANGLE OF A PHOTON MOVING FROM THE SOURCE AT POINT
      (X1,Y1,Z1) TO THE CENTER OF AN ELLIPSOIDAL-SURFACE FACET AT
      POINT (X,Y,Z) AND THEN DIRECTLY TO THE DETECTOR AT POINT
      (X2,Y2,Z2). COORDINATES ARE IN CLOUD-K CARTESIAN SYSTEM.
      CTSCAT( X,Y,Z,X1,Y1,Z1,X2,Y2,Z2 ) =
      1 ( (X-X1)*(X2-X) + (Y-Y1)*(Y2-Y) + (Z-Z1)*(Z2-Z) ) /
      2 SQR( ((X-X1)**2 + (Y-Y1)**2 + (Z-Z1)**2) *
      3 ((X2-X)**2 + (Y2-Y)**2 + (Z2-Z)**2) )

85      CALL POL TO CT( HD+RE,THETAD,PHID,XD,YD,ZD )
      NS = 1

      LOOP OVER FACETS TO DETERMINE THEIR VISIBILITY TO DETECTOR
      AND TO SOURCE.
      WE HAVE ADOPTED J. CARBAPINO'S SUGGESTION TO REDUCE THE NUMBER
      OF FACETS EXAMINED BY CONSIDERING ONLY EVERY OTHER FACET.
      THIS RESULTS IN THE FOLLOWING (I,J) SETS FOR THE 32 POINTS...
      1,1 1,3 ... 1,15
      3,1 3,3 ... 3,15
      5,1 5,3 ... 5,15
      7,1 7,3 ... 7,15

      DO 40 I=1,8,2
      1P= IPRIHE(I)
      DO 40 J=1,16,2
      JP= IPRIHE(J)
      P1= PS( XI(YS,K),ETA(NS,K),ZETA(NS,K),CTHBAR(I,K),CPHIBAR(J,K),K )
      P2= PS( XID(K),ETAD(K),ZETAD(K),CTHBAR(I,K),CPHIBAR(J,K),K )
      PSS(I,J)= P1
      PDD(I,J)= P2

      CALL POL TO CT( CRBAR(IP,JP,K),CTHAR(I,K),CPHIBAR(J,K),
      X XX(I,J),YY(I,J),ZZ(I,J) )

      DETERMINE COSINE OF SCATTERING ANGLE (AS DEFINED ABOVE).
      THSCAT(I,J)=CTSCAT(XX(I,J),YY(I,J),ZZ(I,J),XI(NS,K),ETA(NS,K),
      X ,ZETA(NS,K),XID(K),ETAD(K),ZETAD(K) )

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59 LOSK
 60 LOSK
 61 LOSK
 62 CLOUD
 63 CLOUD
 64 CLOUD
 65 CDCORD
 66 CDCORD
 67 CDCORD
 68 CDCORD
 69 CDCORD
 70 PARAMS
 71 DET
 72 LOS
 73 LOSK
 74 LOSK
 75 LOSK
 76 LOSK
 77 LOSK
 78 LOSK
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 109 LOSK
 110 LOSK


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115      IF( PL-GT. 0. -AND. P2 -GT. 0.) IDISC(I,J) = 1
120      IF( PL-GT. 0. -AND. P2 -LT. 0.) IDISC(I,J) = 2
125      IF( PL-LT. 0. -AND. P2 -GT. 0.) IDISC(I,J) = 3
130      IF( PL-LT. 0. -AND. P2 -LT. 0.) IDISC(I,J) = 4
135      40 CONTINUE
140      DO 45 L=1,64
145      RLOS(L,L) = 0.0
150      45 CONTINUE
155      ORDER THE POINTS
160      SORT THE FACET-CENTERS VISIBLE TO BOTH SOURCE AND DETECTOR IN
165      ORDER OF INCREASING SCATTERING ANGLE.
170      L = 0
175      DO 60 I=1,8,2
180      DO 60 J=1,16,2
185      IF(IDISC(I,J) -NE. 1) GO TO 60
190      L = L + 1
195      THS(L) = THSCAT(I,J)
200      ESTABLISH INDEX-ARRAYS FOR IDISC-1 POINTS.
205      II(LL) = I
210      JJ(LL) = J
215      LL = 0
220      60 CONTINUE
225      IF(L -EQ. 0) GO TO 75
230      SORTING FROM HIGH TO LOW IN COSINE CORRESPONDS TO SORTING FROM
235      LOW TO HIGH IN SCATTERING ANGLE.
240      CALL SORTL3(THS,II,JJ,L,1)
245      THE FIRST CANDIDATE POINT IS AUTOMATICALLY MADE THE FIRST
250      SELECTED POINT.
255      LL = 1
260      ABBREVIATE INDEXES OF FIRST SELECTED POINT TO AID IN GETTING
265      ITS LOS VECTOR.
270      IC = II(LL)
275      JC = JJ(LL)
280      ESTABLISH INDEX-ARRAYS FOR SELECTED POINTS, IS(LL) AND JS(LL).
285      IS(LL) = II(LL)
290      JS(LL) = JJ(LL)
295      CALL CLD C TO E(R,T,PH,XX(IC,JC),YY(IC,JC),ZZ(IC,JC),K)
300      CALL POL TO CT(R,I,PH,XC,YC,ZC)
305      RR = SQRT( (XD-KC)**2 + (YD-YC)**2 + (ZD-ZC)**2 )
310      RLOS(NS,LL) = R - RE
315      ULOS(NS,LL) = ( XC - XD ) / RR
320      VLOS(NS,LL) = ( YC - YD ) / RR
325      WLOS(NS,LL) = ( ZC - ZD ) / RR
330      CHECK REST OF CANDIDATE POINTS, FOR WHICH L= THEIR TOTAL NO.
335      DO 70 I = 2,L
340      ABBREVIATE INDEXES OF CANDIDATE POINT.
345      IC = II(I)
350      JC = JJ(I)
355      FOR EACH NEW (TRIAL) LOS WITHIN THE SFT SORTED WITH RESPECT TO

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175 CLJ      INCREASING SCATTERING ANGLE, FIND THE SEPARATION DISTANCE
      (SEPAR), MEASURED AT THE CLOUD AND NORMAL TO THE TRIAL LOS,
      FROM EACH PREVIOUSLY SELECTED LOS. THE TRIAL LOS IS REJECTED
      IF SEPAR IS LESS THAN THE ADOPTED CRITERION FOR ANY PREVIOUSLY
      SELECTED LOS.
      LL = NUMBER OF SELECTED POINTS.
      DO 65 KK = 1,LL
      IL = IS(KK)
      JL = JS(KK)
      CLJ      ABBREVIATE INDEXES OF THE SELECTED POINT BEING COMPARED WITH.
      CLJ      RDICJC = DISTANCE FROM DETECTOR TO CANDIDATE POINT (IC,JC)
      CLJ      RDILJL = DISTANCE FROM DETECTOR TO A SELECTED POINT (IL,JL)
      CLJ      RDICJC = SQRT( (XID(K)-XX(IC,JC))**2 + (ETAD(K)-VY(IC,JC))**2
      CLJ      $ + (ZETAD(K)-ZZ(IL,JC))**2 )
      CLJ      $ RDILJL = SQRT( (XID(K)-XX(IL,JL))**2 + (ETAD(K)-VY(IL,JL))**2
      CLJ      $ + (ZETAD(K)-ZZ(IL,JL))**2 )
      CLJ      DOT = COSINE OF ANGLE BETWEEN VECTORS FROM (1) DETECTOR TO
      CLJ      CANDIDATE POINT AND (2) DETECTOR TO A SELECTED POINT.
      CLJ      DOT = (
      CLJ      X ( XID(K) - XX(IC,JC) ) * ( XID(K) - XX(IL,JL) ) +
      CLJ      X ( ETAD(K) - VY(IC,JC) ) * ( ETAD(K) - VY(IL,JL) ) +
      CLJ      X ( ZETAD(K) - ZZ(IC,JC) ) * ( ZETAD(K) - ZZ(IL,JL) )
      CLJ      $ / (RDICJC*RDILJL)
      CLJ      IF(DOT .GT. 1.0) DOT = 1.0
      CLJ      SEPAR = RDICJC * ACOS( DOT )
      CLJ      IF( SEPAR .LT. 0.7*SQRT(FOV) ) GO TO 70
      CLJ      65 CONTINUE

200 C      CANDIDATE POINT HAS PASSED TEST. INCREMENT SELECTED-POINT
      CLJ      INDEX LL AND ADD SUCCESSFUL-CANDIDATE INDEXES TO THOSE OF
      CLJ      SELECTED POINTS. PROCEED TO OBTAIN LOS VECTOR OF NEWLY-
      CLJ      SELECTED POINT.
      CLJ      LL = LL + 1
      CLJ      IS(LL) = IC
      CLJ      JS(LL) = JC
      CLJ      CALL CUD C TO E(R,T,PH,XX(IC,JC),VY(IC,JC),ZZ(IC,JC),K)
      CLJ      WLOS(NS,LL) = R - RE
      CLJ      CALL POL TO CT(R,T,PH,XX,VC,ZC)
      CLJ      RR = SQRT( (XD-XC)**2 + (YD-YC)**2 + (ZD-ZC)**2 )
      CLJ      WLOS(NS,LL) = ( XC - XD ) / RR
      CLJ      WLOS(NS,LL) = ( YC - YD ) / RR
      CLJ      WLOS(NS,LL) = ( ZC - ZD ) / RR
      CLJ      70 CONTINUE
      CLJ      75 CONTINUE
      CLJ      SAVE THE NUMBER OF POINTS, LLI=LL, SELECTED FROM THOSE HAVING
      CLJ      IDISC=1.
      CLJ      LLI = LL
      CLJ      C
      CLJ      SORT THE FACET-CENTERS VISIBLE TO DETECTOR BUT NOT TO SOURCE IN
      CLJ      ORDER OF THEIR CLOSENESS TO THE TERMINATOR AS VIEWED FROM THE
      CLJ      DETECTOR. FUNCTION PS IS POSITIVE FOR SUCH POINTS AND RANGES
      CLJ      FROM ZERO FOR A POINT ON THE TERMINATOR TO +1.0 FOR A POINT
      CLJ      WHOSE ELLIPSOIDAL-SURFACE NORMAL LIES ANTIPARALLEL TO THE LOS.
      CLJ      L = 0
      CLJ      DO 80 I=1,3,2
      CLJ      DO 80 J=1,16,2
      CLJ      IF(IDISC(I,J) .NE. 3) GO TO 80

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230      L = L + 1
      THS (L) = PDD(L,J)
      ESTABLISH INDEX-ARRAYS FOR IDISC-3 POINTS.
      CLJ      II(L) = I
                JJ(L) = J
      80 CONTINUE
235      CLJ      SAVE THE NUMBER OF IDISC-3 POINTS, LL3=L.
                LL3 = L
                IF (L.EQ. 0) GO TO 95
                CALL SORTLJ(THS,II,JJ,L,-1)
240      CLJ      LIMIT THE DIFFUSIVE POINTS TO THOSE CLOSEST TO THE PERIMETER.
                THIS LIMIT WOULD BE 16 IF 128 FACETS WERE CONSIDERED BUT IS
                ONLY 8 IF 32 FACETS ARE CONSIDERED.
                LMAX1 = MIN0(L,R)
245      CLJ      DO 90 I = 1,LMAX1
                INCREMENT SELECTED-POINT INDEX LL, ABBREVIATE INDEXES OF
                IDISC-3 POINT, AND PROCEED TO GET ITS LOS VECTOR.
                LL = LL + 1
                IC = II(I)
                JC = JJ(I)
                CALL CLD C TO R(R,T,PH,XX(IC,JC),YY(IC,JC),ZZ(IC,JC),K)
250      CLJ      HLOS(NS,LL) = R - RE
                CALL POL TO CT(R,T,PH,XC,YC,ZC)
                RR = SQRT( (XD-XC)**2 + (YD-YC)**2 + (ZD-ZC)**2 )
                DLOS(NS,LL) = ( XC - XD ) / RR
255      CLJ      VLOS(NS,LL) = ( YC - YD ) / RR
                WLOS(NS,LL) = ( ZC - ZD ) / RR
                90 CONTINUE
                95 CONTINUE
C
260      1001 WRITE(6,1001) (L,ULOS(1,L),VLOS(1,L),WLOS(1,L),L=1,LL)
                FORMAT(* LOS LL UVM*13,1P3E20.12)
                WRITE(6,1002) LL1
265      1002 FORMAT (44H0 NUMBER OF SELECTED LOS FOR IDISC=1 IS LL1=,I5)
C
                1003 WRITE(6,1003) LL3
                FORMAT (44H0 NUMBER OF SELECTED LOS FOR IDISC=3 IS LL3=,I5)
                RETURN
                END

```

```

1      CLJ      FUNCTION PS(XI,ETI,ZET1,THETA,PHI,K)
2      PS
3      PS
4      PS      FUNCTION PS IS A QUANTITY WHOSE SIGN DETERMINES THE VISIBILITY OF
5      CLJ      A POINT (THETA,PHI) ON THE ELLIPSOIDAL CLOUD SURFACE FROM AN
6      PS      EXTERIOR POINT.
7      PS
8      PS      INPUT PARAMETERS
9      PS
10     PS      ARGUMENT LIST
11     PS      XI, = COORDINATES OF AN EXTERIOR POINT (WHICH MAY BE
12     CLJ      EITHER THE SOURCE OR THE DETECTOR) IN THE K-TH
13     PS      CLOUD-CENTERED CARTESIAN COORDINATE SYSTEM, KM
14     CLJ      NOTE. THE COORDINATES ARE XI(1,K), ETI(1,K),
15     CLJ      ZET1(1,K) IF THE POINT IS AT THE SOURCE AND
16     CLJ      XID(K), ETAD(K), ZETA(K) IF AT THE DETECTOR.
17     CLJ      THETA, = POLAR AND AZIMUTHAL COORDINATES OF A GIVEN FACET
18     CLJ      PHI, = CENTER ON CLOUD K
19     CLJ      K = CLOUD NUMBER K=1,20
20     CLJ      CORDO COMMON
21     CLJ      FOLLOWING PARAMETERS ARE SET IN SUBROUTINE CLODEON FOR
22     CLJ      K=1,10
23     CLJ      ASQ(K) = SQUARE OF LENGTH A, THE SEMI-MAJOR AXIS IN
24     CLJ      HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2
25     CLJ      BSQ(K) = SQUARE OF LENGTH B, THE SEMI-MINOR AXIS IN
26     CLJ      HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2
27     CLJ      CSQ(K) = SQUARE OF LENGTH C, THE SEMI-MINOR AXIS IN
28     CLJ      VERTICAL DIRECTION OF ELLIPSOIDAL CLOUD, KM**2
29     CLJ      PARAMS COMMON
30     CLJ      DTR = CONVERSION FACTOR FROM DEGREES TO RADIANS
31     CLJ      FUNCTION
32     CLJ      PS = QUANTITY PROPORTIONAL TO THE DOT PRODUCT OF THE
33     CLJ      OUTWARD NORMAL AT THE POINT (THETA,PHI) AND THE
34     CLJ      VECTOR FROM THE POINT (THETA,PHI) TO THE EXTERIOR
35     CLJ      POINT. THE CALLING SUBROUTINE (EITHER LOS OR
36     CLJ      CLOUD3) DETERMINES THAT THE POINT IS VISIBLE IF
37     CLJ      PS IS POSITIVE AND HIDDEN IF PS IS ZERO OR
38     CLJ      NEGATIVE. (THE UNITS HAPPEN TO BE 1/KM, BUT
39     CLJ      THAT IS UNIMPORTANT.)
40     CLJ      COMMON/CORDO/ XI( 1,20),ETI( 1,20),ZETA( 1,20),
41     CLJ      XID(20),ETAD(20),ZETAD(20),CPH(5,20),CTH(5,20)
42     CLJ      ASQ(20),BSQ(20),CSQ(20)
43     CLJ      CPHIBAR(16,20),CTHBAR(8,20),CRBAR(4,4,20),CAREA(4,4,20)
44     CLJ      COMMON /PARAYS/ IM,IOUT,PI,RE, DTR,RTD
45     CLJ      IS THE POINT(THETA,PHI) ON THE ELLIPSOID SURFACE
46     CLJ      VISIBLE TO THE POINT XI,ETI,ZETA
47     CLJ      ST = SIN(THETA*DTR)
48     CLJ      CT = COS(THETA*DTR)
49     CLJ      SP = SIN(PHI*DTR)
50     CLJ      CP = COS(PHI*DTR)
51     CLJ      R = 1. / SQRT(ST*ST*CP*CP/ASQ(K)+ST*ST*SP*SP/BSQ(K)+
52     CLJ      CT*CT/CSQ(K))
53     CLJ      PS = XI*ST*CP/ASQ(K) + ETI*ST*SP/BSQ(K) + ZET1*CT/CSQ(K) - 1./R
54     CLJ      RETURN
55     CLJ      END

```



```

1      FUNCTION RHOEPS(ALAM,CTHETA)
2      RHOEPS
3      RHOEPS
4      ALAM IS WAVELENGTH IN MICRONS
5      CTHETA IS COS(CEXIT ANGLE)
6      RHOEPS IS DIRECTIONAL RHO
7      THE RHO TABLE COMES FROM CLOUD TYPE 4, I.E. CS
8      FOR 4 ANGLES AND 10 WAVELENGTHS
9      RHOEPS
10     DIMENSION TLAM(10),CTHET(4),RHO(4,10)
11     RHOEPS
12     FUNCTION RHOEPS COMPUTES THE HEMISPHERICAL-DIRECTIONAL
13     REFLECTANCE FROM THE (HORIZONTAL) SURFACE OF CLOUD-TYPE 4
14     (STRATOCUMULUS) FOR RADIATION OF WAVELENGTH ALAM REFLECTED INTO
15     ZENITH ANGLE ACOS(CTHETA).
16     RHOEPS
17     INPUT PARAMETERS
18     RHOEPS
19     ARGUMENT LIST
20     ALAM = WAVELENGTH, MICRONS
21     CTHETA = COSINE OF ZENITH ANGLE THETA
22     FUNCTION
23     RHOEPS = HEMISPHERICAL-DIRECTIONAL REFLECTANCE FOR
24     RADIATION OF WAVELENGTH ALAM REFLECTED AT ANGLE
25     THETA FROM THE NORMAL TO THE SURFACE OF A SEVI-
26     INFINITE SLAB OF CLOUD-TYPE 4 (STRATOCUMULUS)
27     DEFINITION OF DATA
28     RHO(L,N) = HEMISPHERICAL-DIRECTIONAL REFLECTANCE FOR
29     RADIATION OF WAVELENGTH TLAM(N) REFLECTED AT
30     ANGLE THETA(1)=ACOS(CTHET(1)) FROM THE NORMAL
31     TO THE SURFACE OF A SEMI-INFINITE SLAB OF
32     CLOUD-TYPE 4 (STRATOCUMULUS)
33     THETA(1) = 0.30,60,90 DEGREES
34     RHOEPS
35     FOR ABOVE VARIABLES I=1,4 AND N=1,10
36     RHOEPS
37     VALUES OF RHO(L,N) ARE DERIVED FROM THE BIDIRECTIONAL
38     REFLECTANCE DATA RFLN(J,K,1) IN FUNCTION CLDBDR BY THE
39     (SCHEMATIC) FORMULA...
40     RHO(L,N) = 2.*SUM( SUM( RFLN(J,K,1)*CTHOUT(J)*DELCTH(J)
41     *DELPHI(K) ) ) K=1,9 J=1,5
42     CTHOUT(J) = 0.1 + 0.2*(J-1) J=1,5
43     DELCTH(J) = 0.20 J=1,5
44     DELPHI(K) = PI/9. K=1,9
45     RHO(L,N) = (2.*PI/45.)*SUM( CTHOUT(J)*SUM( RFLN(J,K,1),
46     K=1,9 ), J=1,5 )
47     RHOEPS
48     THE MONTE CARLO RESULTS OBTAINED FOR AN INCIDENT ZENITH ANGLE
49     OF 80 DEGREES ARE APPLIED HERE AT THETA(4)=90 DEGREES, A
50     NECESSARY APPROXIMATION IN ORDER TO SPAN THE ENTIRE RANGE.
51     DATA TLAM / 2.,2.5,2.55,2.65,2.75,2.85,3.2,3.5,4.,5. /
52     DATA CTHET / 1.00,0.866,0.500,0.0 /
53     DATA RHO /
54     .246738, .337347, .438561, .582364,
55     .263120, .797961, .409229, .567398,

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60      CLJ      DTR = CONVERSION FACTOR FROM DEGREES TO RADIAN
        CLJ      PTE COMMON
        CLJ      P1, = PROBABILITY LEVELS (FRACTILES) AT WHICH TRANSFER
        CLJ      P2, COEFFICIENTS AND EMISSION RADIANCES ARE DESIRED.
        CLJ      P3,P4 SET IN DRIVER PROGRAM.
        CLJ      SOLARP COMMON
        CLJ      SOLLAT = NORTH LATITUDE OF SUBSOLAR POINT (RADIAN)
        CLJ      SOLLON = EAST LONGITUDE OF SUBSOLAR POINT (RADIAN)
        CLJ      SOURCE COMMON
        CLJ      HSOURCE(1) = ALTITUDE OF SOURCE-1 ABOVE SURFACE, KM
        CLJ      THETAS(1) = COLATITUDE OF SOURCE-1, DEGREES
        CLJ      PHIS(1) = EAST LONGITUDE OF SOURCE-1, DEGREES
        CLJ      RSOURCE(1) = RADIUS OF SOURCE-1, KM
        CLJ      OUTPUT PARAMETERS
        CLJ      FLAGS COMMON
        CLJ      IFLAG = 0 IF SUN IS BELOW THE HORIZON
        CLJ      IFLAG = 1 IF SUN IS ABOVE THE HORIZON
        CLJ      OR IF AN ARTIFICIAL SOURCE IS PRESENT
        CLJ      PTE COMMON
        CLJ      T1, = TRANSFER COEFFICIENTS AT 12-KM ALTITUDE FOR
        CLJ      T2, ARTIFICIAL POINT SOURCE, CORRESPONDING TO P1,P2,
        CLJ      T3, P3,P4. A TRANSFER COEFFICIENT IS THE RATIO OF A
        CLJ      T4, RADIANCE TO AN IRRADIANCE. (1/SR)
        CLJ      S1, = TRANSFER COEFFICIENTS AT 12-KM ALTITUDE FOR SUN AS
        CLJ      S2, A SOURCE, CORRESPONDING TO P1,P2,P3,P4. (1/SR)
        CLJ      S3,S4
        CLJ      E1, = THERMAL EMISSION (SPECTRAL RADIANCE) FROM TOP
        CLJ      E2, LAYER OF CLOUDS OR THE GROUND (FOR THE CLOUD-FREE
        CLJ      E3, LINE-OF-SIGHT), CORRESPONDING TO P1,P2,P3,P4.
        CLJ      E4 (WATTS/(KM**2 SR MICRON))
        CLJ      PCFLOS = PROBABILITY OF THE DETECTOR SEEING THE ARTIFICIAL
        CLJ      SOURCE, EITHER WITH CLOUDS PRESENT (FOR WHICH WE
        CLJ      HAVE USED A POSTULATED ALTITUDE-DEPENDENT CFLOS
        CLJ      FUNCTION) OR WITHOUT CLOUDS BEING PRESENT.
        CLJ      A VALUE OF 0.0 IS RETURNED IF THE SOURCE IS NOT
        CLJ      WITHIN THE FIELD-OF-VIEW.
        CLJ      COMMON /:CLDFREQ/ KMODEL,CCOVER(5,11),CFREQ(17,4,11)
        CLJ      COMMON / DETECT/ HD, THETA0,PHID,FOV
        CLJ      COMMON /PARAMS/ IN,LOUT,PL,KE, DTR,RTD
        CLJ      COMMON/SOURCE/ HSOURCE,HSOURCE(1),RSOURCE(1),THETAS(1),PHIS(1)
        CLJ      COMMON/CLDWT/IDK,WT(161),TRANS(161),EMISS(161)
        CLJ      COMMON/FLAGS/ IFLAG
        CLJ      COMMON/WATERL/MSM,DDM(7),SRFALT
        CLJ      COMMON/ PTE / P1,P2,P3,P4,T1,T2,T3,T4,
        CLJ      S1,S2,S3,S4,E1,E2,E3,E4
        CLJ      PCFLOS
        CLJ      COMMON /SANDP/ XS,YS,ZS,XD,YD,ZD,UL,VL,WL
        CLJ      COMMON/SOLARP/ SOLLAT,SOLLON,DUMDUM(10)
        CLJ      DIMENSION WT(161)
        CLJ      LOGICAL SPCULR,ESURF1
        CLJ      DATA RSN / 1.495979E+08 /
        CLJ      THE ARITHMETIC FUNCTION PLANK PROVIDES SPECTRAL RADIANCE AT
        CLJ      WAVELENGTH AA(MICRONS) AND TEMPERATURE TT(DEG KELVIN),
        CLJ      WATTS/(KM**2 SR MICRON))
        CLJ      PLANK(AA,TT) = 1.191E14/(AA**5*(EXP(14388./(AA*TT))-1.))
        CLJ      THE ARITHMETIC FUNCTIONS CFLOS AND CFLOS RESULT FROM OUR

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115 CLJ      POSTULATING A SIMPLE ALTITUDE-DEPENDENCE TO THE CFLOS
CLJ      FUNCTIONS FOR THE RESPECTIVE PATHS FROM (A) THE ARTIFICIAL
CLJ      SOURCE TO THE GROUND AND (B) THE ARTIFICIAL SOURCE TO THE
CLJ      DETECTOR. THE ALTITUDE-DEPENDENT FACTOR F IS DEFINED IN THE
CLJ      ROUTINE BEFORE USING THESE ARITHMETIC FUNCTIONS.
120 CFLOSQ( KQ,QA,QF ) = 1.0 - ( QF * (1.0-CFLOSQ( KQ,QA ) ) )
      CFLOSH( KQ,QA,QF ) = QF + (1.0-QF) * CFLOSQ( KQ,QA )
CLJ      UL = U
      VL = V
      WL = W
      C
      NS = 1
      ALT = HSOURCE(NS)
      IF( ISUN.EQ.0 ) CALL POL TO CT(ALT*RE,THETAS(NS),PHIS(NS),
      $ XS,YS,ZS)
      IF( ISUN.EQ.1 ) CALL POL TO CT(RSUN,90.-SOLLAT*RTD,SOLLON*RTD,
      $ XS,YS,ZS)
      HSAVE = HSOURCE(1)
      IF( ISUN.EQ.1 ) HSOURCE(1) = RSUN*RE
      CALL POL TO CT(HD*RE,THETAD,PHID,XD,YD,ZD)
      C
      THIS CALL TO SCEOM GETS (1) THE ANGLE TH1 USED TO TEST WHETHER
      OR NOT THE SUN IS ABOVE THE HORIZON AND (2) THE LOS ZENITH
      ANGLE THR FOR USE BY SUBROUTINE CLOUT IN CALLING CPOSP. THE
      ANGLE THR AND THE AZIMUTHAL ANGLE PSI ARE ALSO USED IN CALLING
      SUBROUTINE ESURF, AND THE ANGLE TH1 MAY ALSO BE USED IN THAT
      CALL. HOWEVER, IF THE SOURCE IS AN ARTIFICIAL ONE AND ITS
      ALTITUDE IS LESS THAN THE RADIUS ASSIGNED TO THE FINITE-S*OE
      SOURCE, IT IS THEN NECESSARY TO RESET THE ANGLE TH1 WITH
      ANOTHER CALL TO SUBROUTINE SCEOM BEFORE CALLING SUBROUTINE
      ESURF.
      CALL SCEOM(UL,VL,WL,SRFALT,XD,YD,ZD,XS,YS,ZS,
      $ ROIST,SDIST,TH1,THR,PSI)
      X
      IDAY = 1
      IF( TH1.GT.90. ) IDAY = 0
      ITFLAG = 1
      IF( IDAY.EQ.0 .AND. ISUN.EQ.1 ) ITFLAG = 0
      CALL DIFFRM TO GET DIFFUSION PARAMETERS
      FOR GIVEN WAVELENGTH FOR ALL 14 CLOUDS
      CALL DIFFRM(ALAM,THP)
      IL = IOX
      GET ESURF PARAMETERS
      ZLAM = ALAM
      ZKM = SRFALT
      IFIRS = 0.
      SPCULR = .FALSE.
      ESURF1 = .TRUE.
      C
      CLJ      RESET TH1 TO THIEFF AND SDIST TO SDEFF IF ISUN=0 AND
      CLJ      IF HSOURCE(1) .LT. RSOCE(1).
      IF( ISUN.EQ.1 ) .OR. (ALT.GE.RSOURCE(1)) ) GO TO 2
      SDEFF = 0.5*(ALT + RSOCE(1))
      CALL POL TO CT(HF*HSEFF,THETAS(NS),PHIS(NS),ISEFF,YSSEFF,ZSEFF)
      CALL SCEOM(UL,VL,WL,SRFALT,XD,YD,ZD,XS,YS,ZS,
      $ ROIST,SDIST,TH1,THR,PSI)
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175      $ SDIST = SDEFF
      THI = THIEFF
      FOR LATER USE, SAVE AND SET...
      HSAVE2 = HSOURCE(1)
      HSOURCE(1) = HSEFF
2 CONTINUE
180      CALL ESURF(THI,DTR,THR,DTR,PSI,DTR,ZKM,MSM,DM(1),
      X SPCULR,ZLAN,IDAV,IRCS,ESURF1,SEF,EYSD,TKS )
      T2TP = TAIR(ALAM,THR,ZKM)
      RMIS(1) = EPSD * PLANK(ALAM,TKS) * T2TP
      IF( IFLAG.EQ.0 ) GO TO 4
      WE NOW DEVELOP THE HEIGHT TO BE USED IN RESETTING WT(1) TO
      ACCOUNT FOR THE TWO-LEG CFLOS NEEDED TO VIEW THE SOURCE-LIT
      GROUND.
      IF THE ARTIFICIAL SOURCE WERE ABOVE THE TOP OF THE HIGHEST
      CLOUD TOP IN THE STATISTICAL MODEL (I.E., ABOVE 12-KM
      ALTITUDE), THE PROBABILITY OF THE DETECTOR SEEING THE SOURCE-
      LIT GROUND WOULD BE THE SAME AS THAT FOR THE SUN. IF THE
      ARTIFICIAL SOURCE WERE BELOW SUCH AN ALTITUDE, THEN IT IS
      LIKELY THAT THE VALUE OF AN APPROPRIATE CFLOSF(ICC,THI)
      WOULD BE LARGER THAN THAT FOR THE SUN, WITH THE EXACT AMOUNT
      DEPENDING ON THE ALTITUDE. SUCH A DATA BASE IS NOT READILY
      AVAILABLE (IF IT EXISTS AT ALL), SO WE SHALL USE AN
      APPROXIMATION. DEFINE THE FACTOR F...
      F = 1.0
      IF( HSOURCE(1).LT.12. ) F = 1. - (12. - HSOURCE(1)) / 11.85
      IF( HSOURCE(1).LT.0.15 ) F = 0.
      THEN THE POSTULATED CFLOS-FUNCTION FOR THE DOWNWARD LEG IS
      GIVEN BY THE ARITHMETIC FUNCTION CFLOSG(ICC,THI,F).
      NOTE THAT IF F=1, THEN CFLOSG(ICC,THI,1.)=CFLOSF(ICC,THI).
      THE PROBABILITY OF THE DETECTOR SEEING THE SOURCE-LIT GROUND
      THROUGH THE CLOUDS IS SLGCLO, GIVEN BY...
      SLGCLO = CCOVER(2,KMODEL) * CFLOSF( 4,THR ) * CFLOSG( 4,THI,F)
      + CCOVER(3,KMODEL) * CFLOSF( 6,THR ) * CFLOSG( 6,THI,F)
      + CCOVER(4,KMODEL) * CFLOSF( 9,THR ) * CFLOSG( 9,THI,F)
      + CCOVER(5,KMODEL) * CFLOSF(11,THR) * CFLOSG(11,THI,F)
      THE PROBABILITY OF SEEING THE SOURCE-LIT GROUND WITHOUT
      CLOUDS IS (ESSENTIALLY) SLGCLR...
      SLGCLR = CCOVER(1,KMODEL)
      WHICH SHOULD, IN A SENSE, BE MULTIPLIED BY THE TWO FACTORS
      CFLOSF(1,THR) AND CFLOSF(1,THI). WE SHALL NOT USE THE FACTORS
      HERE FOR CONSISTENCY WITH SUCH NONUSAGE ELSEWHERE IN THE CODE.
      (THE CONFUSION ARISES FROM THE AMBIGUITY IN THE LITERATURE AS
      TO WHAT IS MEANT BY A CLOUD COVER OF ZERO TENTHS, WHEN CFLOS
      IS LESS THAN UNITY FOR SUFFICIENTLY LARGE ZENITH ANGLES. A
      COMPLEMENTARY-TYPE AMBIGUITY EXISTS FOR A CLOUD COVER OF TEN
      TENTHS, WHEN CFLOS IS GREATER THAN ZERO.)
      THE PROBABILITY OF SEEING THE SOURCE-LIT GROUND EITHER WITH
      OR WITHOUT CLOUDS BEING PRESENT IS SLG...
      SLG = SLGCLO + SLGCLR
      IF( SLG.GT.1.0 ) SLG = 1.0
      TO REFERENCE THE TRANSFER COEFFICIENT TO 12-KM ALTITUDE, WE
      WERE SDISTO. IN DOING THIS WE USE THE ORIGINAL SOURCE
      POSITION, WITHOUT ANY RESETTING IF THE SOURCE IS ARTIFICIAL,

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230      CLJ      EVEN THOUGH ITS ALTITUDE MAY BE LESS THAN ITS RADIUS.
      TPALT = 12.
      CALL SGEOM(DL,VL,WL,TPALT,XD,YD,ZD,XS,YS,ZS,
      $      RDIST,SOISTO,THE1I,THE2I,PHIE)
      T12 = TAIR(ALAM,THI,ZKM)
      IF( HSORCE(1).LT.12. ) T12 = T12/TAIR(ALAM,THI,HSORCE(1))
      TRANS(11) = SPN*CDT(THI*OTR)*T12*T2TP*(SOISTO/SOIST)**2
      HSORCE(1) = HSAVF2
      4 CONTINUE
      CLJ      BEFORE DUPLICATING THE WT ARRAY AND BEFORE SORTING THE TRANS
      CLJ      AND EMISS ARRAYS, AUGMENT THE TRANS ARRAY WITH THE MEMBER
      CLJ      TRANS(11+1) = 0.0, THE EMISSION ARRAY WITH THE MEMBER
      CLJ      EMISS(11+1) = 0.0, AND THE WT ARRAY WITH THE MEMBER
      CLJ      WT(11+1) = 0.0. DOING THIS ALLOWS SUBROUTINE LINEAR TO
      CLJ      INTERPOLATE WITHIN ITS GIVEN ARRAY IF THE WEIGHT OF THE
      CLJ      NORMALLY SMALLEST MEMBER EXCEEDS THE SMALLEST FRACTILE (NOW
      CLJ      0.10) FOR WHICH AN INTEGRAL-DISTRIBUTION VALUE IS REQUESTED.
      IISAVE = 11
      11 = 11 + 1
      TRANS(11) = 0.0
      EMISS(11) = 0.0
      WT(11) = 0.0
      DO 5 I = 1,11
      5 WT(I) = WT(I)
      CLJ      NOW RESET WT(IISAVE) TO ACCOUNT FOR A TWO-LEG CFLOS.
      CLJ      IF( ITFLAG.NE.0 ) WT(IISAVE) = SLG
      C
      CLJ      SORT THE ARRAYS FOR TRANSEFER COEFFICIENT AND EMISSION, TRANS
      CLJ      AND EMISS, FROM LOW TO HIGH.
      C
      CLJ      IF( ITFLAG.NE.0 ) CALL SORTLJ(TRANS,WT,WT,11,0)
      CALL SORTLJ(EMISS,WT,WT,11,0)
      C      ACCUMULATE THE WEIGHTING FUNCTION AND NORMALIZE
      DO 10 I = 2,11
      WT(I) = WT(I-1) + WT(I)
      10 WT(1) = WT(1-1) + WT(1)
      DO 15 I = 1,11
      WT(I) = WT(I) / WT(11)
      15 WT(I) = WT(I) / WT(11)
      C
      CLJ      INTERPOLATE TO THE FRACTILES P1,P2,P3,P4 SET IN THE DRIVER.
      IF( ISUN.EQ.1 ) GO TO 22
      CALL LINEAR(P1,E1,WT1,EMISS,11)
      CALL LINEAR(P2,E2,WT1,EMISS,11)
      CALL LINEAR(P3,E3,WT1,EMISS,11)
      CALL LINEAR(P4,E4,WT1,EMISS,11)
      CALL LINEAR(P1,T1,WT,TRANS,11)
      CALL LINEAR(P2,T2,WT,TRANS,11)
      CALL LINEAR(P3,T3,WT,TRANS,11)
      CALL LINEAR(P4,T4,WT,TRANS,11)
      IF( ISUN.EQ.0 ) GO TO 24
      22 CONTINUE
      CALL LINEAR(P1,E1,WT1,EMISS,11)
      CALL LINEAR(P2,E2,WT1,EMISS,11)
      CALL LINEAR(P3,E3,WT1,EMISS,11)
      CALL LINEAR(P4,E4,WT1,EMISS,11)
      IF( ITFLAG.EQ.0 ) GO TO 24

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290      CALL LINEAR(P1,S1,WT,TRANS,II)
      CALL LINEAR(P2,S2,WT,TRANS,II)
      CALL LINEAR(P3,S3,WT,TRANS,II)
      CALL LINEAR(P4,S4,WT,TRANS,II)
294      CONTINUE
      SOURCE(1) = NSAVE
      IF( ISUN.EQ.1 ) GO TO 30
      FINALLY, WE RETURN TO THE USER THROUGH PTE COMMON. THE
      PROBABILITY (PCFLOS) OF SEEING THE ARTIFICIAL SOURCE
      (PROVIDED IT IS WITHIN THE FIELD-OF-VIEW), EITHER WITH CLOUDS
      BEING PRESENT (AND WITH ACCOUNT OF OUR POSTULATED ALTITUDE-
      DEPENDENT CFLOS FUNCTION) OR WITHOUT CLOUDS BEING PRESENT.
      PCFLOS = 0.0
      THE CHARACTERISTIC HALF-ANGLE OF THE FIELD-OF-VIEW IS
      TAKEN TO BE CHIFOV...
      CHIFOV = SQRT( FOV/PI ) / HD
      GET THE DIRECTION COSINES OF A VECTOR FROM THE DETECTOR
      TO THE SOURCE.
      RSD = SQRT( (XS-XD)**2 + (YS-YD)**2 + (ZS-ZD)**2 )
      US = (XS-XD)/RSD
      VS = (YS-YD)/RSD
      WS = (ZS-ZD)/RSD
      THE ANGLE BETWEEN THE INPUT LOS AND THE DETECTOR-TO-SOURCE
      VECTOR IS CHISL...
      CHISL = ACOS( US*UL + VS*VL + WS*WL )
      IF( CHISL.GT.CHIFOV ) GO TO 30
      PCFLOS = CCOVER(2,KMODEL) * CFLOSH( 4,THR,F)
      $      + CCOVER(3,KMODEL) * CFLOSH( 6,THR,F)
      $      + CCOVER(4,KMODEL) * CFLOSH( 9,THR,F)
      $      + CCOVER(5,KMODEL) * CFLOSH(11,THR,F) + CCOVER(1,KMODEL)
300      CONTINUE
      RETURN
      END

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1  SUBROUTINE SGEOM(UL,VL,AL,CLDTOP,XD,YD,ZD,XS,YS,ZS,
X RDIST,SDIST,THETI,THETE,PHIE )
COMMON/PARAMS/ IAL,IOUT,PI,RE, DTR,RTD
      ANGLES IN DEGREES AND DISTANCES IN KILOMETERS

5  INPUTS
      UL,VL,WL ARE LOS DIRECTION COSINES
      CLDTOP = CLOUD TOP ALTITUDE
      XD,YD,ZD - XS,YS,ZS DETECTOR AND SOURCE LOCATION..EARTH CENT

10 THIS IS CODE FOR THE INCIDENT AND EXIT LOOK ANGLES
      AND THE AZIMUTHAL ANGLE FOR SOURCE ABOVE THE CLOUD
      THE VECTOR RI IS TO THE CLOUD TOP FROM THE EARTH CENTER
      S IS THE DISTANCE FROM THE DETECTOR TO THE CLOUD TOP

15 THETI IS THE INCIDENT LOOK ANGLE
      THETE IS THE EXIT LOOK ANGLE
      PHIE IS THE AZIMUTHAL ANGLE I.E. THE ANGLE BETWEEN THE
      RS,RI PLANE AND THE RD,RI PLANE
      SDIST IS DISTANCE FROM SOURCE TO INTERSECTION OF CLOUD TOP AND
      LINE-OF-SIGHT (KILOMETERS)
      RDIST IS HORIZONTAL COMPONENT OF SDIST

20 SUBROUTINE SGEOM COMPUTES THE GEOMETRICAL RELATIONS BETWEEN
      A SOURCE, STATISTICAL CLOUD, AND DETECTOR.

25 INPUT PARAMETERS
      ARGUMENT LIST
      UL,VL,WL = DIRECTION COSINES IN THE GEOCENTRIC CARTESIAN
      COORDINATE SYSTEM OF THE LINE-OF-SIGHT (LOS)
      VECTOR FROM THE DETECTOR
      CLDTOP = ALTITUDE OF THE (STATISTICAL) CLOUD TOP INTER-
      SECTED BY THE LOS FROM THE DETECTOR, KM
      XD,YD,ZD = GEOCENTRIC CARTESIAN COORDINATES OF THE
      DETECTOR, KM
      XS,YS,ZS = GEOCENTRIC CARTESIAN COORDINATES OF THE
      SOURCE, KM

40 PARANS COMMON
      DTR = CONVERSION FACTOR FROM DEGREES TO RADIANS, PI/180
      RTD = CONVERSION FACTOR FROM RADIANS TO DEGREES, 180/PI
      RE = EARTH RADIUS, KM

45 OUTPUT PARAMETERS
      ARGUMENT LIST
      SDIST = DISTANCE FROM THE SOURCE TO THE INTERSECTION OF
      THE DETECTOR LOS VECTOR WITH THE HORIZONTAL
      SURFACE WHOSE ALTITUDE IS INPUTTED TO THIS
      ROUTINE AS CLDTOP, KM
      (INTERSECTION POINT DENOTED BY VECTOR RI IN THE
      GEOCENTRIC CARTESIAN COORDINATE SYSTEM)
      RDIST = COMPONENT OF SDIST NORMAL TO THE VECTOR RI, KM
      THETI = ZENITH ANGLE OF SOURCE AT POINT RI, DEGREES
      THETE = ZENITH ANGLE OF DETECTOR AT POINT RI, DEGREES
      PHIE = AZIMUTHAL ANGLE THROUGH WHICH A PHOTON IS
      DEFLECTED AT THE POINT RI WHILE GOING FROM THE
      SOURCE TO THE DETECTOR, DEGREES

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 SGEOM 3
 PARANS 2
 SGEOM 5
 SGEOM 6
 SGEOM 7
 SGEOM 8
 SGEOM 9
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 SGEOM 11
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60      RD = XD**2 + VD**2 + ZD**2
      S = UL*XD + VL*VD + WL*ZD
      S = -S - S*SQRT(S**2 - RD + (RE+CLDTP)**2)
      RD = SQRT(RD)
      XI = XD + S*UL
      VI = VD + S*VL
      ZI = ZD + S*WL

65      C
      C
      C
      READ THE VARIABLE NAMES AS
      R DMLDML MEANING (RD MINUS RI) DOT (RD MINUS RI) ETC.
      RDMLOMI = (XD-XI)*(XD-XI) + (VD-VI)*(VD-VI) + (ZD-ZI)*(ZD-ZI)
      RSMISMI = (XS-XI)*(XS-XI) + (YS-VI)*(YS-VI) + (ZS-ZI)*(ZS-ZI)
      SDIST = SQRT( RSMISMI )
      RISMI = XI * (XS-XI) + VI * (YS-VI) + ZI * (ZS-ZI)
      R DDOOTI = XD*XI + VD*VI + ZD*ZI
      R DDOOTS = XD*XS + VD*VS + ZD*ZS
      R SDOTI = XI*XS + VI*VS + ZI*ZS
      R IDOTI = XI*XI + VI*VI + ZI*ZI
      R DDOOTD = XD*XD + VD*VD + ZD*ZD
      R DDOOTS = XS*XS + VS*VS + ZS*ZS
      RS = SQRT( XS**2 + VS**2 + ZS**2 )
      US = XS / RS
      VS = VS / RS
      WS = ZS / RS
      RI = SQRT( RIDOTI )
      D1 = XI*US + VI*VS + ZI*WS
      D2 = XI*UL + VI*VL + ZI*WL
      D3 = UL*US + VL*VS + WL*WS
      THETE = ACOS( -D2/RI )
      THETI = ACOS( RISMI/( RI*SDIST ) )

80      C
      C
      C
      CHECK FOR COLINEARITY, IF SO, PHIE = 0
      PHIE = 1.0E-05
      IF(ABS (RSDOTS*RIDOTI / RSDOTI**2) .GT. .999999) GO TO 10
      IF(ABS (RDDOTD*RIDOTI / RDDOTI**2) .GT. .999999) GO TO 10
      PHIE = 0.0
      IF( (THETE.EQ.0.0) .OR. (THETI.EQ.0.0) ) GO TO 10
      PHIE = ACOS( (RI*COS(THETE)*D1 + RIDOTI*D3) /
      $      (RIDOTI*SIN(THETE)*SIN(THETI)) )
      10 CONTINUE
      THETE = THETE * RTD
      THETI = THETI * RTD
      PHIE = PHIE * RTD
      PDIST = SDIST * SIN(THETI*DTDR)
      RETURN
      END

90      C
      C
      C
      PHIE = 1.0E-05
      IF(ABS (RSDOTS*RIDOTI / RSDOTI**2) .GT. .999999) GO TO 10
      IF(ABS (RDDOTD*RIDOTI / RDDOTI**2) .GT. .999999) GO TO 10
      PHIE = 0.0
      IF( (THETE.EQ.0.0) .OR. (THETI.EQ.0.0) ) GO TO 10
      PHIE = ACOS( (RI*COS(THETE)*D1 + RIDOTI*D3) /
      $      (RIDOTI*SIN(THETE)*SIN(THETI)) )
      10 CONTINUE
      THETE = THETE * RTD
      THETI = THETI * RTD
      PHIE = PHIE * RTD
      PDIST = SDIST * SIN(THETI*DTDR)
      RETURN
      END

95      C
      C
      C
      PHIE = 1.0E-05
      IF(ABS (RSDOTS*RIDOTI / RSDOTI**2) .GT. .999999) GO TO 10
      IF(ABS (RDDOTD*RIDOTI / RDDOTI**2) .GT. .999999) GO TO 10
      PHIE = 0.0
      IF( (THETE.EQ.0.0) .OR. (THETI.EQ.0.0) ) GO TO 10
      PHIE = ACOS( (RI*COS(THETE)*D1 + RIDOTI*D3) /
      $      (RIDOTI*SIN(THETE)*SIN(THETI)) )
      10 CONTINUE
      THETE = THETE * RTD
      THETI = THETI * RTD
      PHIE = PHIE * RTD
      PDIST = SDIST * SIN(THETI*DTDR)
      RETURN
      END

100      C
      C
      C
      PHIE = 1.0E-05
      IF(ABS (RSDOTS*RIDOTI / RSDOTI**2) .GT. .999999) GO TO 10
      IF(ABS (RDDOTD*RIDOTI / RDDOTI**2) .GT. .999999) GO TO 10
      PHIE = 0.0
      IF( (THETE.EQ.0.0) .OR. (THETI.EQ.0.0) ) GO TO 10
      PHIE = ACOS( (RI*COS(THETE)*D1 + RIDOTI*D3) /
      $      (RIDOTI*SIN(THETE)*SIN(THETI)) )
      10 CONTINUE
      THETE = THETE * RTD
      THETI = THETI * RTD
      PHIE = PHIE * RTD
      PDIST = SDIST * SIN(THETI*DTDR)
      RETURN
      END

105      C
      C
      C
      PHIE = 1.0E-05
      IF(ABS (RSDOTS*RIDOTI / RSDOTI**2) .GT. .999999) GO TO 10
      IF(ABS (RDDOTD*RIDOTI / RDDOTI**2) .GT. .999999) GO TO 10
      PHIE = 0.0
      IF( (THETE.EQ.0.0) .OR. (THETI.EQ.0.0) ) GO TO 10
      PHIE = ACOS( (RI*COS(THETE)*D1 + RIDOTI*D3) /
      $      (RIDOTI*SIN(THETE)*SIN(THETI)) )
      10 CONTINUE
      THETE = THETE * RTD
      THETI = THETI * RTD
      PHIE = PHIE * RTD
      PDIST = SDIST * SIN(THETI*DTDR)
      RETURN
      END

```


2	SORTLJ
3	SORTLJ
4	SORTLJ
5	SORTLJ
6	SORTLJ
7	SORTLJ
8	SORTLJ
9	SORTLJ
10	SORTLJ
11	SORTLJ
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14	SORTLJ
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16	SORTLJ
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36	SORTLJ
37	SORTLJ
38	SORTLJ
39	SORTLJ

```

1      FUNCTION TAIR(ALAM,THETA,ALT)
2      DIMENSION T(10,6,4)
3      TAILR T(10,6,4)
4      DATA TAILR / 2.0,2.5,2.55,2.65,2.75,2.85,3.2,3.5,4.0,5.0 /
5      DATA TAILR / 1.2,2.4,6.8,12. /
6      DATA THETA / 1.2,3.864,11.4737 /
7
8
9
10     THE FIRST INDEX IS ON WAVELENGTH
11     THE SECOND INDEX IS ON ALTITUDE
12     THE THIRD INDEX IS ON ANGLE
13
14     THE INTERPOLATION (AND EXTRAPOLATION FOR THETA -GT- 85
15     DEGREES AND ALT -LT- 1 KM) IS LINEAR IN (LN(T),SEC(THETA))--
16     (T,ALAM)--, AND (LN(T),ALT)-SPACE. HOWEVER, FOR THETA -GT-
17     85 DEGREES, SEC(THETA) IS REDEFINED BY A PARABOLIC
18     APPROXIMATION TO THE CHAPMAN FUNCTION.
19
20     THE TRANSMISSION IS FROM LOWTRAN III FOR 1962 STD ATMOSPHERE
21
22     THE FOLLOWING TABLE CONTAINS THE TRANSMISSION
23     FROM 1 TO 12KM, 2 TO 12KM ETC., NOT FROM ONE ALTITUDE TO
24     THE TOP OF THE ATMOSPHERE
25
26     FUNCTION TAIR COMPUTES THE TRANSMITTANCE FOR RADIATION OF
27     WAVELENGTH ALAM FROM ALTITUDE ALT TO 12 KM ALONG A PATH AT
28     ZENITH ANGLE THETA.
29
30     INPUT PARAMETERS
31     ARGUMENT LIST
32     ALAM = WAVELENGTH, MICRONS
33     THETA = ZENITH ANGLE, DEGREES
34     ALT = ALTITUDE, KM
35
36     OUTPUT PARAMETER
37     FUNCTION
38     TAIR = TRANSMITTANCE FOR RADIATION OF WAVELENGTH ALAM
39     FROM ALTITUDE ALT TO 12 KM ALONG PATH AT
40     ZENITH ANGLE THETA
41
42     DEFINITION OF DATA
43     T(I,J,K) = TRANSMITTANCE FOR RADIATION OF WAVELENGTH
44     TAILR(I) ALONG PATH AT ZENITH ANGLE THETA(K)=
45     ACOS( 1./STHET(K) ) FROM ALTITUDE TAILR(J) TO
46     12 KM I=1,10 J=1,6 K=1,4
47     THETA(K) = 0.60,75,85 DEGREES K=1,4
48
49     DATA (T(I,1,1),I=1,60) /
50     X .4093,-.2150,.0009,-.0009,-.0001,-.0107,-.2042,-.8398,-.8973,-.4081,
51     X .4690,-.3247,-.0010,-.0010,-.0001,-.0370,-.3038,-.8880,-.9239,-.5183,
52     X .5800,-.5681,-.0232,-.0198,-.0001,-.1893,-.5217,-.9474,-.9568,-.7284,
53     X .6834,-.7758,-.1834,-.1723,-.0043,-.4413,-.7199,-.9744,-.9762,-.8636,
54     X .7788,-.9064,-.5081,-.4649,-.0440,-.7240,-.8549,-.9925,-.9889,-.9479,
55     X .9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999 /
56     DATA (T(I,1,2),I=1,60) /
57     X .2753,-.1063,-.0008,-.0008,-.0001,-.0007,-.0978,-.7645,-.8070,-.2728,
58     X .3313,-.1952,-.0009,-.0009,-.0001,-.0073,-.1753,-.8257,-.8544,-.3863,

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59          X .4151,-.4358,.0033,.0022,.0001,-.0898,.3853,.9150,-.9163,-.6227,
60          X .5648,-.5823,-.0848,-.0765,-.0003,-.3065,-.6127,-.9625,-.9531,-.8081,
61          X .6817,-.8623,-.3792,-.3652,-.0094,-.6060,-.7874,-.9861,-.9733,-.9210,
62          X .9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999 /
63          DATA (T(1,1,3),I=1,60) /
64          X .1151,-.0363,-.0008,-.0008,-.0001,-.0006,-.0338,-.6544,-.6620,-.1559,
65          X .2069,-.0960,-.0008,-.0008,-.0001,-.0007,-.0822,-.7461,-.7401,-.2579,
66          X .3179,-.3065,-.0009,-.0009,-.0001,-.0287,-.2587,-.8683,-.8460,-.5006,
67          X .4347,-.5742,-.0259,-.0224,-.0001,-.1855,-.4908,-.9388,-.9125,-.7328,
68          X .5725,-.8094,-.2502,-.2368,-.0011,-.4807,-.7131,-.9753,-.9549,-.8818,
69          X .9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999 /
70          DATA (T(1,1,4),I=1,60) /
71          X .0330,-.0014,-.0006,-.0006,-.0001,-.0004,-.0017,-.3949,-.3140,-.0344,
72          X .0586,-.0125,-.0007,-.0007,-.0001,-.0004,-.0096,-.5345,-.4282,-.0874,
73          X .1291,-.1208,-.0008,-.0008,-.0001,-.0009,-.0879,-.7463,-.6242,-.2915,
74          X .2294,-.3680,-.0010,-.0009,-.0001,-.0476,-.2729,-.8674,-.7712,-.5590,
75          X .3658,-.6700,-.0828,-.0745,-.0001,-.2725,-.5372,-.9405,-.8768,-.7991,
76          X .9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999,-.9999 /
77          CCC
78          BETA = ANIMI( THETA,(180.-THETA) )
79          STHETA = 1.0 / COS( BETA/57.2958 )
80          FOR BETA .GT. 85 DEGREES, REDEFINE SEC(BETA) BY A SIMPLE
81          PARABOLIC APPROXIMATION TO THE CHAPMAN FUNCTION.
82          CLJ
83          IF( BETA.GT.85. ) STHETA = 1.0 / COS( 85./57.2958 )
84          $
85          IF( BETA.GT.85. ) STHETA = 1.0 / COS( 85./57.2958 )
86          $
87          FIND THE INDEX I FOR THE FIRST TABULAR WAVELENGTH LESS THAN
88          OR EQUAL TO ALAM (USE I=9 IF ALAM=5.0).
89          DO 10 II = 2,10
90          I = II - 1
91          IF(ALAM .LT. TLAM(II))GO TO 15
92          I = 9
93          10 CONTINUE
94          15 CONTINUE
95          CLJ
96          FIND THE INDEX J FOR THE FIRST TABULAR ALTITUDE LESS THAN
97          OR EQUAL TO ALT (BUT ONLY LESS IF ALT=12.0. ALSO, USE J=1 IF
98          ALT .LE. 1.0).
99          DO 20 JJ = 2,6
100          J = JJ - 1
101          IF(ALT .LT. TALT(JJ) ) GO TO 25
102          20 CONTINUE
103          J = 5
104          25 CONTINUE
105          CLJ
106          FIND THE INDEX K FOR THE FIRST TABULAR SEC(THETA) LESS THAN
107          OR EQUAL TO STHETA (BUT USE K=3 IF 85.LE.THETA.LE.90 DEGREES)
108          DO 30 KK = 2,4
109          K = KK - 1
110          IF(STHETA .LT. STHET(KK)) GO TO 35
111          30 CONTINUE
112          K = 3
113          35 CONTINUE
114          H = ALT
115          CLJ
116          FIND THE FRACTIONAL DISTANCE, TLAMX, ALAM LIES BETWEEN
117          TLAM(I) AND TLAM(I+1).
118          TLAMX = (ALAM - TLAM(I)) / (TLAM(I+1) - TLAM(I))

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60      CLJ      MODIFIED DIFFUSION PARAMETERS ARE REQUIRED.  WE ALSO COMPUTE
      CLJ      THE LATTER TYPE AND USE THEM AFTER 9/30/78.
      CCC
      CLJ      SAKDD COMMON
      CLJ      UL,VL,WL = DETECTOR LOS DIRECTION COSINES
      CLJ      XD,YD,ZD = DETECTOR GEOCENTRIC CARTESIAN COORDINATES, KM
      CLJ      XS,YS,ZS = SOURCE GEUCENTRIC CARTESIAN COORDINATES, KM
      CLJ      SOURCE COMMON
      CLJ      NSORCE = NUMBER OF SOURCES BEING CONSIDERED
      CLJ      RSORCE(N) = ALTITUDE OF SOURCE-N
      CLJ      RSORCE(N) = RADIUS OF SOURCE-N, KM
      CLJ      OUTPUT PARAMETER
      CLJ      FUNCTION
      CLJ      TRANSF = THE IRRADIANCE-TO-RADIANCE TRANSFER COEFFICIENT
      CLJ      AT THE TRANSFER POINT, 1/5K
      CLJ      (SEE ABOVE FOR FULLER DESCRIPTION)
      CCC
      CLJ      SINH(ARG) = (EXP(ARG) - EXP(-ARG)) / 2.
      CLJ      COSH(ARG) = (EXP(ARG) + EXP(-ARG)) / 2.
      CLJ      COMMENTS...
      CLJ      THERE ARE 7 LOW-LAYER CLOUDS FOR WHICH THE INDEX IS LL=1,7
      CLJ      THERE ARE 3 MID-LAYER CLOUDS FOR WHICH THE INDEX IS MM=1,3
      CLJ      THERE ARE 4 HI-LAYER CLOUDS FOR WHICH THE INDEX IS HH=1,4
      CLJ      C
      CLJ      LL = 8 MEANS NO LOW CLOUD
      CLJ      MM = 4 MEANS NO MID CLOUD
      CLJ      HH = 5 MEANS NO HI CLOUD
      CLJ      C
      CLJ      EVALUATE LAYER PARAMETERS.  SORALT IS SOURCE ALTITUDE ABOVE
      CLJ      THE GROUND.  COUNT THE NUMBER OF LAYERS, NLAVER, ABOVE THE
      CLJ      SOURCE, INCLUDING THE ONE CONTAINING THE SOURCE.
      CLJ      GET HORIZONTAL DISTANCE OF SOURCE FROM POINT OF
      CLJ      INTERSECTION OF LOS AND CLOUD TOP...RDIST
      CLJ      C
      CLJ      MAKE NO CALCULATIONS FOR SUN BELOW HORIZON
      CLJ      TRANSF = 0.
      CLJ      IF( IFLAG.EQ.0 ) RETURN
      CLJ      DETERMINE INDEX OF CLOUD IN HIGHEST LAYER PRESENT.
      CLJ      KLCLOUD = HH + 10
      CLJ      IF(HH.LT.5) GO TO 4
      CLJ      KLCLOUD = MM + 7
      CLJ      IF(MM.LT.4) GO TO 4
      CLJ      KLCLOUD = LL
      CLJ      4 CLOUDTOP = CLOBASE(KLCLOUD) + CLDTHK(KLCLOUD)
      CLJ      DETERMINE RDIST AND OTHER GEOMETRICAL QUANTITIES FOR
      CLJ      ABOVE-IDENTIFIED CLOUD.
      CLJ      CALL SGEOM(UL,VL,WL,CLOUDTOP,XD,YD,ZD,XS,YS,ZS,
      CLJ      $ RDIST,SDEST,THETI,THETE,PHIE)
      CLJ      SORALT = HSORCE(NSORCE)
      CLJ      AZPU = 0.
      CLJ      NLAVER = 0
      CLJ      SKIP TO 10 IF NO LOW-LAYER CLOUD OR IF IT IS BELOW SOURCE.
      CLJ      IF(LL.GT.7) GO TO 10
      CLJ      IF(SORALT.GT.CLOBASE(LL) + CLDTHK(LL)) GO TO 10
      CLJ      NLAVER = NLAVER + 1
      CLJ      THFN(NLAVER) = CLDTHK(LL)
      CLJ      RESET THKN(NLAVER) BY TRUNCATING PORTION OF CLOUD BELOW SOURCE
      CLJ

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115      IF(SORALT .GT. CLDBASE(LL) ) THKN(NLAYER) = CLDTHK(LL) +
116      CLDBASE(LL) - SORALT
117      AZRO = DISTANCE OF SOURCE BELOW BOTTOM OF LOWEST-ALTITUDE
118      CLOUD LAYER.
119      IF(SORALT .LT. CLDBASE(LL)) AZRO = CLDBASE(LL) - SORALT
120      CORRELATE CLOUD-TYPE DIFFUSION PARAMETERS WITH LAYER DIFFUSION
121      PARAMETERS.
122      DALFAN(NLAYER) = DALFA(LL)
123      DBETAN(NLAYER) = DBETA(LL)
124      DKAPPAN(NLAYER) = DKAPPA(LL)
125      CORRELATE CLOUD-TYPE INDEX WITH LAYER INDEX.
126      LINDEK(NLAYER) = LL
127      SET ALTITUDE OF BOTTOM OF CLOUD NLAYER=1
128      A(NLAYER) = AMAX1(CLDDBASE(LL),SORALT)
129      SET ALTITUDE OF TOP OF CLOUD NLAYER=1
130      A(NLAYER+1) = A(NLAYER) + THKN(NLAYER)
131      CONTINUE
132      SKIP TO 20 IF NO MID-LAYER CLOUD OR IF IT IS BELOW SOURCE.
133      IF(MH.GT. 3) GO TO 20
134      IF(SORALT .GT. CLDBASE(MH+7) + CLDTHK(MH+7) ) GO TO 20
135      NLAYER = NLAYER + 1
136      THKN(NLAYER) = CLDTHK(MH+7)
137      RESET THKN(NLAYER) BY TRUNCATING PORTION OF LAYER BELOW SOURCE
138      IF(SORALT .GT. CLDBASE(MH+7) ) THKN(NLAYER) = CLDTHK(MH+7) +
139      CLDBASE(MH+7) - SORALT
140      IF(SORALT .LT. CLDBASE(MH+7) .AND. NLAYER .EQ. 1)
141      AZRO = CLDBASE(MH+7) - SORALT
142      CORRELATE CLOUD-TYPE DIFFUSION PARAMETERS WITH LAYER DIFFUSION
143      PARAMETERS.
144      DALFAN(NLAYER) = DALFA(MH+7)
145      DBETAN(NLAYER) = DBETA(MH+7)
146      DKAPPAN(NLAYER) = DKAPPA(MH+7)
147      CORRELATE CLOUD-TYPE INDEX WITH LAYER INDEX.
148      LINDEK(NLAYER) = MH + 7
149      SET ALTITUDE OF BOTTOM OF CLOUD NLAYER=1
150      IF(NLAYER .EQ. 1) A(NLAYER) = AMAX1(CLDDBASE(MH+7),SORALT)
151      SET ALTITUDE OF TOP OF CLOUD NLAYER=1
152      A(NLAYER+1) = AMAX1(CLDDBASE(MH+7),SORALT) + THKN (NLAYER)
153      CONTINUE
154      SKIP TO 30 IF NO HIGH-LAYER CLOUD OR IF IT IS BELOW SOURCE.
155      IF(MH .GT. 4) GO TO 30
156      IF(SORALT .GT. CLDBASE(HH+10) + CLDTHK(HH+10) ) GO TO 30
157      NLAYER = NLAYER + 1
158      THKN(NLAYER) = CLDTHK(HH+10)
159      IF(SORALT .GT. CLDBASE(HH+10) ) THKN(NLAYER) = CLDTHK(HH+10) +
160      CLDBASE(HH+10) - SORALT
161      IF(SORALT .LT. CLDBASE(HH+10) .AND. NLAYER .EQ. 1)
162      AZRO = CLDBASE(HH+10) - SORALT
163      DALFAN(NLAYER) = DALFA(HH+10)
164      DBETAN(NLAYER) = DBETA(HH+10)
165      DKAPPAN(NLAYER) = DKAPPA(HH+10)
166      LINDEK(NLAYER) = HH + 10
167      IF(NLAYER .EQ. 1) A(NLAYER) = AMAX1(CLDDBASE(HH+10),SORALT)
168      A(NLAYER+1) = AMAX1(CLDDBASE(HH+10),SORALT) + THKN (NLAYER)
169      CONTINUE
170      CHECK FOR 1,2, OR 3 LAYERS
171      IF THERE IS ONLY ONE LAYER, USE FORMALISM PREVIOUSLY DEVELOPED

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175 C
175 C IF NO LAYERS ABOVE, WE HAVE AN ALBEDO FROM THE TOP LAYER
175 C IN THE LL,NM,HH COMBINATION.
175 C IF(NLAYER.EQ.0) GO TO 400
175 CLJ T1 = THICKNESS OF LAYER-1.
175 CLJ T1 = A(2) - A(1)
175 CLJ RE-LABEL DIFFUSION PARAMETERS FOR LAYER-1.
175 CLJ DAI = DALFAN(1)
175 CLJ DB1 = DBETAN(1)
175 CLJ DK1 = DKAPPAN(1)
175 CLJ IF(NLAYER.EQ.1.AND.AZRO.EQ.0.) T1 = CLDTHK(LINDEX(NLAYER))
175 CLJ IF(NLAYER.EQ.1) GO TO 100
175 CLJ T2 = A(3) - A(2)
175 CLJ SCALE DIFFUSION PARAMETERS BETA AND KAPPA TO ACCOUNT FOR
175 CLJ ADJUSTED THICKNESS OF A HIGHER LAYER MADE CONTIGUOUS WITH A
175 CLJ LOWER LAYER.
175 CLJ NOTE THAT DBETA (THE DIFFUSION COEFFICIENT) IS INVERSELY
175 CLJ PROPORTIONAL TO THE DENSITY (OR PROPORTIONAL TO THE RATIO
175 CLJ THK-NEW TO THK-OLD) AND DKAPPA (THE INVERSE DIFFUSION LENGTH)
175 CLJ IS PROPORTIONAL TO THE DENSITY (OR INVERSELY PROPORTIONAL TO
175 CLJ THE RATIO THK-NEW TO THK-OLD). DALFA IS DIMENSIONLESS AND
175 CLJ REQUIRES NO CHANGE.
175 CLJ DA2 = DALFAN(2)
175 CLJ DB2 = DBETAN(2) * T2 / THKN(2)
175 CLJ DK2 = DKAPPAN(2) * THKN(2) / T2
175 CLJ IF(NLAYER.EQ.2) GO TO 200
175 CLJ T3 = A(4) - A(3)
175 CLJ SCALE DIFFUSION PARAMETERS BETA AND KAPPA TO ACCOUNT FOR
175 CLJ ADJUSTED THICKNESS OF A HIGHER LAYER MADE CONTIGUOUS WITH A
175 CLJ LOWER LAYER.
175 CLJ DA3 = DALFAN(3)
175 CLJ DB3 = DBETAN(3) * T3 / THKN(3)
175 CLJ DK3 = DKAPPAN(3) * THKN(3) / T3
175 CLJ IF(NLAYER.EQ.3) GO TO 300
175 CLJ 100 CONTINUE
175 C
175 C ONE-LAYER USE ORIGINAL FORMALISM
175 C
175 C IF(SORALT.LE.CLDRASE(LINDEX(1))) GO TO 105
175 C FOR SOURCE INSIDE OF THE CLOUD
175 C H = SORALT - CLDRASE(LINDEX(1))
175 C FLUX = 0.
175 C PMIN = 1.E-20
175 C PHAX = 10. / T1
175 C MXP = AMIN1(AMAX1(50.,PHAX*ROIST/6.28*10.),200.)
175 C P = 1.E-10
175 C ANS = 0.
175 C DELTP = (PHAX - PMIN) / MXP
175 C USK1 = SQR(DK1*2 + P*2)
175 C C = 1.
175 C CKT = EXP(USK1 * T1)
175 C CKH = EXP(USK1 * H)
175 C CKA = EXP(USK1*(T1 - H))
175 C SKT = 0.5 *(CKT - 1. / CKT)

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230      CLJ      REDEFINE CKT.
          CKT = 0.5 * (CKT + 1. / CKT)
          SKH = 0.5 * (CKH - 1. / CKH)
231      CLJ      REDEFINE CKH.
          CKH = 0.5 * (CKH + 1. / CKH)
232      CLJ      REDEFINE SKA.
          SKA = 0.5 * (CKA - 1. / CKA)
233      CLJ      REDEFINE SKA.
          SKA = 0.5 * (CKA + 1. / CKA)
234      CLJ      REDEFINE SKA.
          SKA = 0.5 * (CKA - 1. / CKA)
235      CLJ      REDEFINE SKA.
          SKA = 0.5 * (CKA + 1. / CKA)
          ANS = ANS + C * ((DBI*DSKI - DAI) / (DAI*(DBI*DSKI)**2 * 4. *
236      CLJ      1 * ((DAI - DBI*DSKI) * (DAI*SKH + DBI*DSKI*DAI) * SKT))
          2 * ((DAI - DBI*DSKI) * (DAI*SKH + DBI*DSKI*CKH)
237      CLJ      3 * ((DAI + DBI*DSKI) * (DAI*SKA + DBI*DSKI*CKA) * EXP(-DSKI*TI)))
          4 * EXP(-DSKI*(TI-H)) * (DAI + DBI*DSKI) / (DBI*DSKI*2.))
238      CLJ      5 * BESSO(P*RDIST) * P
          C = 2.
239      CLJ      DO 104 I = 1, NWP
          P = P + DELTP
240      CLJ      C = 6. - C
          CKT = EXP(DSKI * TI)
          CKH = EXP(DSKI * H)
          CKA = EXP(DSKI*(TI - H))
241      CLJ      SKT = 0.5 * (CKT - 1. / CKT)
          SKH = 0.5 * (CKH - 1. / CKH)
          CPH = 0.5 * (CKH + 1. / CKH)
          SKA = 0.5 * (CKA - 1. / CKA)
          CKA = 0.5 * (CKA + 1. / CKA)
242      CLJ      ANS = ANS + C * ((DBI*DSKI - DAI) / (DAI*(DBI*DSKI)**2 * 4. *
          1 * ((DAI - DBI*DSKI) * (DAI*SKH + DBI*DSKI*DAI) * SKT))
          2 * ((DAI - DBI*DSKI) * (DAI*SKH + DBI*DSKI*CKH)
243      CLJ      3 * ((DAI + DBI*DSKI) * (DAI*SKA + DBI*DSKI*CKA) * EXP(-DSKI*TI)))
          4 * EXP(-DSKI*(TI-H)) * (DAI + DBI*DSKI) / (DBI*DSKI*2.))
          5 * BESSO(P*RDIST) * P
          104 CONTINUE
          FLUX = ANS * DELTP / 3.
          CHECK UNITS HERE
244      CLJ      GO TO 500
          CONTINUE
          105
          CLJ      CLJ      CONSIDER THE CASE OF A POINT SOURCE BELOW A SINGLE-LAYER
          CLJ      CLOUD.
          CLJ      THE FOLLOWING STEPS EVALUATE THE INTEGRAL IN EQ. (30A) OF THE
          CLJ      CLOUD REPORT. THIS INTEGRAL (HERE GIVEN THE FORTRAN NAME
          CLJ      FLUX), WHEN DIVIDED BY (4.*PI), WILL BE THE TRANSMITTED FLUX
          CLJ      (OR BETTER, RADIANT EXITANCE OR EMITTANCE) FOR A UNIT-LENGTH
          CLJ      SOURCE EMITTING ISOTROPICALLY INTO 4*PI STERADIANS.
          CLJ      FLUX = 1.E-50
          P*IN = 1.E-20
          P*AX = 10. / (TI + AZRO)
          CLJ      LIMIT THE NUMBER OF INTERVALS, NWP, IN THE SIMPSON-INTEGRATION
          CLJ      RULE TO THE RANGE FROM 50 TO 200. NO ATTEMPT IS MADE TO
          CLJ      INSURE THAT NWP IS EVEN.
          CLJ      NWP = AMIN(AMAX(150., P*AX*RDIST/6.28*10.), 200.)
          CLJ      DELTP = (P*AX - P*IN) / NWP
          CLJ      C = 1.003
          CLJ      THE FOLLOWING P IS THE EFFECTIVE P-SUB-0.

```

```

290          P = 1.E-10
          DSK1 = SQRT(DK1**2 + P**2)
          CLJ IF THE ARGUMENT OF THE SINH AND COSH FUNCTIONS EXCEEDS 100,
          CLJ SKIP THE INTEGRATION AND USE THE ABOVE-INITIALIZED VALUE OF
          CLJ FLUX TO SET AN ARBITRARILY SMALL VALUE.
          IF(DSK1 * T1 .GT. 100.) GO TO 111
          AL1 = DB1 * DK1 / DA1
          DD1 = COSH(DSK1*T1) - 0.5*(1./AL1+AL1) * SINH(DSK1*T1)
          AL1 = 0.5*(1./AL1 - AL1) * SINH(DSK1*T1)
          FBAR = EXP(-P * AZRO )
          DENOM = 1. - AL1**2
          CLJ BY USING THE RELATION 1. = (COSH( ))**2 - (SINH( ))**2 IN
          CLJ DENOM, ONE CAN SHOW THAT DD1/DENOM IS THE DENOMINATOR IN THE
          CLJ INTEGRAL BEING EVALUATED.
          SIGMA = DD1 * FBAR / DENOM
          CLJ THE SECOND TERM IN THE FOLLOWING EXPRESSION IS FLUX-SUB-0.
          FLUX = FLUX + SIGMA * BESSO (P*RDIST) * P * C
          C = 2.
          CLJ IN DD-110, THE UPPER LIMIT SHOULD BE NNP-1 IF NNP IS EVEN.
          CLJ THE CONSEQUENCE IS THAT FLUX-SUB-HNP WILL BE GIVEN TWICE THE
          CLJ WEIGHT IT SHOULD HAVE. IF NNP IS ODD, A DIFFERENT (SMALL)
          CLJ ERROR WILL RESULT.
          DO 110 I = 1,NNP
          P = P + DELTP
          C = 6. - C
          DSK1 = SQRT(DK1**2 + P**2)
          IF(DSK1 * T1 .GT. 100.) GO TO 111
          AL1 = DB1 * DK1 / DA1
          DD1 = COSH(DSK1*T1) - 0.5*(1./AL1+AL1) * SINH(DSK1*T1)
          AL1 = 0.5*(1./AL1 - AL1) * SINH(DSK1*T1)
          FBAR = EXP(-P * AZRO )
          DENOM = 1. - AL1**2
          SIGMA = DD1 * FBAR / DENOM
          FLUX = FLUX + SIGMA * BESSO (P*RDIST) * P * C
          110 CONTINUE
          111 FLUX = FLUX * DELTP / 3.
          C CHECK UNITS HERE
          C
          C
          C GO TO 500
          C
          C TWO LAYERS INTEGRATE OVER P
          C
          200 CONTINUE
          FLUX = 1.E-50
          PMIN = 1.E-20
          PMAX = 10. / (T1 + T2 + AZRO)
          NNP = AMIN1(AMAX1(50.,PMAX*RDIST/6.28*10.),200.)
          DELTP = (PMAX - PMIN) / NNP
          C = 1.000
          P = 1.E-10
          DSK1 = SQRT(DK1**2 + P**2)
          DSK2 = SQRT(DK2**2 + P**2)
          IF(DSK1 * DSK2 * T1 * T2 .GT. 100.) GO TO 121
          AL2 = DB2 * DK2 / DA2
          AL1 = DB1 * DK1 / DA1
          DD1 = COSH(DSK1*T1) - 0.5*(1./AL1+AL1) * SINH(DSK1*T1)

```


TRANS	343
TRANS	344
TRANS	345
TRANS	346
TRANS	347
TRANS	348
TRANS	349
TRANS	350
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TRANS	397
TRANS	398
TRANS	399

B-91


```

460      FLUA=CLDRDR(COS(THETI=DTR),COS(THETE=DTR),COS(PHIE=DTR)
      X ,ALAM,KCLOUN)
      TPALT = 12.
      IN COMPUTING SDISTO WE USE THE ORIGINAL ZS, WITHOUT ANY
      CLJ      RESETING IF THE SOURCE IS ARTIFICIAL, EVEN THOUGH ITS
      CLJ      ALTITUDE ABOVE CLDTOP MAY BE LESS THAN ITS RADIUS.
      CLJ      CALL SCEM(U,V,L,VL,TPALT,XD,YD,ZD,XS,YS,ZS,
      X      ROIST,SDISTO,THETI,THETE,PHIE)
      TRANSF = FLUX * TSX * TOX * COS(THETI/57.295) *(SDISTO/SDIST)**2
      RETURN
500 CONTINUE
      CLJ      404 COMPUTE AIR TRANSMITTANCE FOR CASE THAT THE SOURCE IS
      CLJ      BELOW THE HIGHEST CLDTOP.
      THI = 180.-THETI
      T1 = TAIR(ALAM,THI,SORALT)
      T2 = TAIR(ALAM,THI,CLDTOP)
      TSX = T1 / T2
      TPALT = 12.
      CALL SCEM(U,V,L,VL,TPALT,XD,YD,ZD,XS,YS,ZS,
      X      ROIST,SDISTO,THETI,THETE,PHIE)
      TDX = TAIR(ALAM,THETE,CLDTOP)
      TRANSF = FLUX * TSX * TOX / P1 * SDISTO**2
      IF (TRANSF.GE.0.0) GO TO 600
      WRITE(6,550) TRANSF,ROIST
550 FORMAT (*0 WARNING ... WARNING ... WARNING
1 * (SUBROUTINE TRANSF) */
2 *0 THE PROGRAM HAS COMPUTED A NEGATIVE VALUE FOR THE*,
3 * TRANSMITTANCE TRANSFER COEFFICIENT, TRANSF =*,E14.5/,
4 * AT A LATERAL DISPLACEMENT OF ROIST =*,E14.5,*, KM */
5 * THE PROGRAM ALSO TOOK THE ABSOLUTE VALUE OF TRANSF AND*,
6 * PROCESSED NORMALLY, TO FACILITATE THE USER */
7 * MAKING A NOMINAL RYN. THE ABSOLUTE MAGNITUDE OF TRANSF*,
8 * IS LIKELY LESS THAN THE CORRECT VALUE, */
9 * BUT THE RESULTS AT SUCH A LARGE VALUE OF ROIST ARE NOT*/
A * RELIABLE BECAUSE THE INTERNAL INTEGRATION */
B * SCHEME WAS NOT INTENDED TO TREAT SUCH CASES.*)
      TRANSF = ABS( TRANSF )
600 CONTINUE
      CLJ      RETURN
      CLJ      END
495

```

```

1      SUBROUTINE VSNORM(X,Y,Z,EVI,EN2,EN3,K)
2
3      CLJ
4      CLJ
5      CLJ
6      CLJ
7      CLJ
8      CLJ
9      CLJ
10     CLJ
11     CLJ
12     CLJ
13     CLJ
14     CLJ
15     CLJ
16     CLJ
17     CLJ
18     CLJ
19     CLJ
20     CLJ
21     CLJ
22     CLJ
23     CLJ
24     CLJ
25     CLJ
26     CLJ
27     CLJ
28     CLJ
29     CLJ
30     CLJ
31     CLJ
32     CLJ
33     CLJ
34     CLJ
35     CLJ
36     CLJ
37     CLJ

```

SUBROUTINE VSNORM COMPUTES THE COMPONENTS, IN THE K-TH CLOUD-CENTERED CARTESIAN COORDINATE SYSTEM, OF THE UNIT VECTOR NORMAL TO THE ELLIPSOIDAL-SURFACE POINT X,Y,Z.

INPUT PARAMETERS
 ARGUMENT LIST
 X,Y,Z = COORDINATES OF AN ELLIPSOIDAL-SURFACE POINT IN THE K-TH CLOUD-CENTERED CARTESIAN COORDINATE SYSTEM
 K = CLOUD NUMBER

CDCORD COMMON
 FOLLOWING PARAMETERS ARE SET IN SUBROUTINE CLODEOM FOR K=1,10
 ASQ(K) = SQUARE OF LENGTH A, THE SEMI-MAJOR AXIS IN HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2
 BSQ(K) = SQUARE OF LENGTH B, THE SEMI-MINOR AXIS IN HORIZONTAL PLANE OF ELLIPSOIDAL CLOUD, KM**2
 CSQ(K) = SQUARE OF LENGTH C, THE SEMI-MINOR AXIS IN VERTICAL DIRECTION OF ELLIPSOIDAL CLOUD, KM**2

OUTPUT PARAMETERS
 ARGUMENT LIST
 EN1, = COMPONENTS, IN THE K-TH CLOUD-CENTERED CARTESIAN COORDINATE SYSTEM, OF THE UNIT VECTOR NORMAL TO THE ELLIPSOIDAL-SURFACE POINT X,Y,Z.

COMMON/CDCORD/ XI(1,20),ETA(1,20),ZETA(1,20),
 XID(20),ETAD(20),ZETAD(20),CPH(5,20),CTH(5,20)
 2,CPHBAR(16,20),CTHBAR(8,20),CHPAR(4,4,20),CAREA(4,4,20)
 EN1 = X/ASQ(K)
 EN2 = Y / BSQ(K)
 EN3 = Z / CSQ(K)
 R = SQR(EVI**2 + FN2**2 + EN3**2)
 EN1 = EN1 / R
 EN2 = EN2 / R
 EN3 = EN3 / R
 RETURN
 END

APPENDIX C
LISTING OF UPDATE CARDS NECESSARY FOR SAMPLE PROBLEMS

```

*IDENT TPROB1/4
*/   FOR PROGRAM ROSCOER
*INSERT ROSCOER.13
      COMMON/ TPM4 / IFLAG4
      DIMENSION RRR(161), RRTR(161,4)
*DELETE ROSCOER.94
      KKK = 0
      DO 9 J=1,4
      DO 9 I=1,161
      RRTR(I,J) = 0.0
      9 CONTINUE
      7 CONTINUE
      KKK = KKK+1
      IFLAG4 = -2
*DELETE ROSCOER.176
      PIDX2 = PI*DX1/2.0   $   JR = 161
      DO 301 I=1,JR
*DELETE ROSCOER.182
*INSERT ROSCOER.188
      RRR(I) = X
      RRTR(I,KKK) = T4
*DELETE ROSCOER.192,ROSCOER.194
*DELETE ROSCOER.206,ROSCOER.208
*INSERT ROSCOER.211
      WRITE(6,103)
103  FORMAT (1H1,* RANGE *,* SC AC CI *,
$ * SC-AC-CI *,* INT( SC ) INT( AC ) INT( CI ) *,
$ * INT(TOTAL) *)
      RSM1 = 0.0 $ RSM2 = 0.0 $ RSM3 = 0.0 $ RSM4 = 0.0
      WRITE(6,105) RRR(1),(RRTR(1,J),J=1,4),RSM1,RSM2,RSM3,RSM4
105  FORMAT (1X,F8.2,4E12.4,4E14.6)
      DO 110 I=2,JR
      RSM1 = RSM1 + PIDX2*( RRR(I)*RRTR(I,1) + RRR(I-1)*RRTR(I-1,1) )
      RSM2 = RSM2 + PIDX2*( RRR(I)*RRTR(I,2) + RRR(I-1)*RRTR(I-1,2) )
      RSM3 = RSM3 + PIDX2*( RRR(I)*RRTR(I,3) + RRR(I-1)*RRTR(I-1,3) )
      RSM4 = RSM4 + PIDX2*( RRR(I)*RRTR(I,4) + RRR(I-1)*RRTR(I-1,4) )
      WRITE(6,105) RRR(I),(RRTR(I,J),J=1,4),RSM1,RSM2,RSM3,RSM4
110  CONTINUE
*/   FOR SUBROUTINE DIFPRM
*INSERT DIFPRM.81
      DATA IF1234 / -1 /
*DELETE DIFPRM.105
      IF( IF1234 .GT. 0 ) GO TO 111
*DELETE DIFPRM.124
      IF( IF1234 .GT. 0 ) GO TO 27
*DELETE DIFPRM.149
      IF( IF1234 .GT. 0 ) GO TO 29
*INSERT DIFPRM.156
      IF1234 = +2
*/   FOR SUBROUTINE SCLOUD
*INSERT SCLOUD.157
      E4 = EMISS(1)
      IF( ISUN.EQ.0 ) T4 = TRANS(1)
      IF( ISUN.EQ.1 ) S4 = TRANS(1)
      HSORCE(1) = HSAVE

```

Figure C-1. Update IDENT for Problems 1 to 4.

```

      GO TO 30
*/    FOR FUNCTION TRANSF
*BEFORE TRANS.9
      COMMON/ TP44 / IFLAG4
*INSERT TRANS.11
      DATA KCLDZ / 0 /
*INSERT TRANS.101
      IF( KCLOUD.EQ.KCLDZ ) GO TO 6
      KCLOZ = KCLOUD
      PRODKL = DKAPPA(KCLOUD) * CLDTHK(KCLOUD)
      ADIVKB = DALFA(KCLOUD) / (DKAPPA(KCLOUD)*DBETA(KCLOUD))
      T = 1.0 / (COSH(PRODKL) + 0.5*(ADIVKB + 1.0/ADIVKB)*SINH(PRODKL))
      WRITE(6,13) KCLOUD, T
      13 FORMAT (*0 TOTAL TRANSMISSION FOR KCLOUD = *,I4,* IS *,E12.4)
      6 CONTINUE
*INSERT TRANS.386
CLJ   THE MAIN PROGRAM INITIALIZES IFLAG4 TO A NEG. VALUE.
      IF( IFLAG4.GT.0 ) GO TO 1301
CLJ   FOR SAMPLE PROBLEM NO. 4 WE WANT TO EVALUATE THE ANALYTIC
CLJ   EXPRESSION FOR THE TOTAL (SPATIALLY-INTEGRATED) TRANSMITTANCE
CLJ   THROUGH THREE LAYERS ABOVE A POINT SOURCE.
CLJ   FIRST, EVALUATE THE TRANSMITTANCE S AND REFLECTANCE R FOR EACH
CLJ   OF THE THREE LAYERS SEPARATELY, PER EQS. (31A) AND (31B) IN
CLJ   CLOUD REPORT APPENDIX A.
      DK1T1 = DK1*T1
      DK2T2 = DK2*T2
      DK3T3 = DK3*T3
      HSKT1 = SINH(DK1T1)
      HSKT2 = SINH(DK2T2)
      HSKT3 = SINH(DK3T3)
      S1 = 1.0/( COSH(DK1T1) + 0.5*(1./AL1 + AL1)*HSKT1 )
      S2 = 1.0/( COSH(DK2T2) + 0.5*(1./AL2 + AL2)*HSKT2 )
      S3 = 1.0/( COSH(DK3T3) + 0.5*(1./AL3 + AL3)*HSKT3 )
      R1 = S1*0.5*(1./AL1 - AL1)*HSKT1
      R2 = S2*0.5*(1./AL2 - AL2)*HSKT2
      R3 = S3*0.5*(1./AL3 - AL3)*HSKT3
CLJ   NOW EVALUATE THE TOTAL TRANSMITTANCE FOR THE THREE-LAYER
CLJ   CASE, S123.
      S123 = S1*S2*S3/( (1.-R1*R2)*(1.-R2*R3) - R1*R3*S2*S2 )
      IFLAG4 = +2
      WRITE(6,1300) S1,S2,S3,R1,R2,R3,S123
      1300 FORMAT (*0 TRANSMITTANCES AND REFLECTANCES FOR EACH OF THREE*,
1 * CLOUDS ARE...*/ * T1,T2,T3 =*,3E14.5/* R1,R2,R3 =*,3E14.5/
2 *0 TRANSMITTANCE FOR THREE-LAYER COMBINATION IS...*,
3 * T123 =*,E14.5)
      1301 CONTINUE
*DELETE TRANS.390
*DELETE TRANS.413
*DELETE TRANS.478
      TRANSF = FLUX / PI
*DELETE TRANS.480
*DELETE TRANS.493

```

Figure C-1. (Continued)


```

*IDENT TPROB/5
*/   FOR PROGRAM ROSCOER
*DELETE ROSCOER.176
DO 301 I=1,1
*DELETE ROSCOER.201
*/   FOR SUBROUTINE CLDWT
*INSERT CLDWT.7
DIMENSION LLMH(160,3),ZCFLOS(160,4)
*INSERT CLDWT.123
LLMH(IDX,1) = LL $ LLMH(IDX,2) = MM $ LLMH(IDX,3) = HH
ZCFLOS(IDX,II-1) = PIJKL*(1.0-CFLOS)
*INSERT CLDWT.138
LLMH(IDX,1) = LL $ LLMH(IDX,2) = MM $ LLMH(IDX,3) = HH
ZCFLOS(IDX,II-1) = PIJKL*(1.0-CFLOS)
*INSERT CLDWT.153
LLMH(IDX,1) = LL $ LLMH(IDX,2) = MM $ LLMH(IDX,3) = HH
ZCFLOS(IDX,II-1) = PIJKL*(1.0-CFLOS)
*INSERT CLDWT.173
LLMH(IDX,1) = LL $ LLMH(IDX,2) = MM $ LLMH(IDX,3) = HH
ZCFLOS(IDX,II-1) = PIJKL*(1.0-CFLOS)
*INSERT CLDWT.191
LLMH(IDX,1) = LL $ LLMH(IDX,2) = MM $ LLMH(IDX,3) = HH
ZCFLOS(IDX,II-1) = PIJKL*(1.0-CFLOS)
*INSERT CLDWT.209
LLMH(IDX,1) = LL $ LLMH(IDX,2) = MM $ LLMH(IDX,3) = HH
ZCFLOS(IDX,II-1) = PIJKL*(1.0-CFLOS)
*INSERT CLDWT.228
LLMH(IDX,1) = LL $ LLMH(IDX,2) = MM $ LLMH(IDX,3) = HH
ZCFLOS(IDX,II-1) = PIJKL*(1.0-CFLOS)
*BEFORE CLDWT.233
WRITE(6,303)
303 FORMAT (2H1,* IDX LL MM HH *,* TRANS EMISS *,*,
$ * CC=2 CC=3 CC=4 CC=5 WT *,*,
$ * WT(SUM) *)
RSUM = 0.0
DO 310 IX=1,160
RSUM = RSUM + WT(IX)
WRITE(6,305) IX,(LLMH(IX,I),I=1,3),TRANS(IX),EMISS(IX),
$ (ZCFLOS(IX,I),I=1,4),WT(IX),RSUM
305 FORMAT (2X,4I4,2X,8E12.4)
310 CONTINUE
*/   FOR SUBROUTINE DIFPRM
*DELETE DIFPRM.105
*DELETE DIFPRM.124
*DELETE DIFPRM.149
*/   FOR SUBROUTINE SCLOUD
*INSERT SCLOUD.254
WRITE(6,103) IDX,TRANS(160),EMISS(160),WT(160)
103 FORMAT (2H0,4X,* IDX = *,I5,5X,* TRANS(160) = *,E12.4,5X,
$ * EMISS(160) = *,E12.4,5X,* WT (160) = *,E12.4)
*INSERT SCLOUD.260
WRITE(6,111) SLGCLO,SLGCCLR,SFR,THI,TI2,T2TP,RDIST,SDISTO,
$ THETI,THETE,PHIE
111 FORMAT (*0 SLGCLO,SLGCCLR,SFR,THI,TI2,T2TP,RDIST,SDISTO,*,
$ *THETI,THETE,PHIE*,/(5X,6E12.4))
WRITE(6,113) (TRANS(I),WT(I),I=1,II)
WRITE(6,115) (EMISS(I),WT1(I),I=1,II)
113 FORMAT (*0 TRANS,WT =*/(5X,8E12.4))
115 FORMAT (*0 EMISS,WT1 =*/(5X,8E12.4))
*INSERT SCLOUD.266
WRITE(6,117) (WT(I),WT1(I),I=1,II)
117 FORMAT (*0 WT,WT1 =*/(5X,8E12.4))

```

Figure C-2. Update IDENT for Problem 5.

```

*IDENT TPROB/6
*/   FOR PROGRAM ROSCOER
*INSERT ROSCOER.13
      COMMON/XX0000/  XCC(64),YCC(64),ZCC(64)
*DELETE ROSCOER.17
      DATA SOLLAT, SOLLON / 0.0, -0.785398 /
*DELETE   ROSCOER.139,ROSCOER.140
      IF( I.EQ.1 ) WRITE(6,123)
123 FORMAT (*1CLOUD  ALAM      TCOEF      EMISS      XCC      *,
1 *      YCC      ZCC      *)
      WRITE(6,125)  KCLOUD(K),ALAM,TCOEF,TEMISS,XCC(I),YCC(I),ZCC(I)
125 FORMAT (1X,I5,F8.2,E12.4,E12.4,3E12.4)
*/   FOR SUBROUTINE CLOUD2
*DELETE CLOUD2.72
*DELETE CLOUD2.84
*DELETE CLOUD2.96
*/   FOR SUBROUTINE CLOUD3
*DELETE CLOUD3.185
*DELETE   CLOUD3.216,CLOUD3.217
*/   FOR SUBROUTINE DIFFUS
*DELETE DIFFUS.143
*DELETE DIFFUS.165
*DELETE DIFFUS.222
*/   FOR SUBROUTINE LOS
*BEFORE LOSK.67
      COMMON/XX0000/  XCC(64),YCC(64),ZCC(64)
*INSERT LOSK.118
      XCC(L) = 0.0
      YCC(L) = 0.0
      ZCC(L) = 0.0
*INSERT LOSK.153
      XCC(LL) = XX(IC,JC)
      YCC(LL) = YY(IC,JC)
      ZCC(LL) = ZZ(IC,JC)
*INSERT LOSK.203
      XCC(LL) = XX(IC,JC)
      YCC(LL) = YY(IC,JC)
      ZCC(LL) = ZZ(IC,JC)
*INSERT LOSK.245
      XCC(LL) = XX(IC,JC)
      YCC(LL) = YY(IC,JC)
      ZCC(LL) = ZZ(IC,JC)

```

Figure C-3. Update IDENT for Problem 6.

APPENDIX D
TRANSMITTANCE AND REFLECTANCE OF TWO- AND THREE-LAYER PLANAR SLABS

To help validate the code it is valuable to compare the code's results with information obtained by other means. One type of calculation performed by the code is the computation of the photon flux emerging from one-, two-, and three-layer slabs at a given lateral displacement from the vertical through the point source below the slabs.

Sample Problems 1 to 3 in Section 4-3 are for one-layer slabs and Problem 4 is for a three-layer slab. To provide a check on the code's operation for Problems 1 to 3, we used Equation (32a) in Appendix A for the spatially-integrated transmittance of a planar slab. By performing a spatial integration of the code-computed flux, we compared the code's result with the analytic result in Equation (32a). Problem 4, with its three layers, is more complicated. Hence, we need another exact, analytic expression for the transmittance of three layers, given the transmittance and reflectance of each of the three separate layers. We derive such a formula here; it is applied in Section 4-3.1.

The approach is to derive formulas for the transmittance and reflectance of two layers and then to apply the two-layer formulas to the three-layer configuration. The derivation is greatly facilitated by drawing an appropriate diagram, such as that in Figure D-1. The total transmitted flux is seen to be a geometric series:

$$\begin{aligned} T_{12} &= T_2 T_1 [1 + R_2 R_1 + (R_2 R_1)^2 + (R_2 R_1)^3 + \dots] \\ &= \frac{T_2 T_1}{1 - R_2 R_1} \end{aligned} \quad (1)$$

Similarly, the reflectance from the lower layer includes a geometric series:

$$\begin{aligned} R_{12} &= R_1 + T_1^2 R_2 [1 + R_2 R_1 + (R_2 R_1)^2 + (R_2 R_1)^3 + \dots] \\ &= R_1 + \frac{T_1^2 R_2}{1 - R_2 R_1} \end{aligned} \quad (2)$$

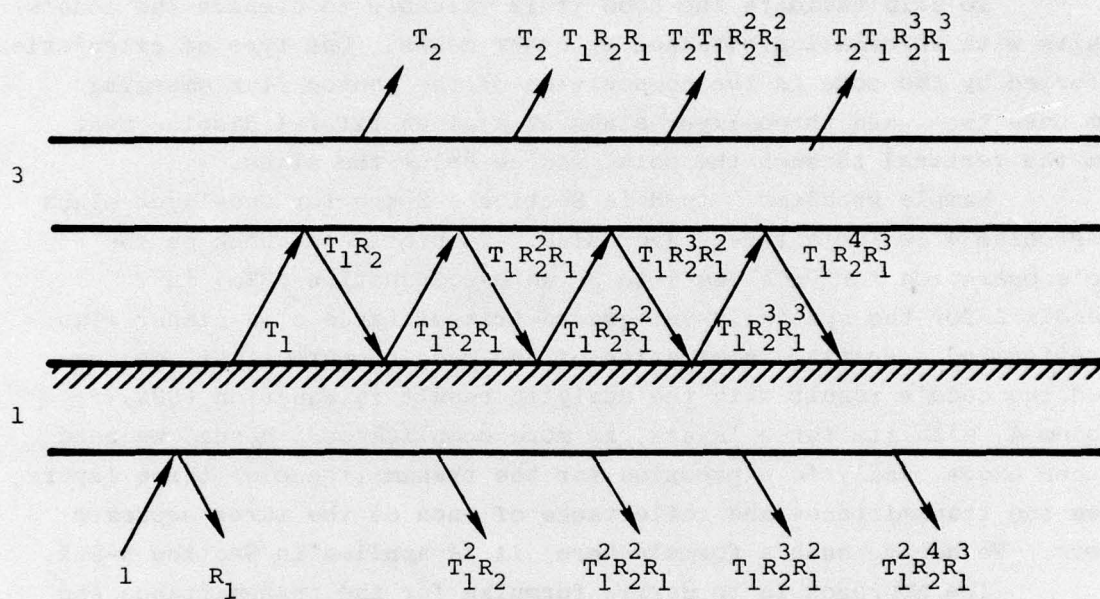


Figure D-1. Illustration of contributions to transmitted and reflected fluxes for a two-layer configuration.

Note that Equation (1) for the transmittance is symmetric in the indices 1 and 2 whereas Equation (2) for the reflectance is not symmetric.

If one makes the assumption of conservative scattering (i.e., no absorption), so that

$$T_1 + R_1 + 1$$

$$T_2 + R_2 = 1 ,$$

then one can show that the reflectance is symmetric, i.e.,

$$R_{12} = R_{21} = \frac{R_1 + R_2 - 2R_1R_2}{1 - R_1R_2}$$

and that

$$T_{12} + R_{12} + 1 .$$

For three layers, consider Figure D-2 where we denote the pair of Layers 1 and 2 as Layer A and Layer 3 as Layer B. The symbol R_{A+} denotes the net reflectance for flux incident on the Layer-1 side of Layer A and R_{A-} denotes the net reflectance for flux incident on the Layer-2 side of Layer A.

The transmittance for flux incident on the Layer-1 side is

$$T_{AB} = T_B T_A [1 + R_B R_{A-} + (R_B R_{A-})^2 + \dots]$$

$$= \frac{T_B T_A}{1 - R_B R_{A-}} .$$

The reflectance for flux incident on the Layer-1 side is

$$R_{AB} = R_{A+} + T_A^2 R_B [1 + R_B R_{A-} + (R_B R_{A-})^2 + \dots]$$

$$= R_{A+} + \frac{T_A^2 R_B}{1 - R_B R_{A-}} .$$

By using the expressions

$$T_A = \frac{T_2 T_1}{1 - R_2 R_1}$$

$$T_B = T_3$$

$$R_{A+} \equiv R_{12} = R_1 + \frac{T_1^2 R_2}{1 - R_2 R_1}$$

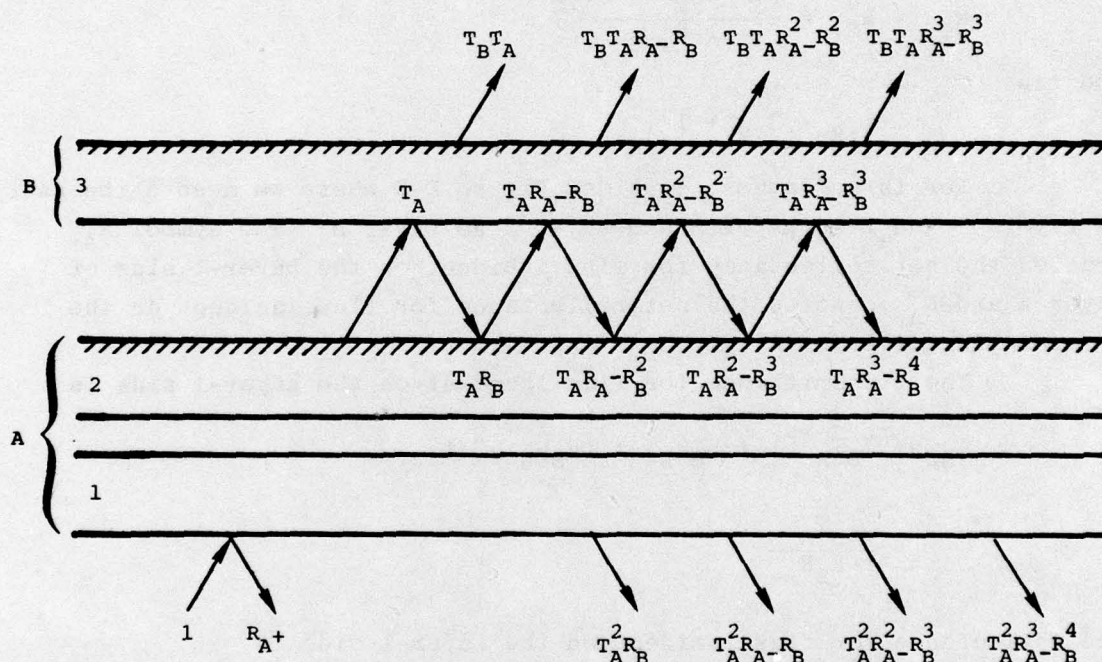


Figure D-2. Illustration of contributions to transmitted and reflected fluxes for a three-layer configuration expressed in terms of those for a two-layer configuration.

$$R_{A-} \equiv R_{21} = R_2 + \frac{T_2^2 R_1}{1 - R_1 R_2}$$

$$R_B = R_3$$

we find

$$T_{123} \equiv T_{AB} = \frac{T_3 T_2 T_1}{1 - R_2 R_1} \frac{1}{1 - R_3 \left[R_2 + \frac{T_2^2 R_1}{1 - R_1 R_2} \right]}$$

$$T_{123} = \frac{T_3 T_2 T_1}{(1 - R_2 R_1) (1 - R_3 R_2) - T_2^2 R_3 R_1}$$

which is symmetric with respect to an interchange of the 1 and 3 and hence is valid for the source irradiating either Layer 1 or Layer 3.

The reflectance R_{123} for a source below Layer 1 is

$$\begin{aligned} R_{123} \equiv R_{AB} &= R_{A+} + \frac{T_A^2 R_B}{1 - R_B R_{A-}} \\ &= R_1 + \frac{T_1^2 R_2}{1 - R_2 R_1} + \frac{\left(\frac{T_2 T_1}{1 - R_2 R_1} \right)^2 R_3}{1 - R_3 \left[R_2 + \frac{T_2^2 R_1}{1 - R_1 R_2} \right]} \\ &= \frac{R_1 (1 - R_2 R_1) + T_1^2 R_2}{1 - R_2 R_1} \\ &\quad + \frac{\frac{(T_2 T_1)^2}{1 - R_2 R_1} R_3}{(1 - R_3 R_2) (1 - R_2 R_1) - T_2^2 R_3 R_1} \end{aligned}$$

whereas the reflectance R_{321} for a source above Layer 3 is

$$R_{321} \equiv R_{BA} = R_B + \frac{T_B^2 R_{A-}}{1 - R_B R_{A-}}$$

$$= R_3 + \frac{T_3^2 \left(R_2 + \frac{T_2^2 R_1}{1 - R_1 R_2} \right)}{1 - R_3 \left[R_2 + \frac{T_2^2 R_1}{1 - R_1 R_2} \right]} .$$

One can show that for conservative scattering, i.e.,

$$T_i + R_i = 1 \quad \text{for } i = 1, 2, 3 ,$$

that

$$R_{123} = R_{321}$$

and

$$T_{123} + R_{123} = 1 .$$

Finally, in Figure D-3 we illustrate the enhanced effective transmission of a single layer due to a reflecting surface located below the source. Let T be the transmittance of the layer without the reflecting surface. With the reflecting surface present, there are two contributions to the transmittance:

$$T_1 = T + TR^2 + TR^4 + \dots = T / (1 - R^2)$$

$$T_2 = TR + TR^3 + TR^5 + \dots = TR / (1 - R^2)$$

$$T_1 + T_2 = T(1 + R) / (1 - R^2) = T / (1 - R) .$$

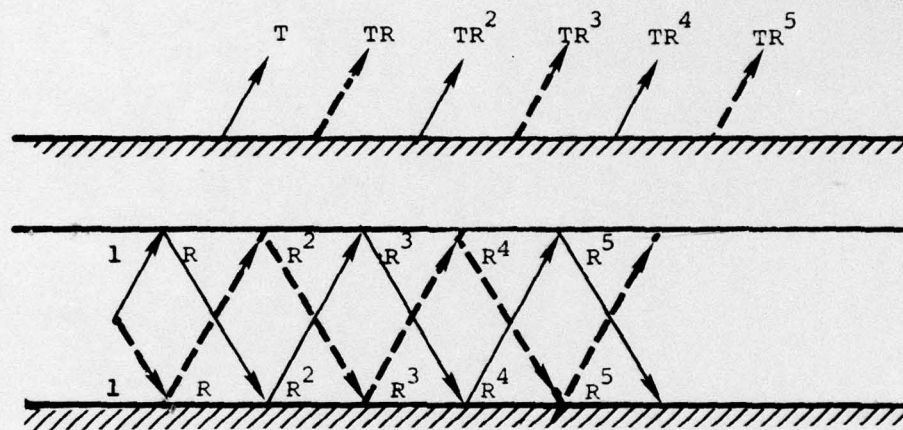


Figure D-3. Illustration of enhanced effective transmission of a single layer due to a reflecting surface.

The factor of increased transmittance due to the reflecting surface is

$$\frac{T_1 + T_2}{T} = \frac{1}{1-R} ,$$

a result stated in Section 2-2.

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